

# Quantum CCA-Secure PKE, Revisited

Varun Maram

Cybersecurity Group

SandboxAQ



: <https://varun-maram.github.io/>

: varun-maram-pqc

Joint work with Navid Alamat

**ETH** zürich

 **SANDBOXAQ**

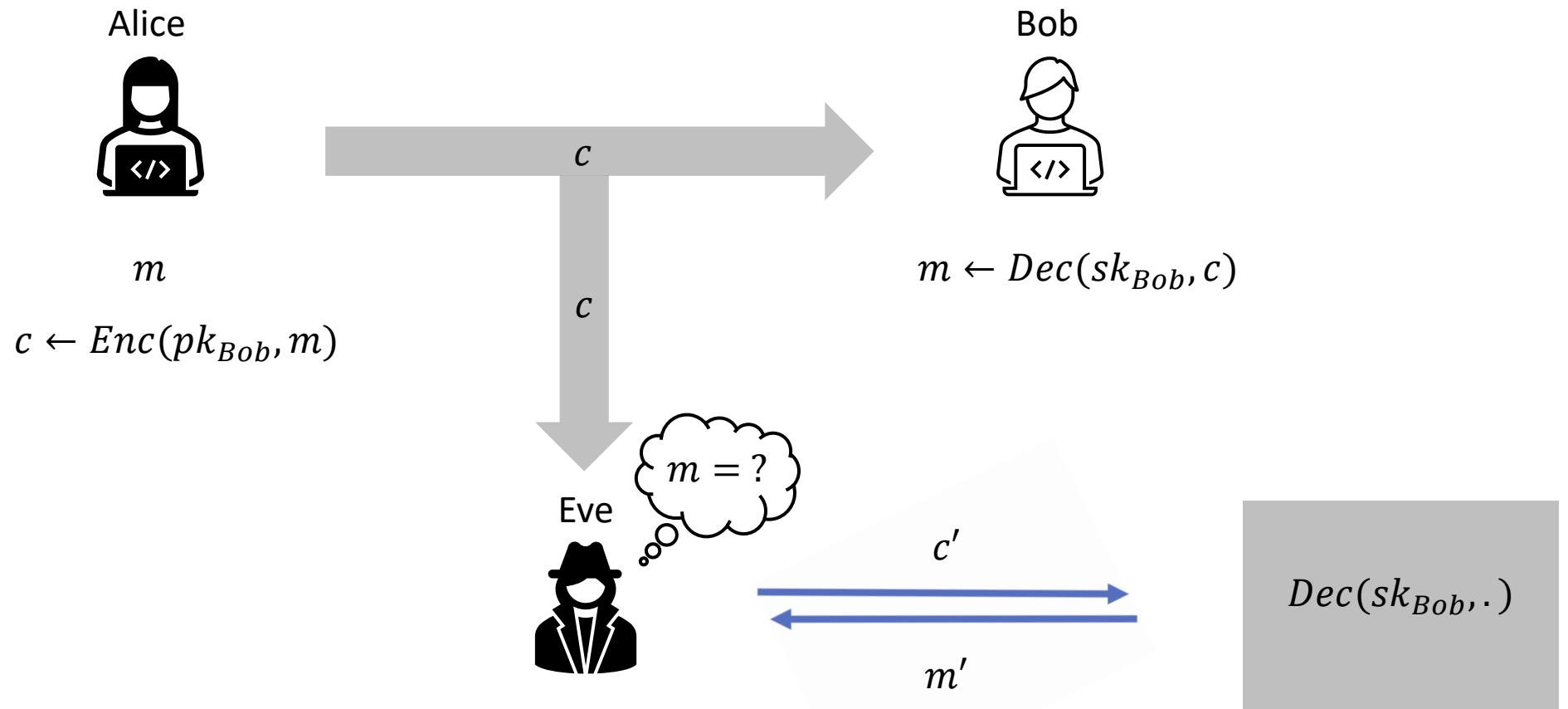
**VISA**

# Quantum CCA-Secure PKE, Revisited

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# IND-CCA Security

$$PKE = (KGen, Enc, Dec)$$

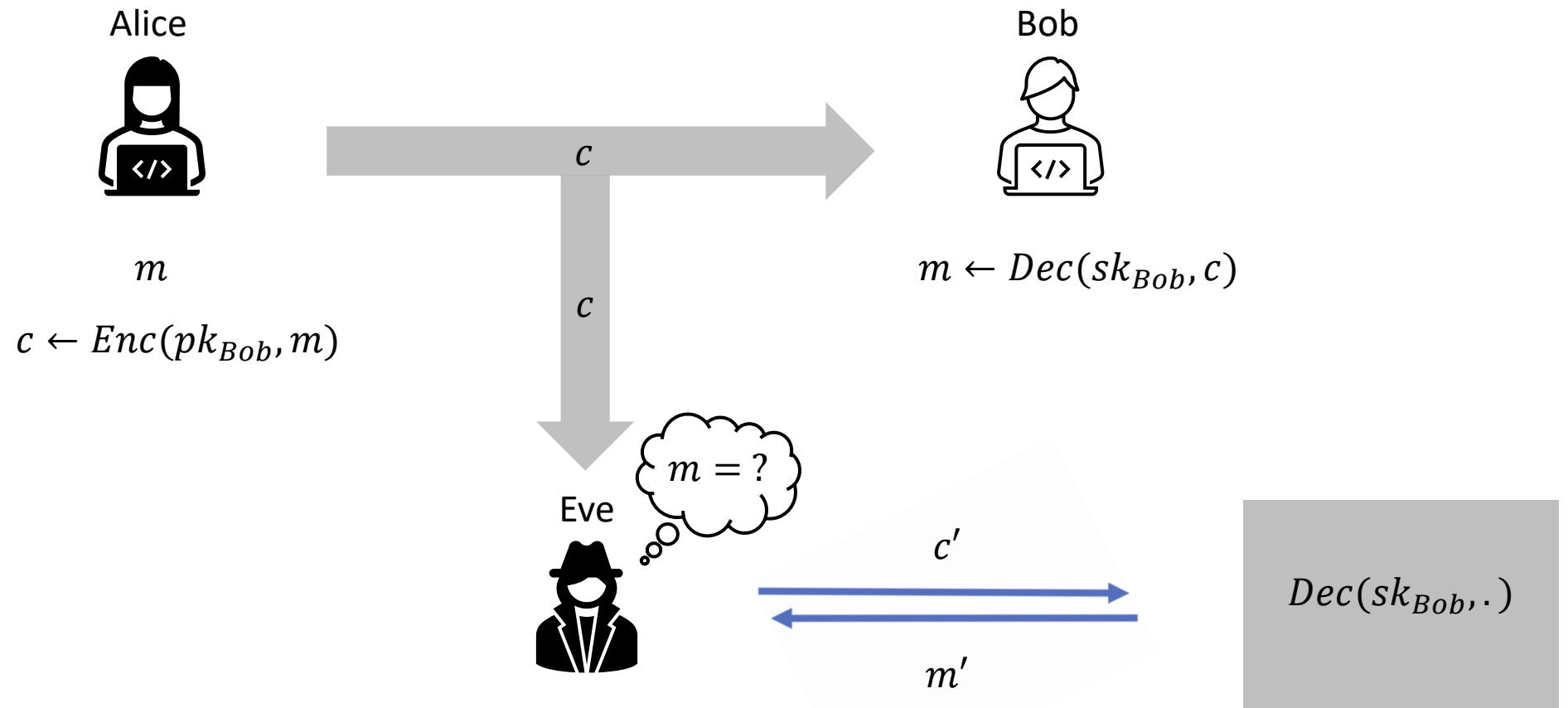


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# IND-CCA Security

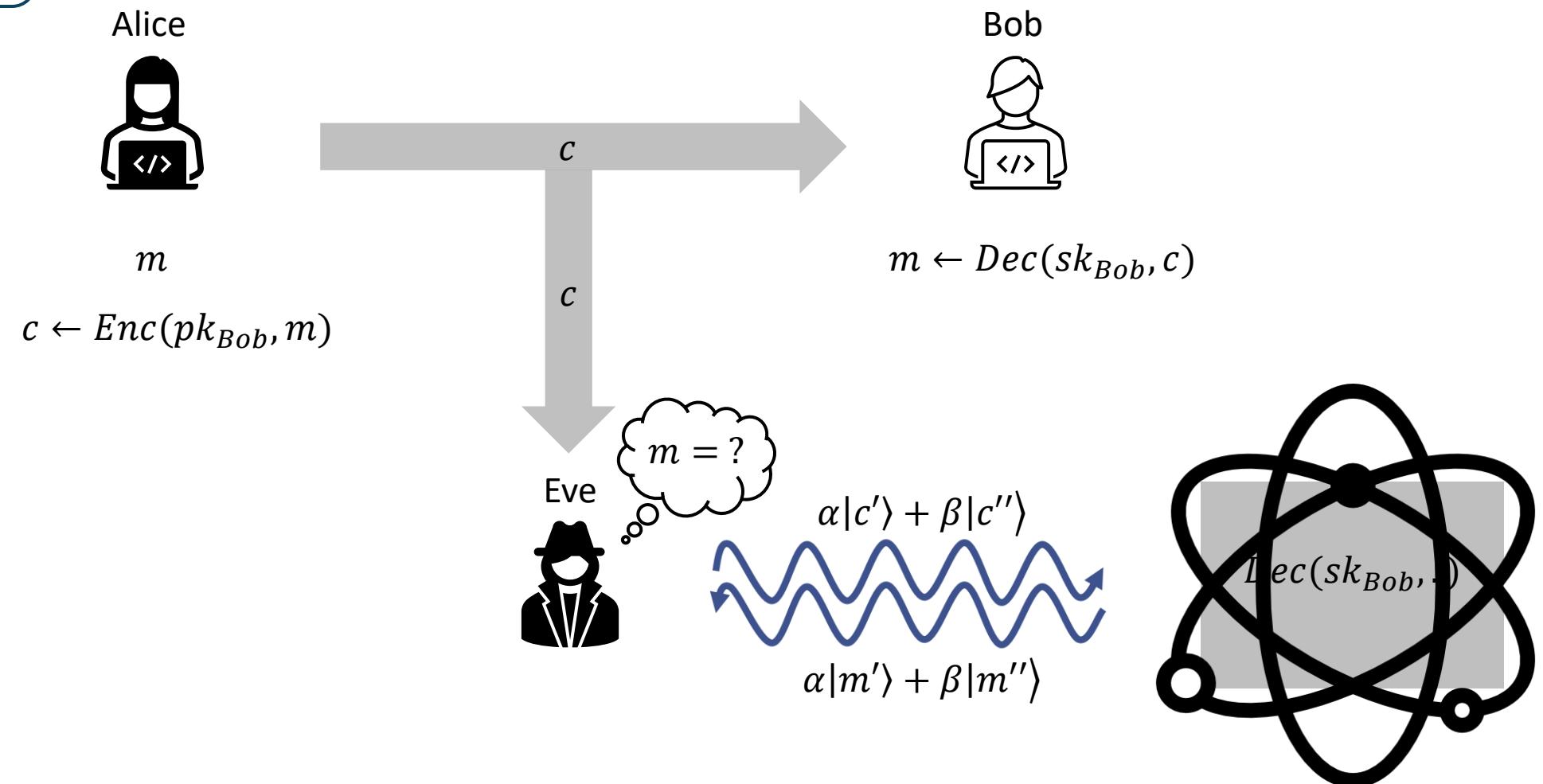
$$PKE = (KGen, Enc, Dec)$$



# IND-qCCA Security

Introduced by [Boneh-Zhandry'13].

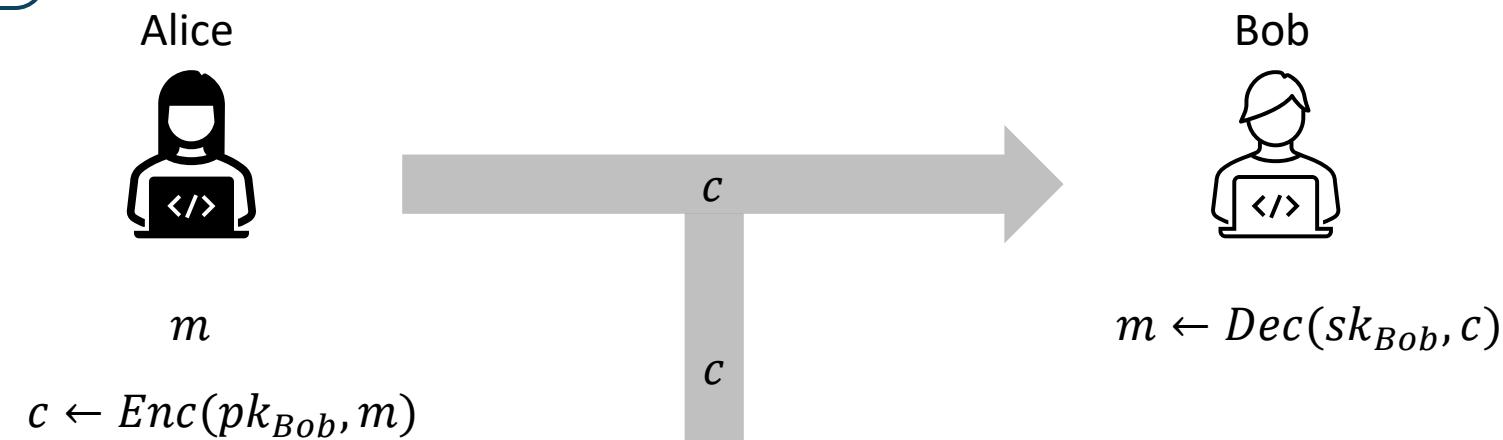
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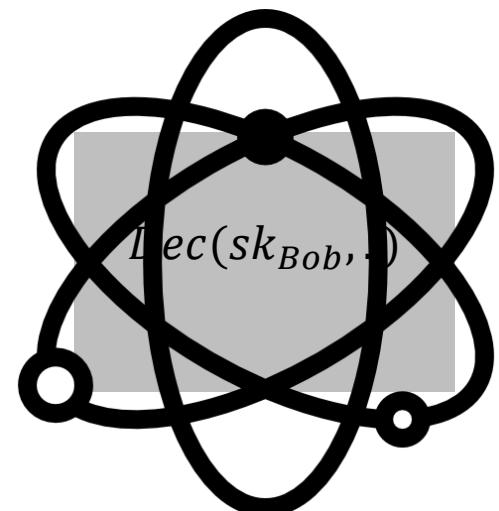
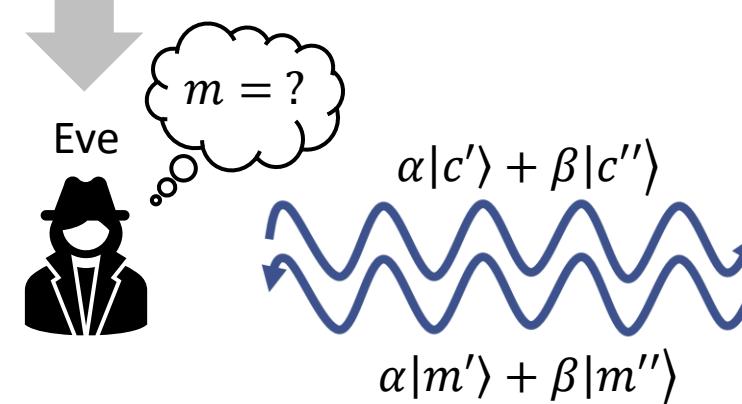
# IND-qCCA Security

Introduced by [Boneh-Zhandry'13].

$$PKE = (KGen, Enc, Dec)$$



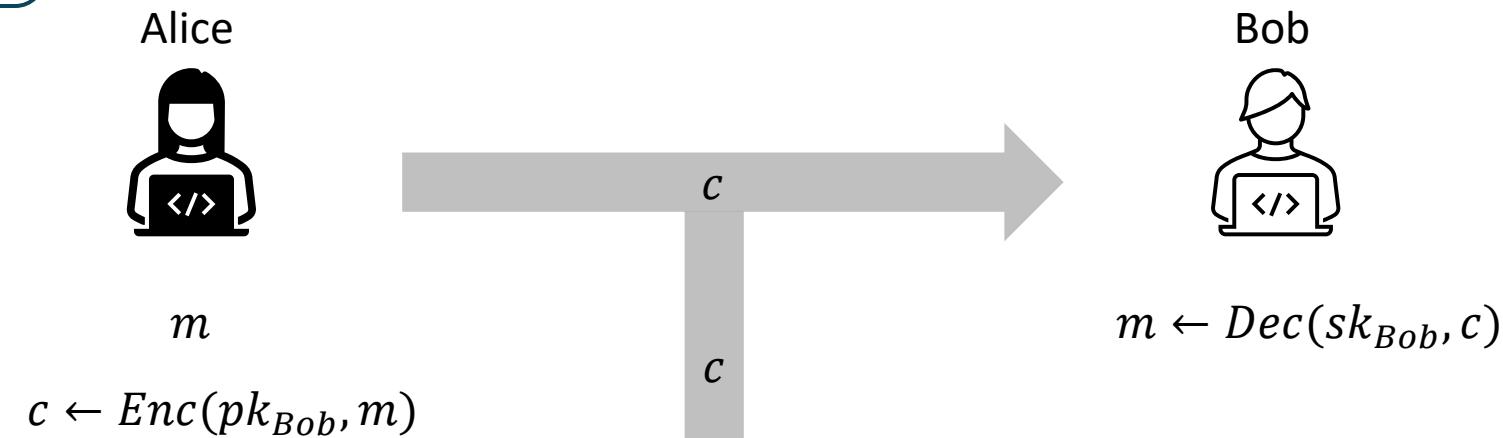
- Relevance in future when quantum computing becomes ubiquitous.



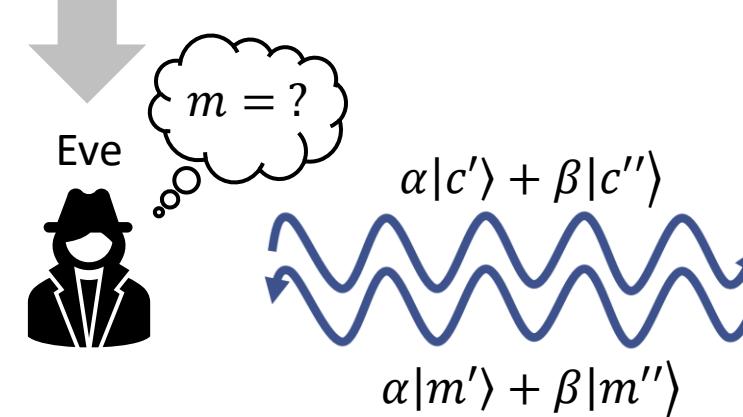
# IND-qCCA Security

Introduced by [Boneh-Zhandry'13].

$$PKE = (KGen, Enc, Dec)$$



- Relevance in future when quantum computing becomes ubiquitous.
- Also, in not-so-far future when adversaries can trick classical devices to behave “quantumly” (e.g., “frozen smart-card attacks”).



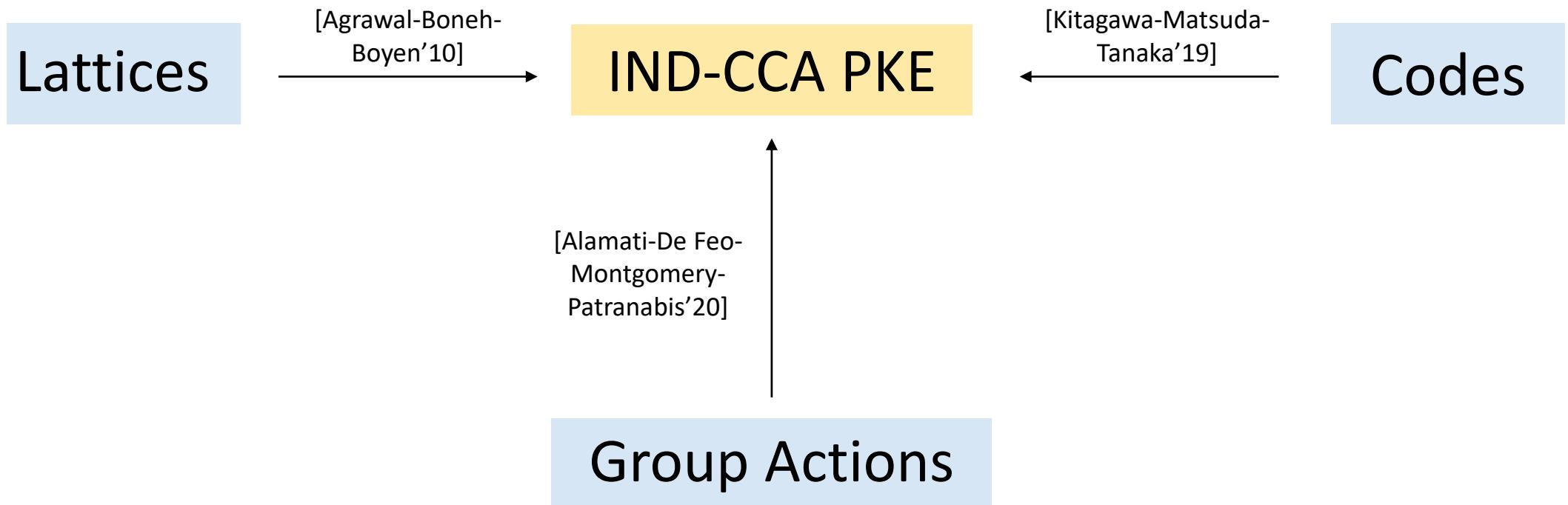
# Quantum CCA-Secure PKE, Revisited

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# Motivation

IND-CCA PKE

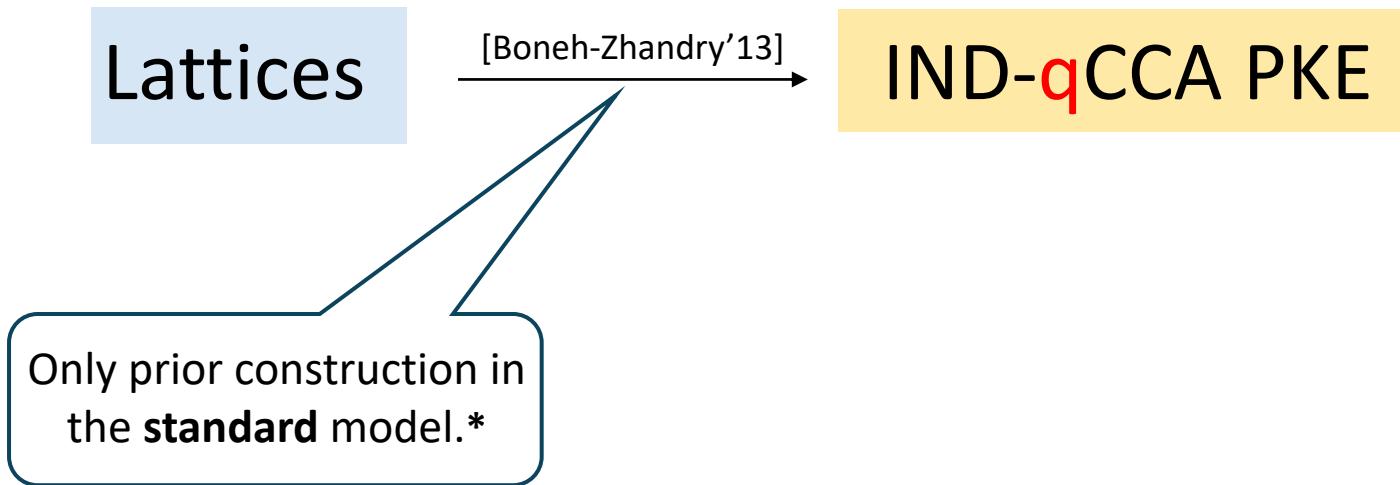
# Motivation



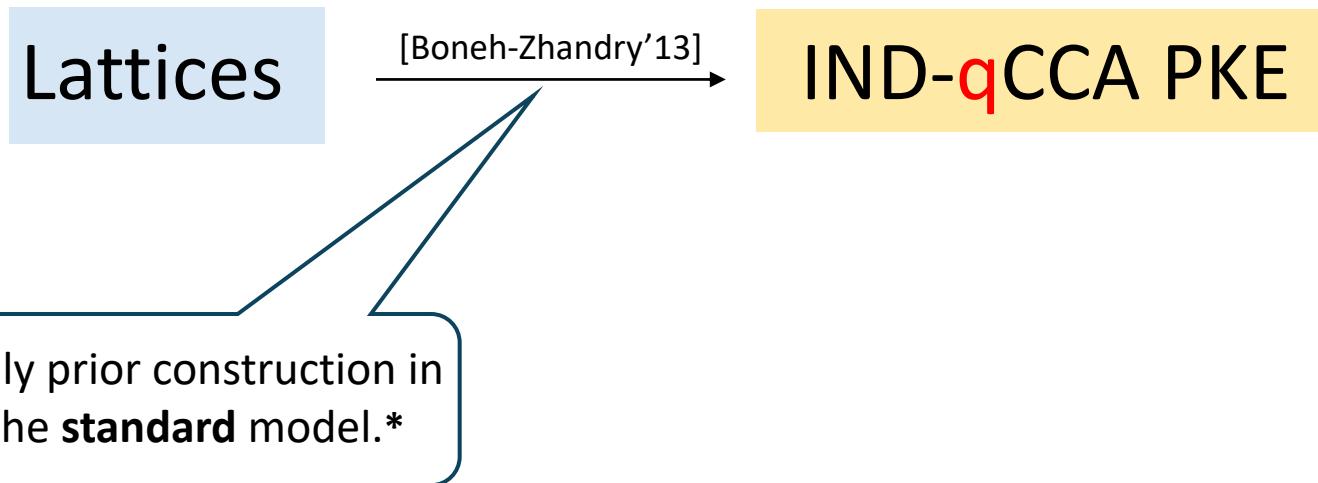
# Motivation

IND-**q**CCA PKE

# Motivation

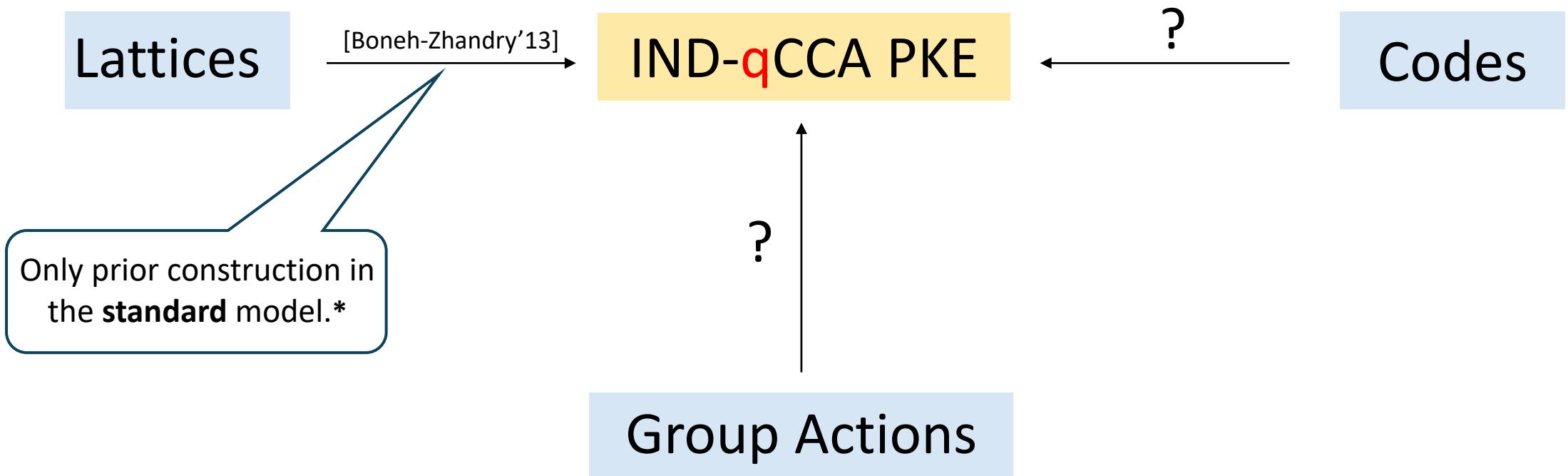


# Motivation

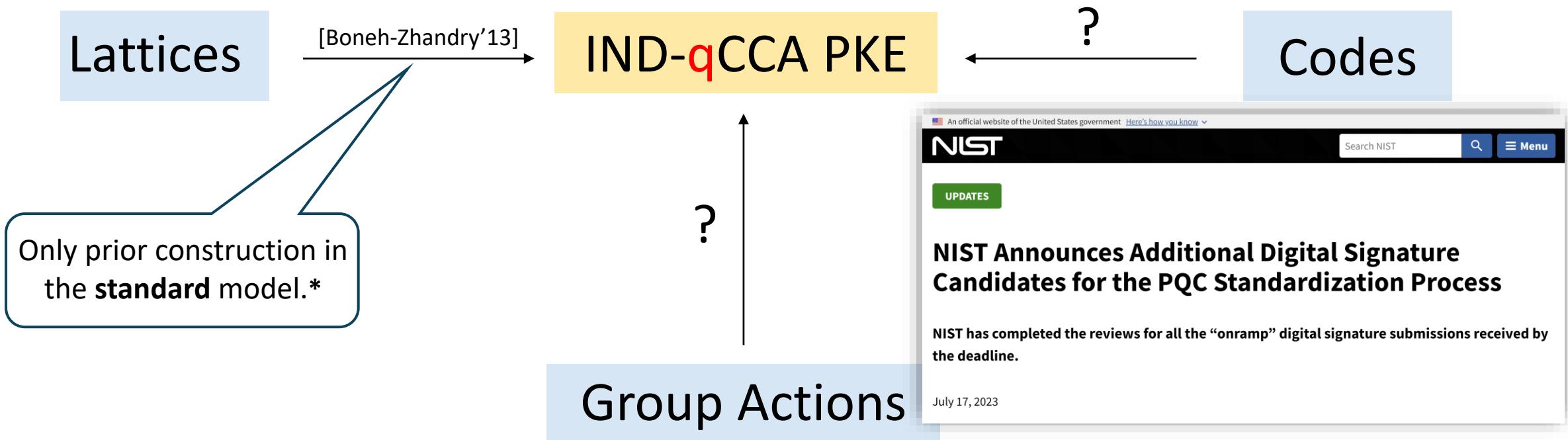


\*There exist richer constructions of qCCA-secure PKE in the idealized **quantum ROM** – e.g., by [Xagawa-Yamakawa'19].

# Motivation



# Motivation

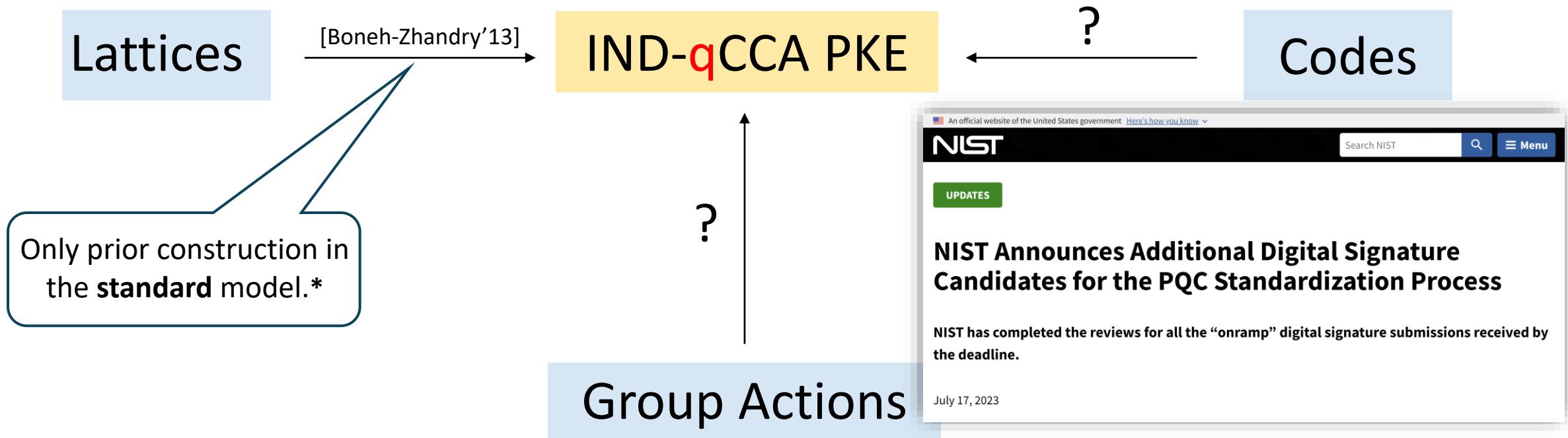


# Motivation

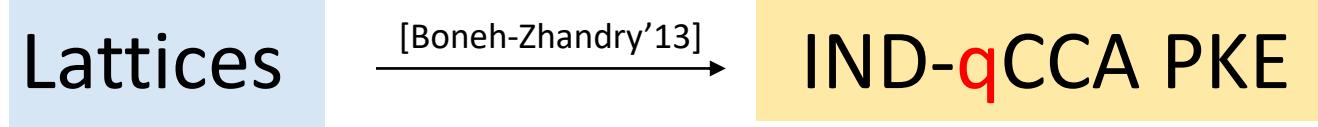
Quantum Algorithms for Lattice Problems

Yilei Chen\*

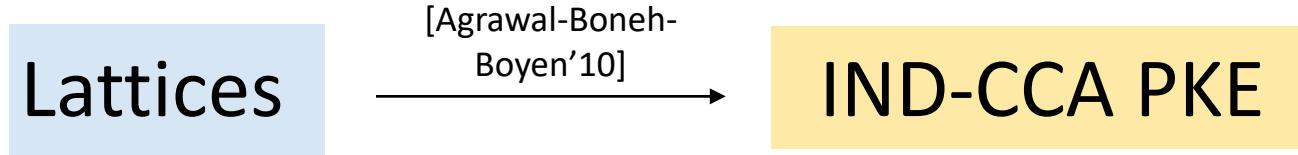
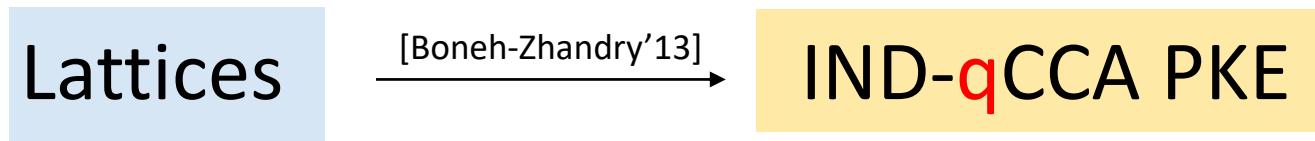
April 10, 2024



# Motivation



# Motivation



# Motivation

Lattices

[Boneh-Zhandry'13]

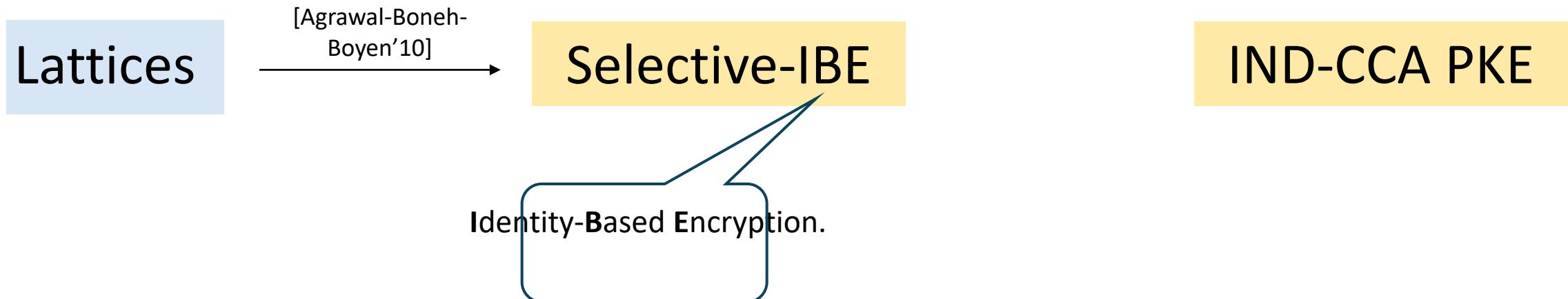
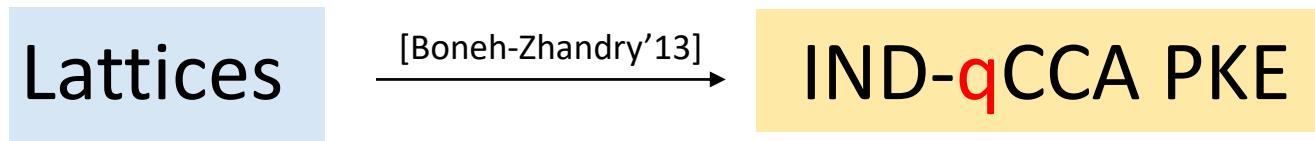
IND-**q**CCA PKE

Lattices

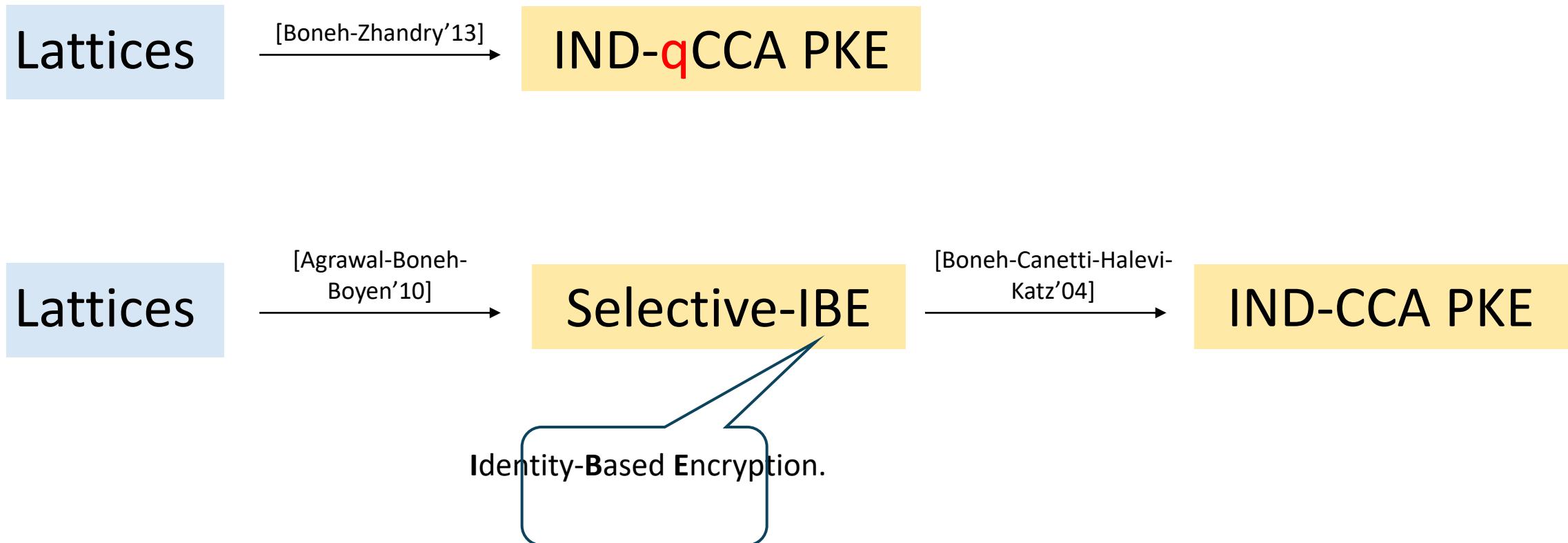
[Agrawal-Boneh-  
Boyen'10]

IND-CCA PKE

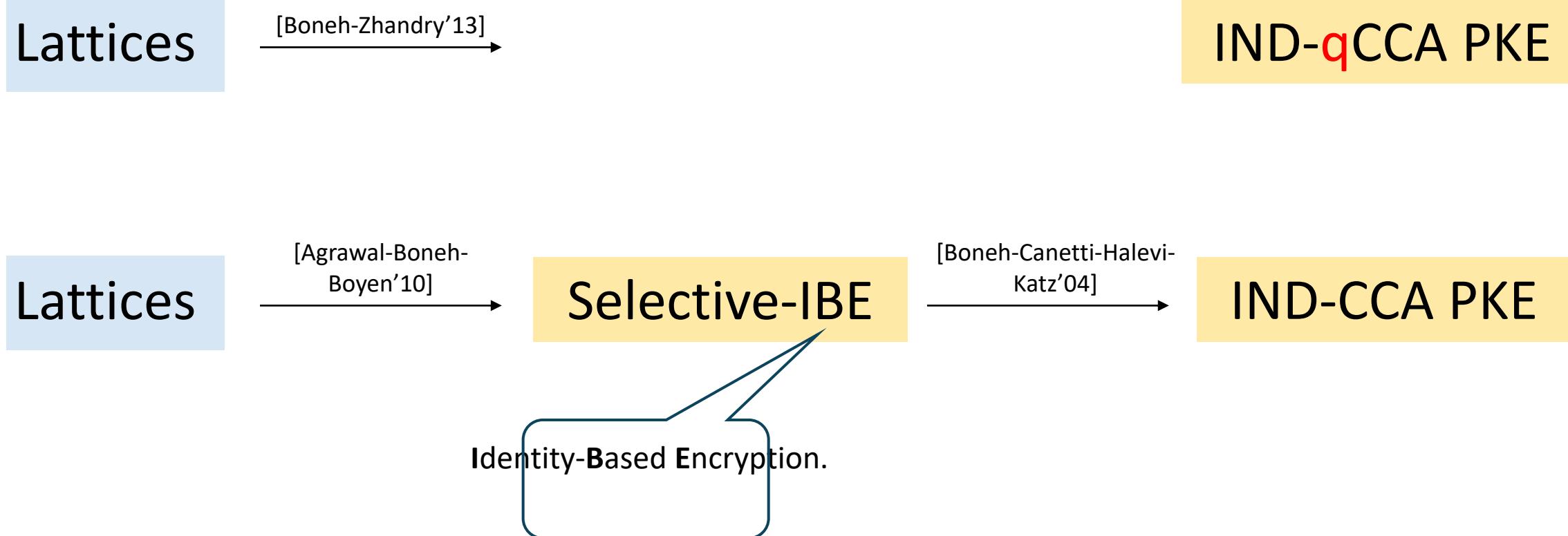
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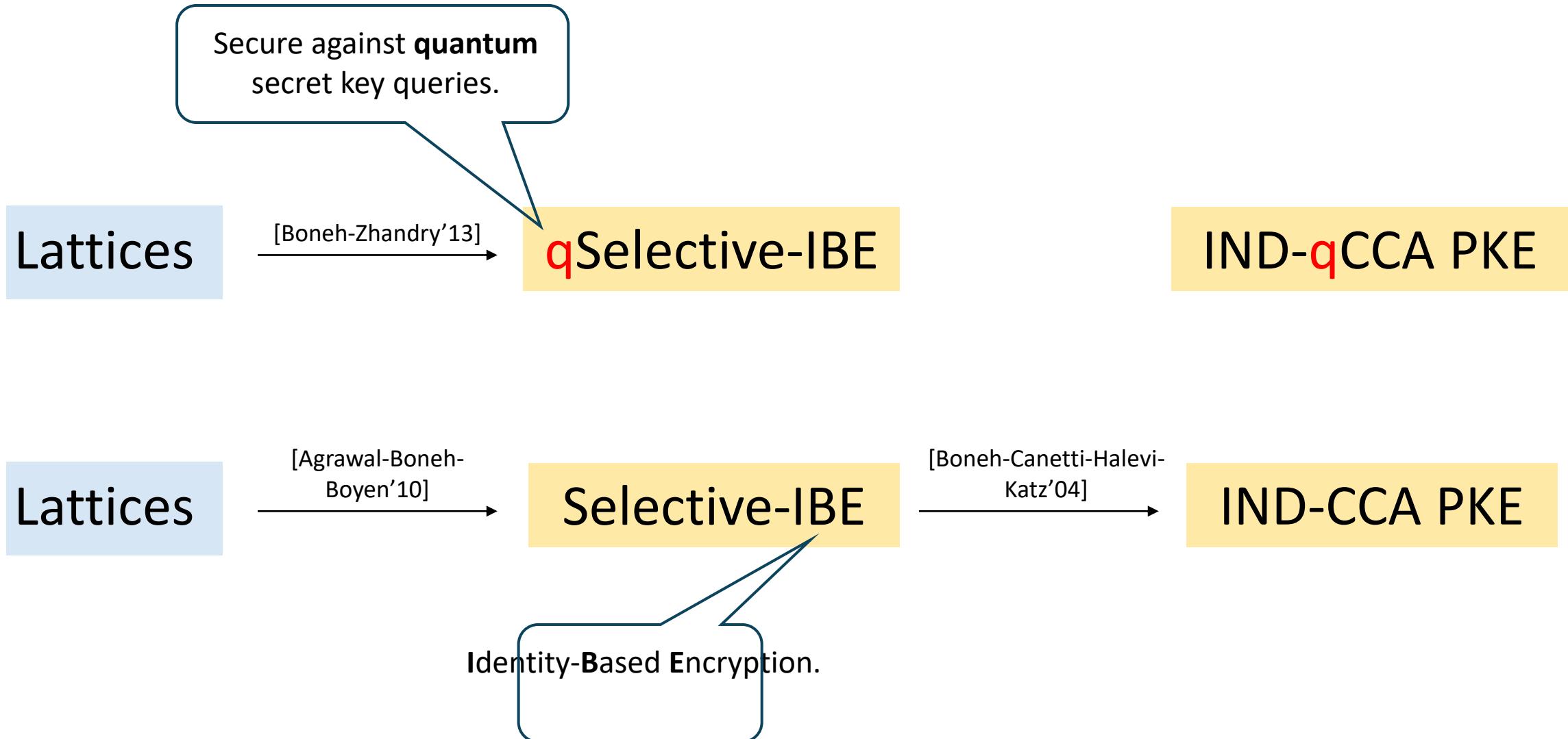
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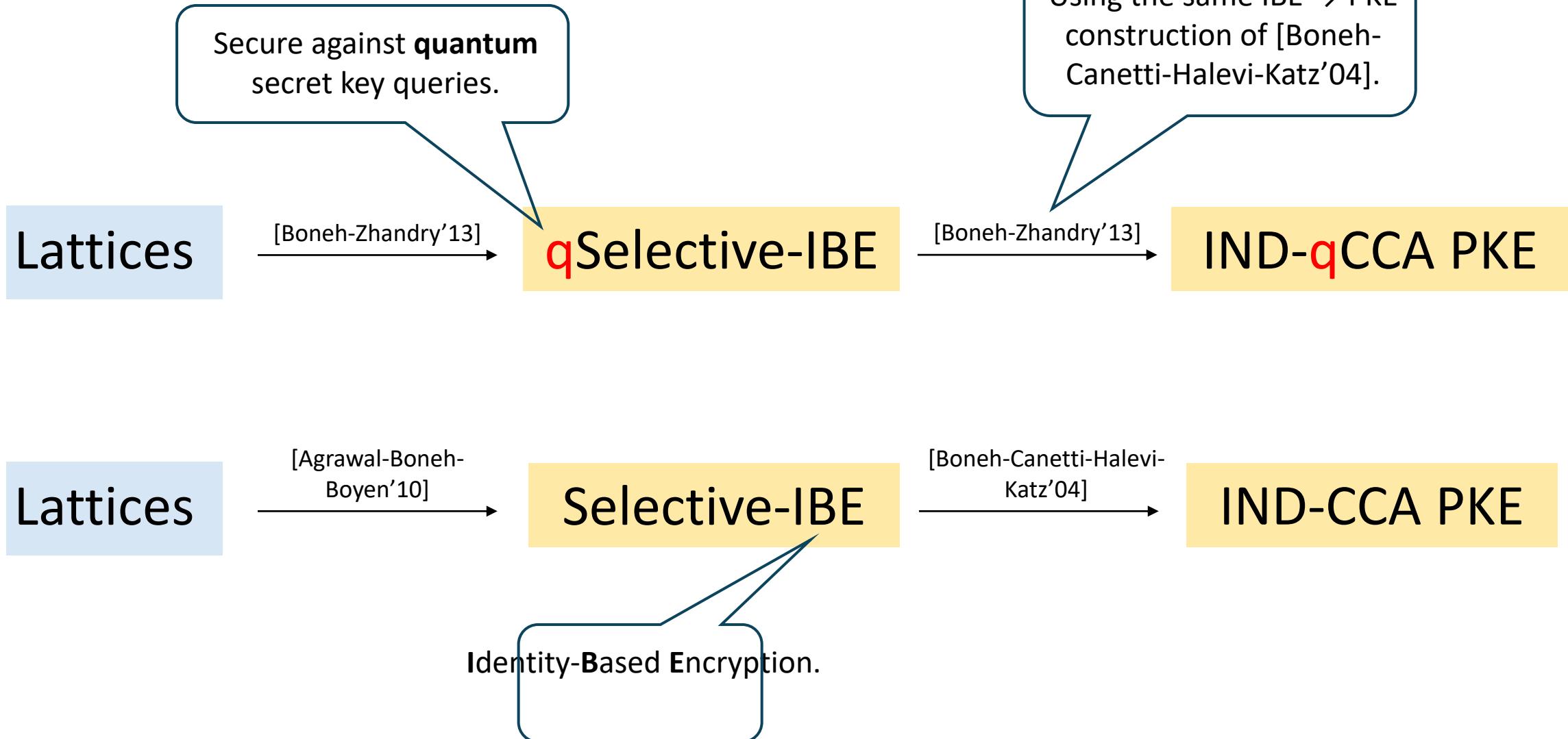
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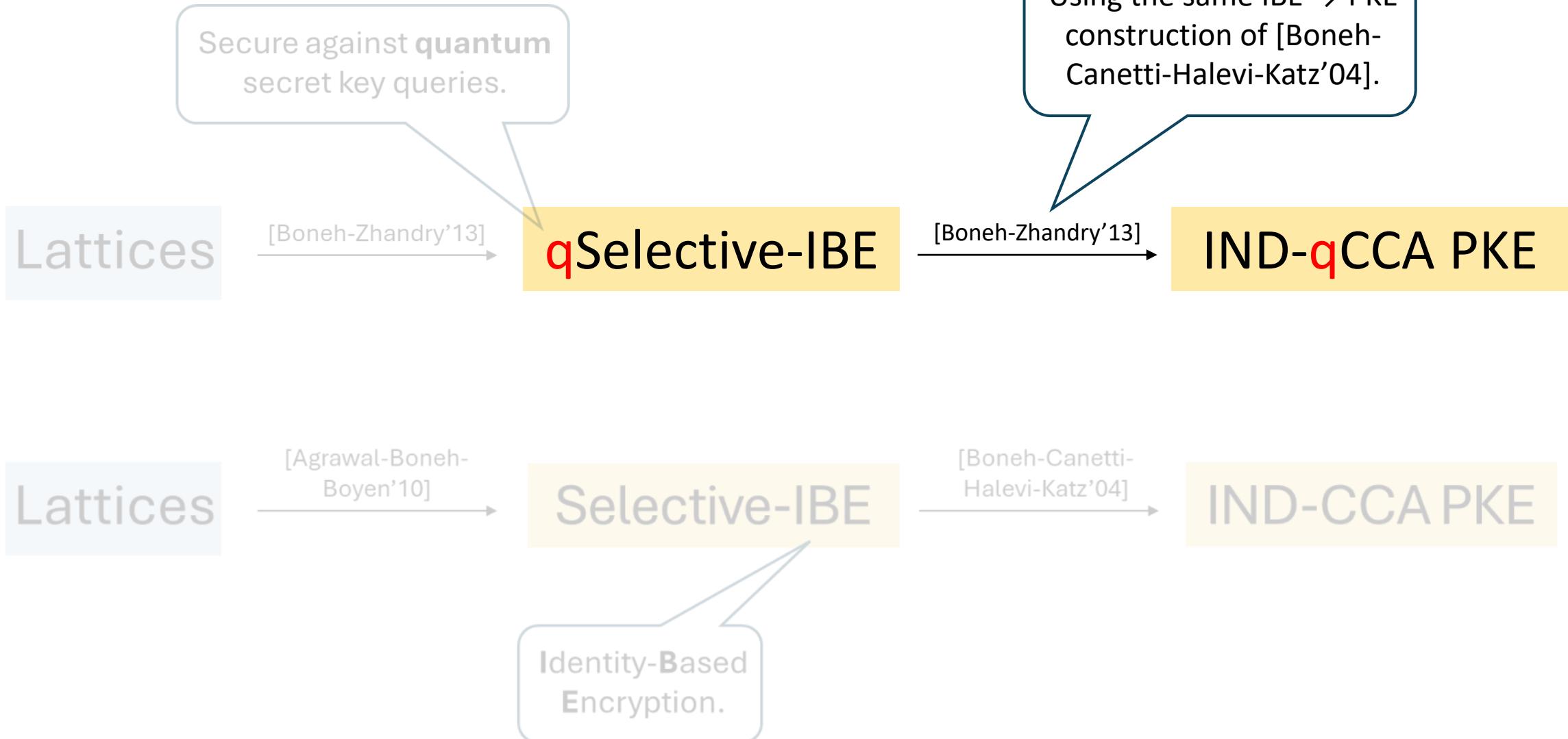
# Motivation



# Motivation



# Motivation



# Motivation

Selective-IBE

[Boneh-Canetti-Halevi-Katz'04]

IND-CCA PKE

# Motivation

Key-Dependent Message.

Selective-IBE

[Boneh-Canetti-Halevi-Katz'04]

KDM-secure PKE

[Kitagawa-Matsuda-Tanaka'19]

IND-CCA PKE

[Kiltz-Mohassel-O'Neill'10]

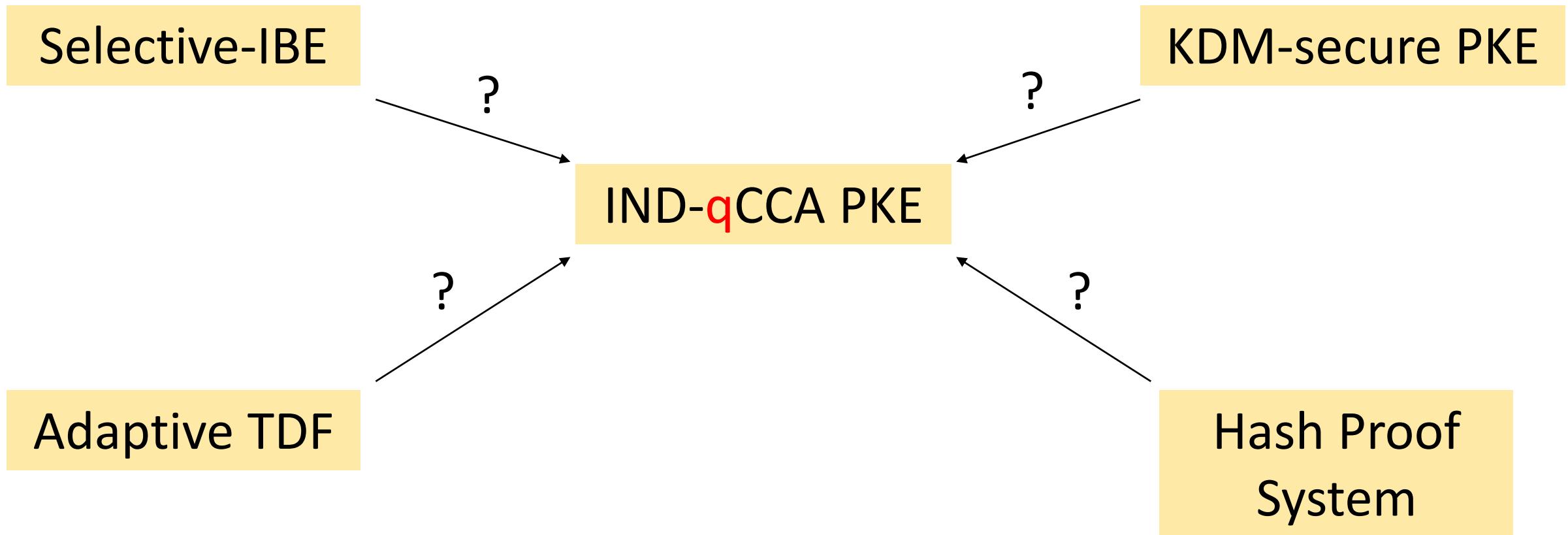
Adaptive TDF

[Cramer-Shoup'02]

Hash Proof System



# Motivation



# Motivation

Secure against post-quantum  
adversaries with quantum  
access to secret oracles.

**qSelective-IBE**

**KDM-secure PKE**

**IND-qCCA PKE**

**Adaptive TDF**

**Hash Proof  
System**

[Boneh-Zhandry'13]

?

?

?

Secure against post-quantum  
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# Overview: Results

**qSelective-IBE**

**KDM-secure PKE**

**Adaptive TDF**

**IND-qCCA PKE**

?

[Boneh-Zhandry'13]

[Our Work]

[Our Work]

**Hash Proof  
System**

Secure against **post-quantum** adversaries with **quantum** access to secret oracles.

# Overview: Results

**qSelective-IBE**

**KDM-secure PKE**

**Adaptive TDF**

Secure against **post-quantum** adversaries with no special quantum access!

**Hash Proof System**

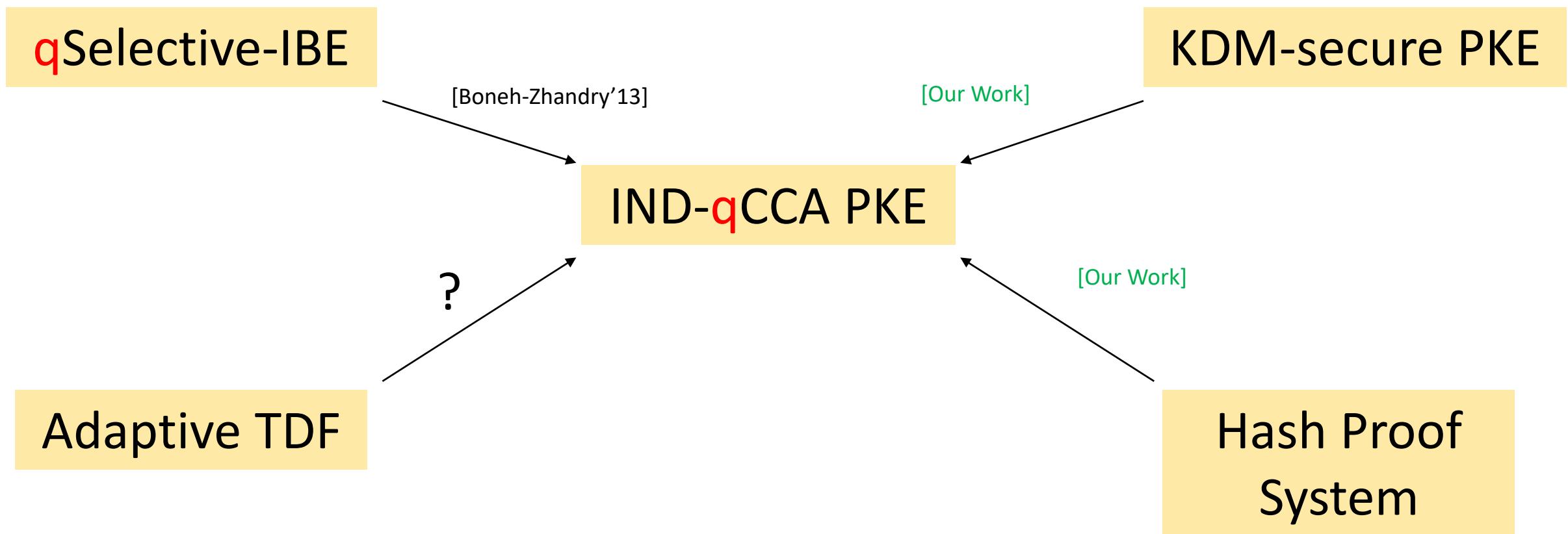
[Boneh-Zhandry'13]

[Our Work]

[Our Work]

?

# Overview: Results



Lattices

# Overview: Results

[Boneh-Zhandry'13]

qSelective-IBE

[Boneh-Zhandry'13]

KDM-secure PKE

[Our Work]

IND-qCCA PKE

Adaptive TDF

?

[Our Work]

Hash Proof  
System

Lattices

# Overview: Results

Codes

qSelective-IBE

[Boneh-Zhandry'13]

KDM-secure PKE

[Applebaum-Cash-Peikert-Sahai'09]

Adaptive TDF

[Boneh-Zhandry'13]

IND-qCCA PKE

[Our Work]

Group Actions

[Alamati-De Feo-Montgomery-Patranabis'20]

Hash Proof System

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[Our Work]

Lattices

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qSelective-IBE

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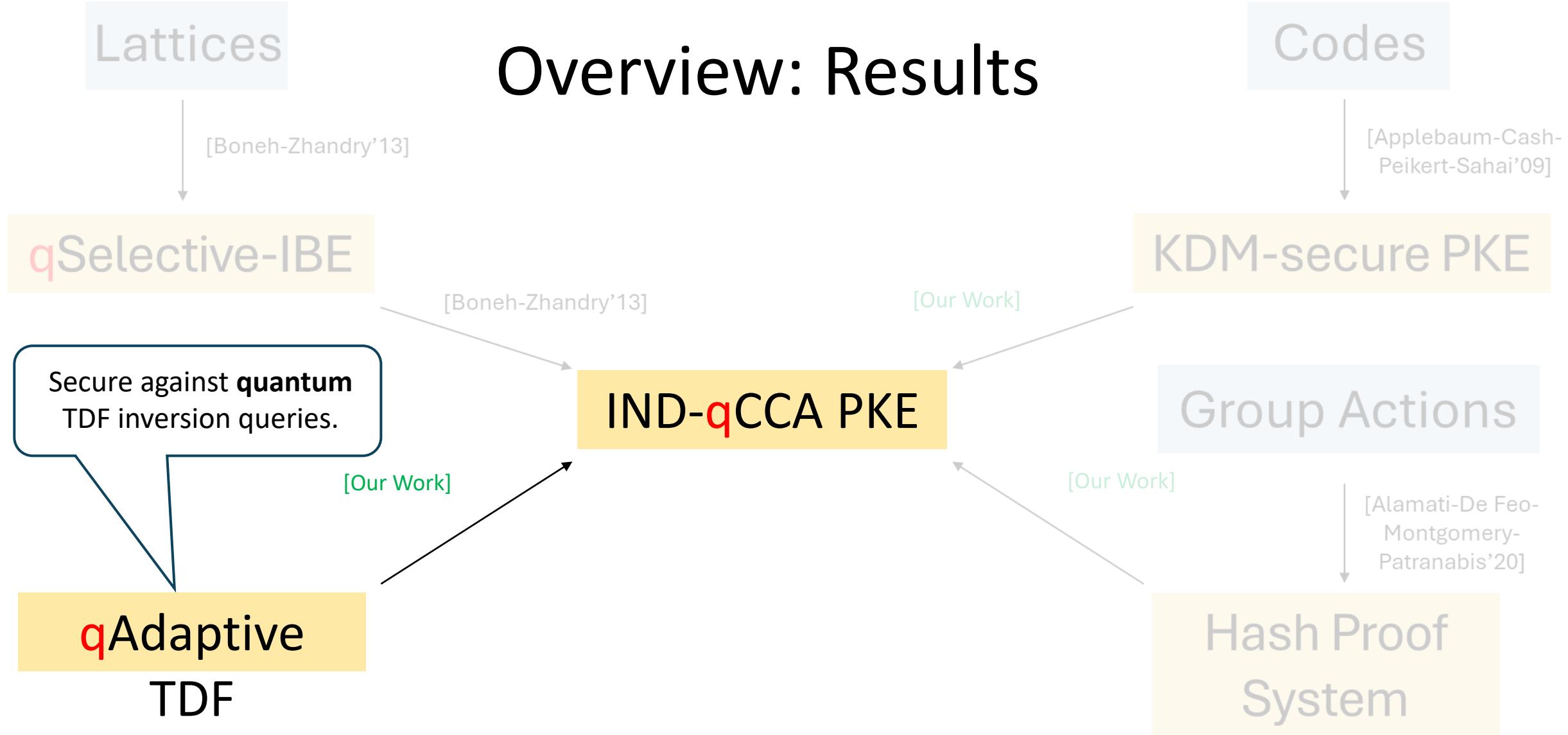
[Boneh-Zhandry'13]

[Our Work]

[Our Work]

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# Overview: Results



Lattices

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Codes

qSelective-IBE

[Boneh-Zhandry'13]

KDM-secure PKE

[Applebaum-Cash-Peikert-Sahai'09]

Secure against **quantum** TDF inversion queries.

[Boneh-Zhandry'13]

Group Actions

[Alamati-De Feo-Montgomery-Patranabis'20]

qAdaptive TDF

[Our Work]

IND-qCCA PKE

[Our Work]

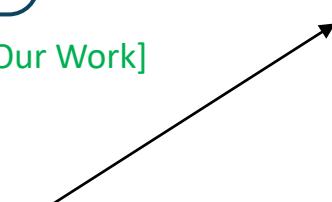
Only need **post-quantum** security.

[Our Work]

Hash Proof System

[Our Work]

Correlated-product TDF



Lattices

# Overview: Results

Codes

qSelective-IBE

Secure against **quantum**  
TDF inversion queries.

qAdaptive  
TDF

Lattices

[Boneh-Zhandry'13]

IND-qCCA PKE

[Our Work]

KDM-secure PKE

Group Actions

[Alamati-De Feo-  
Montgomery-  
Patranabis'20]

Hash Proof  
System

Only need **post-quantum**  
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Correlated-  
product TDF

[Our Work]

[Our Work]

[Our Work]

[Micciancio-Peikert'13]

Lattices

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Codes

qSelective-IBE

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Hash Proof System

[Boneh-Zhandry'13]

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[Boneh-Zhandry'13]

[Our Work]

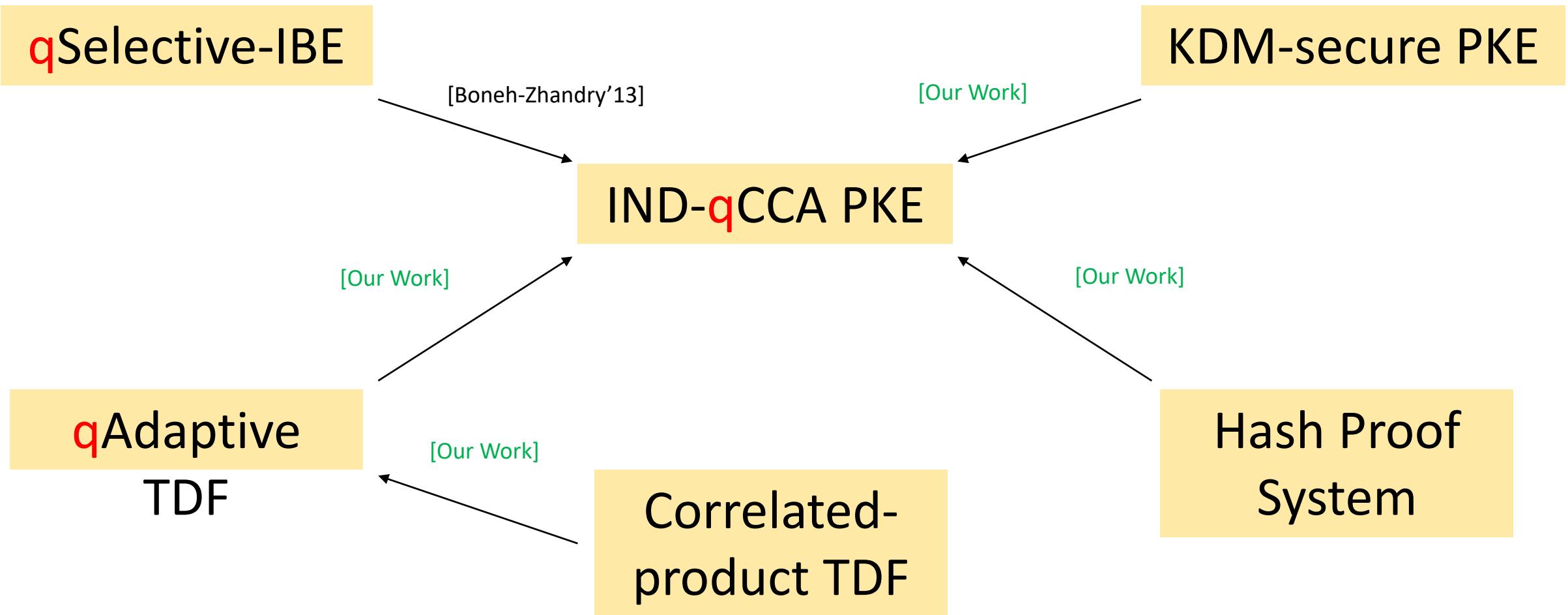
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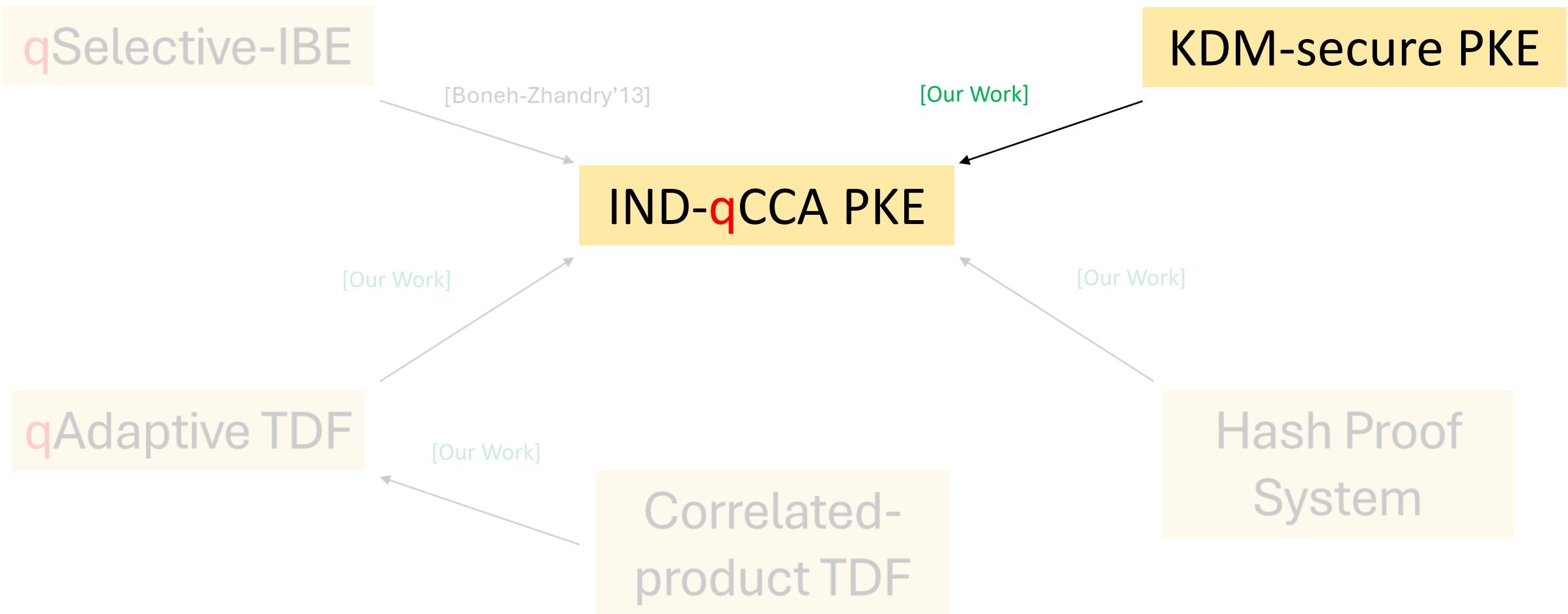
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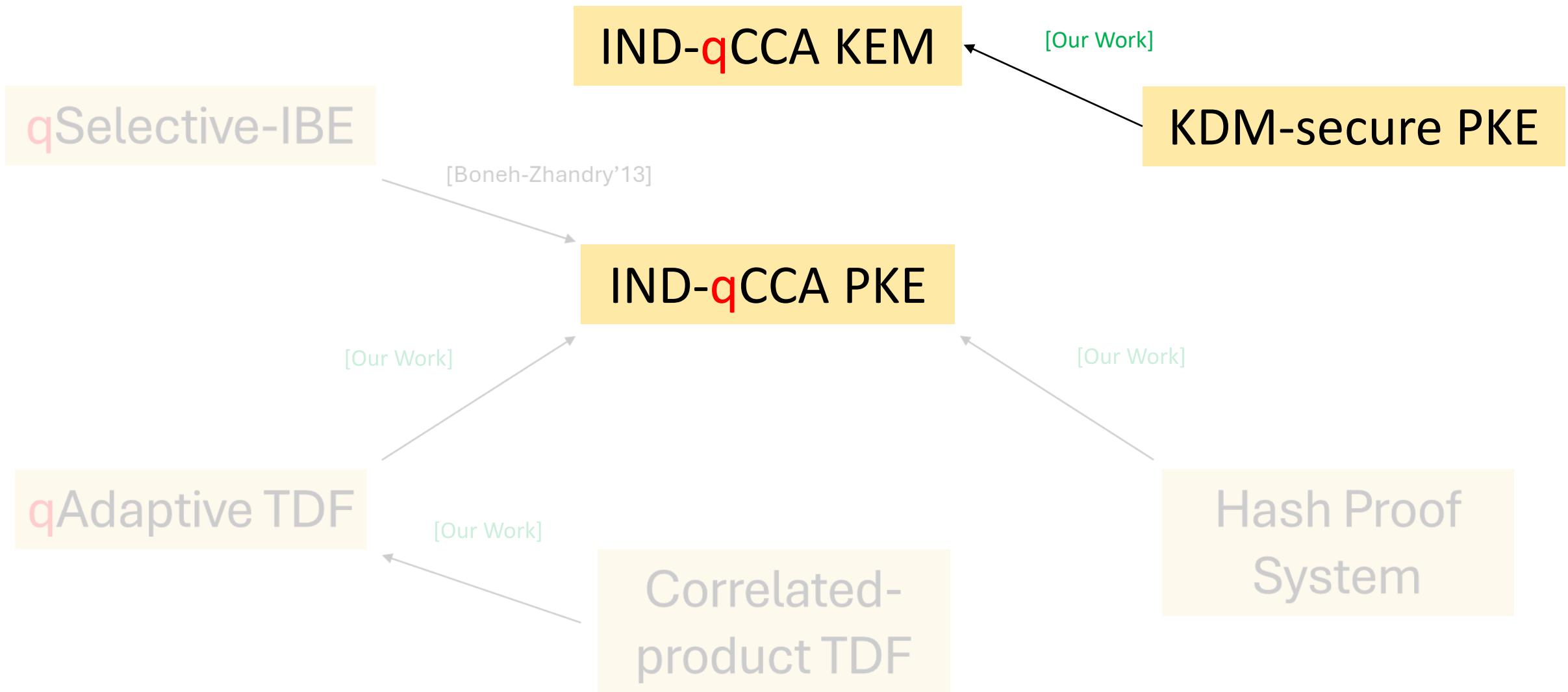
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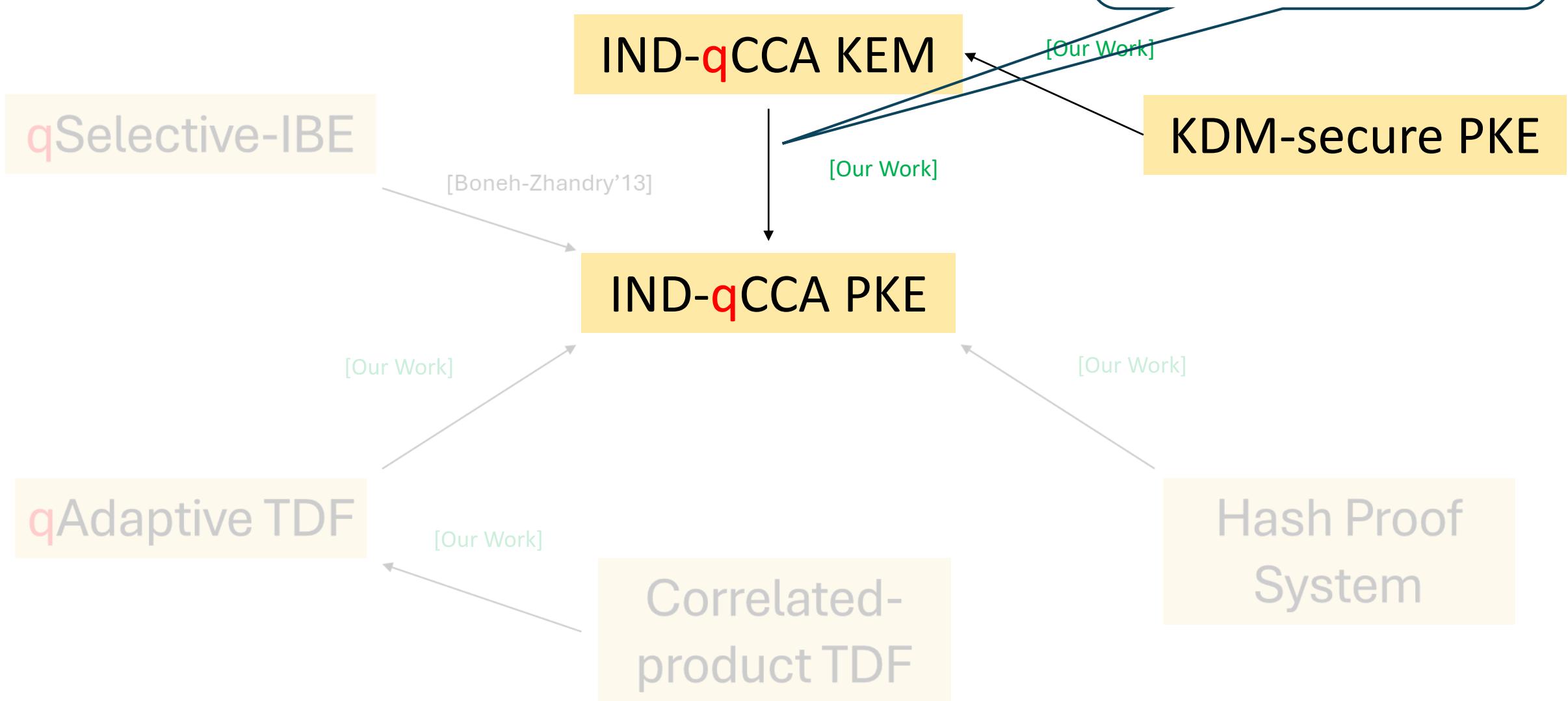


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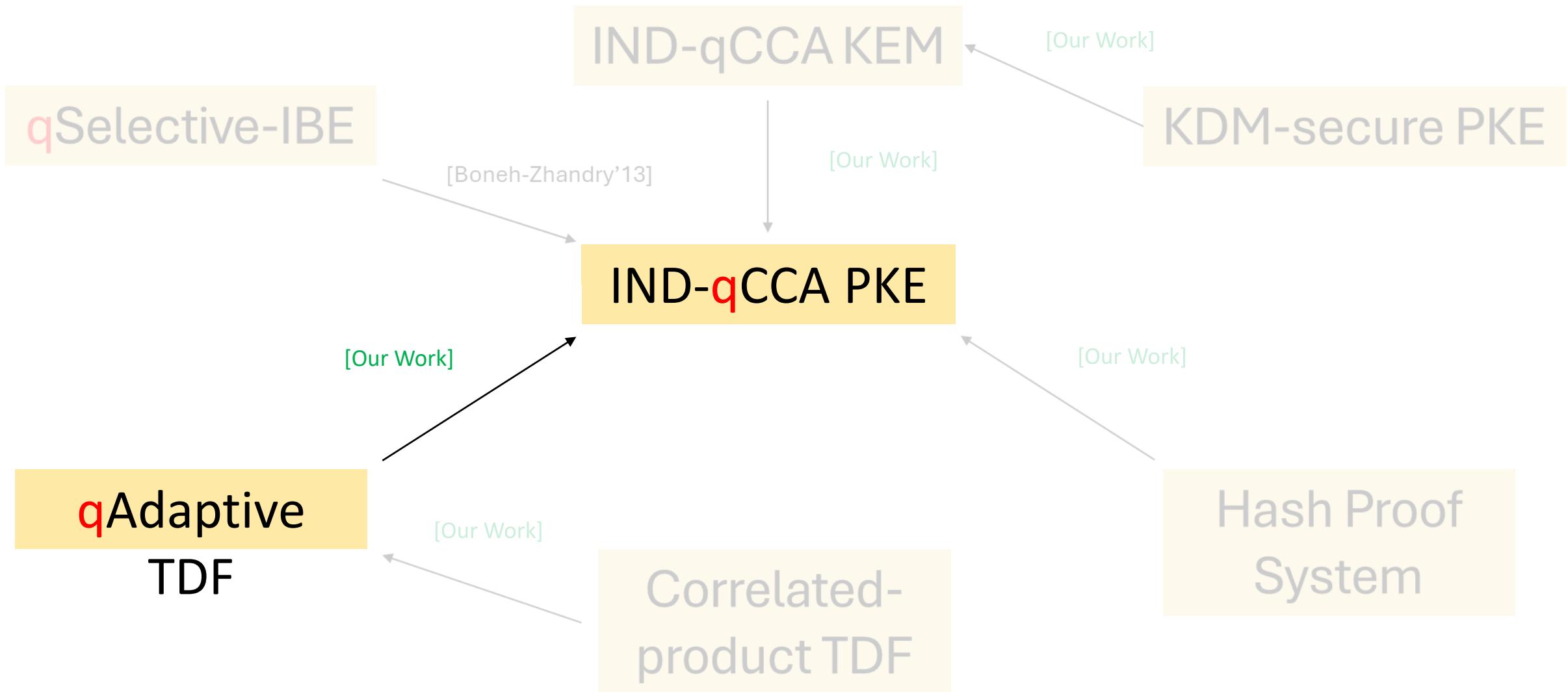


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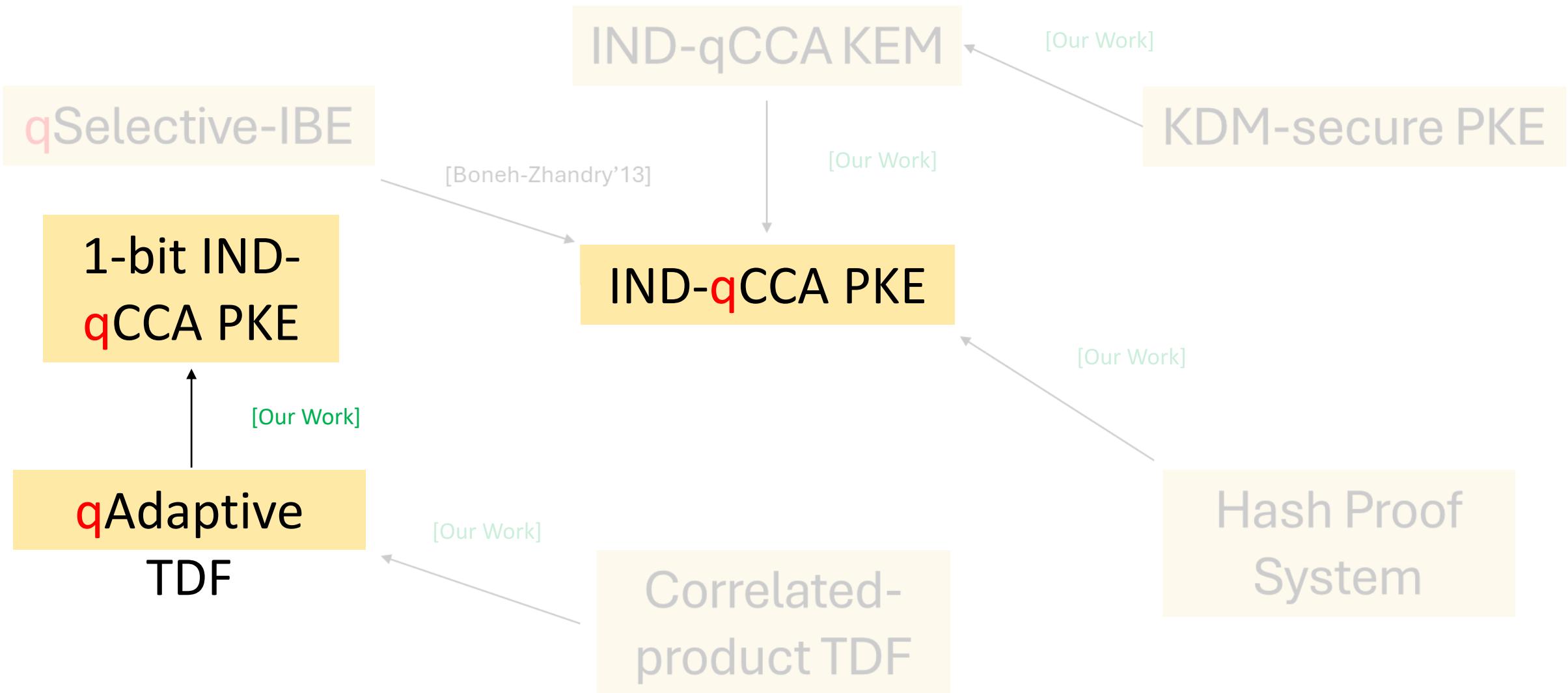
Using the KEM-DEM paradigm of [Cramer-Shoup'03], with only a **post-quantum** secure DEM!



# Overview: Results

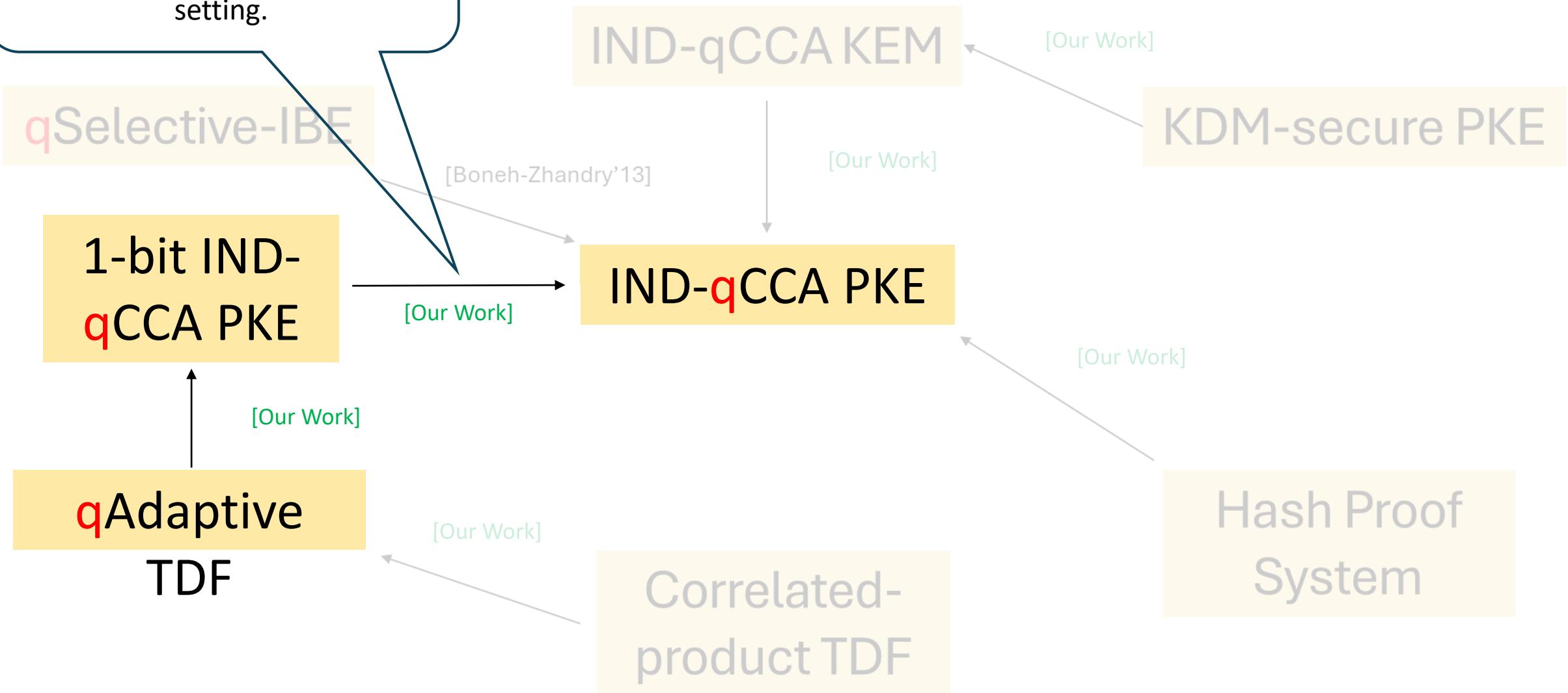


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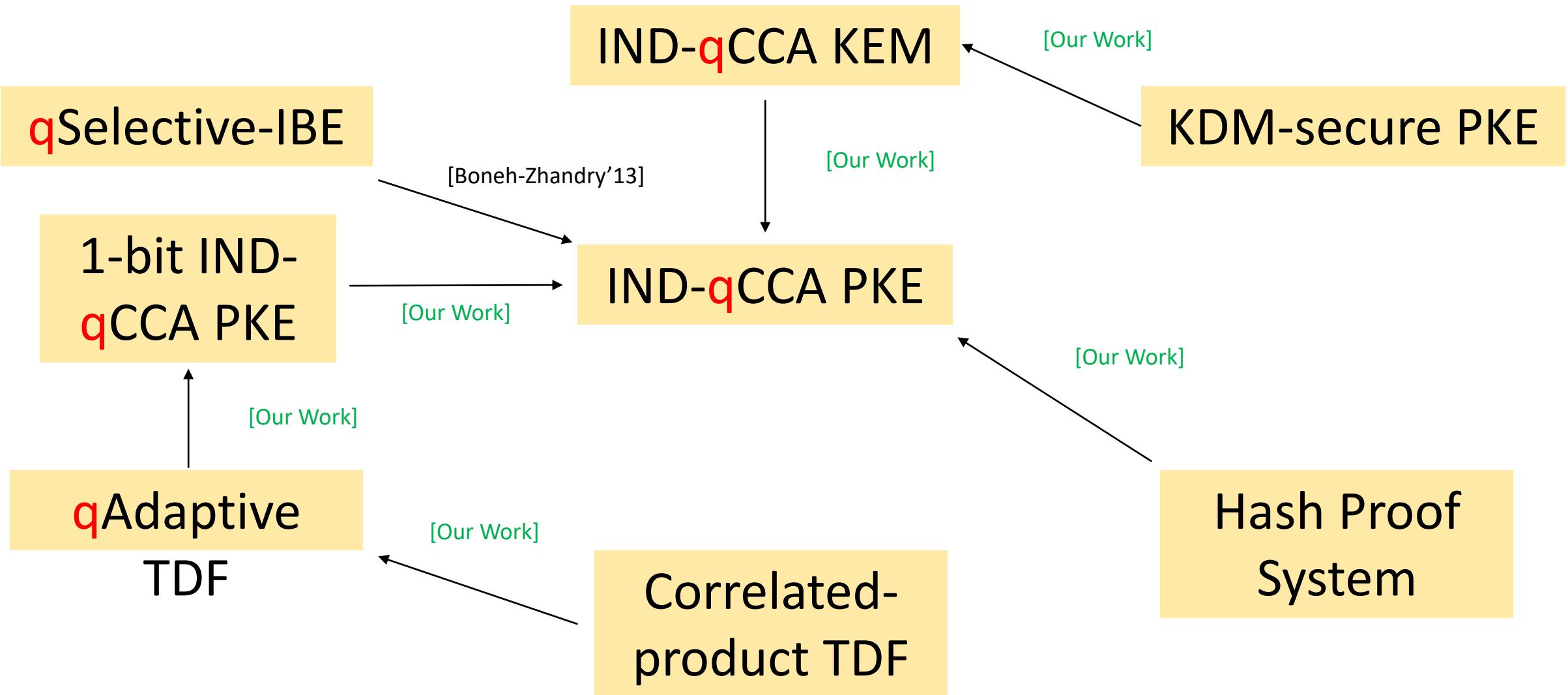


Extending **bit completeness** of CCA-secure PKE by [Hohenberger-Lewko-Waters'12] to the quantum setting.

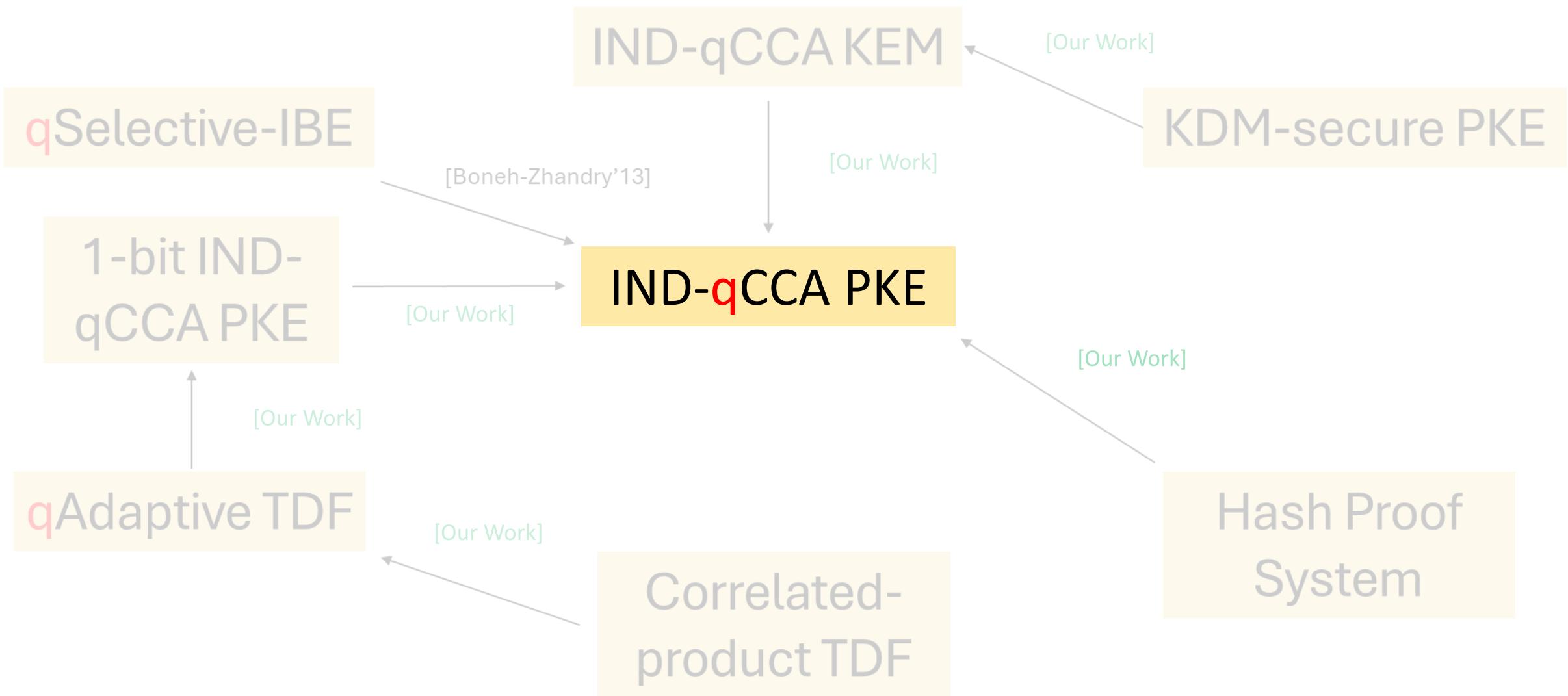
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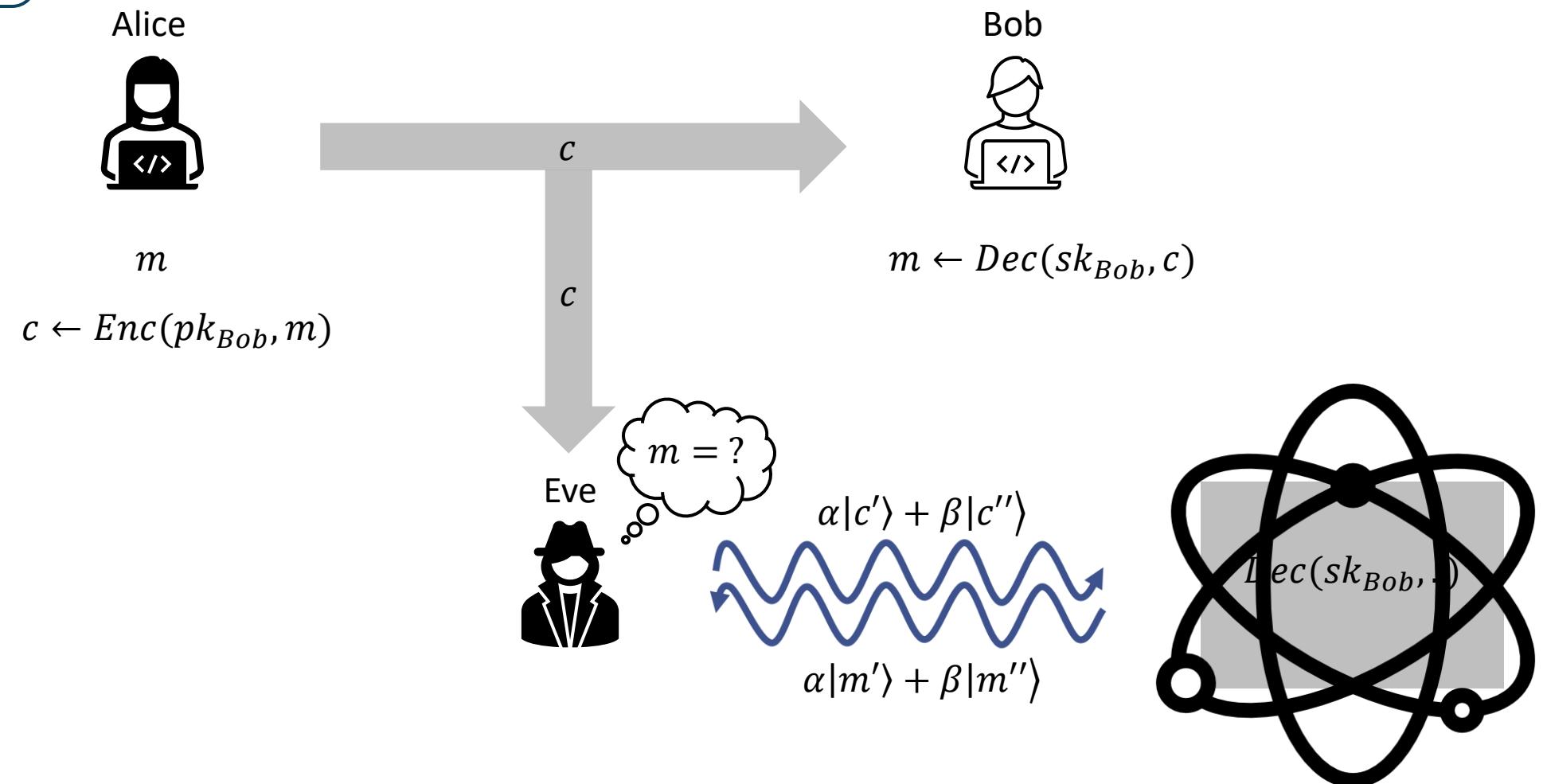
# Overview: Results



# IND-qCCA Security

Introduced by [Boneh-Zhandry'13].

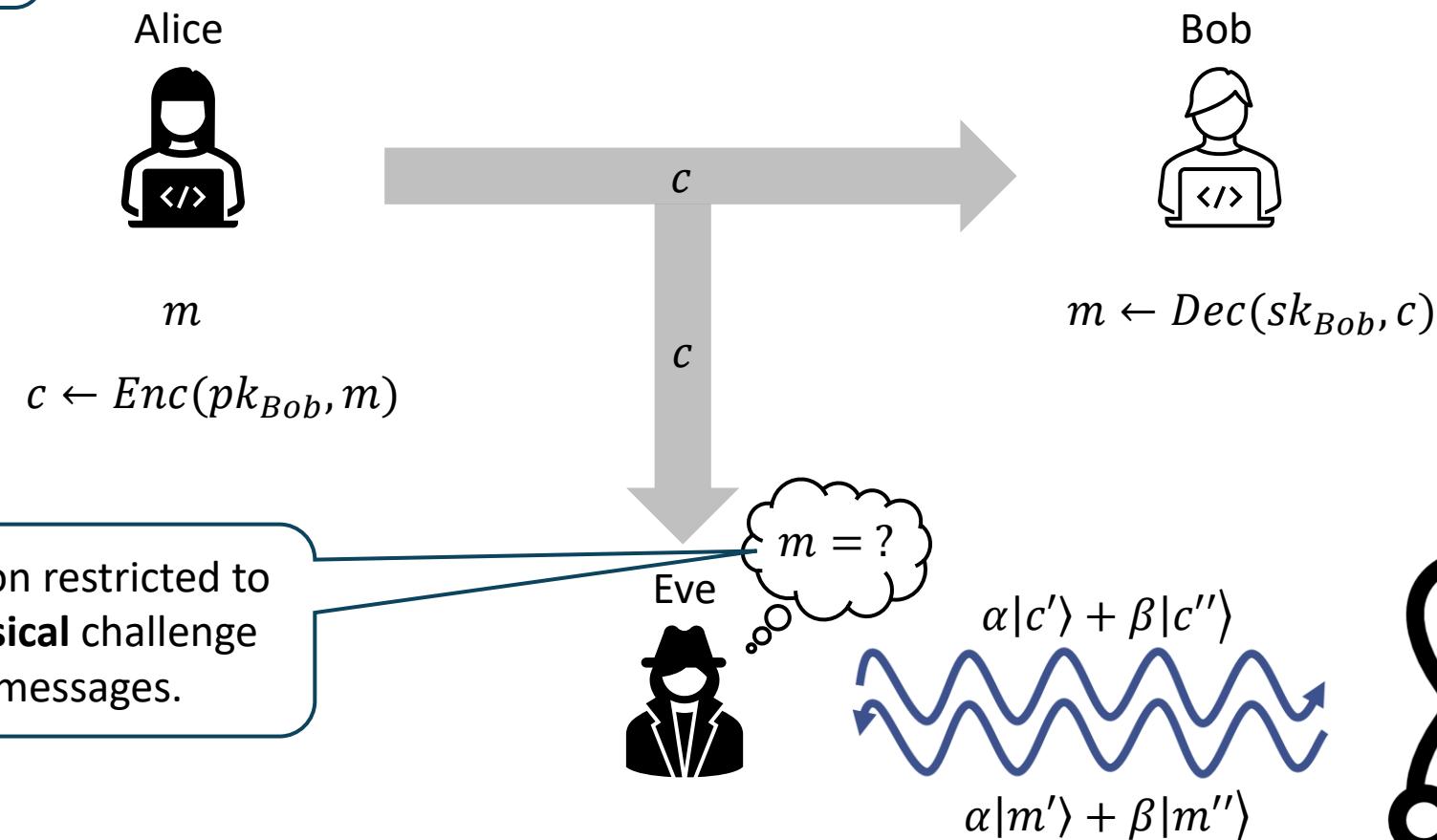
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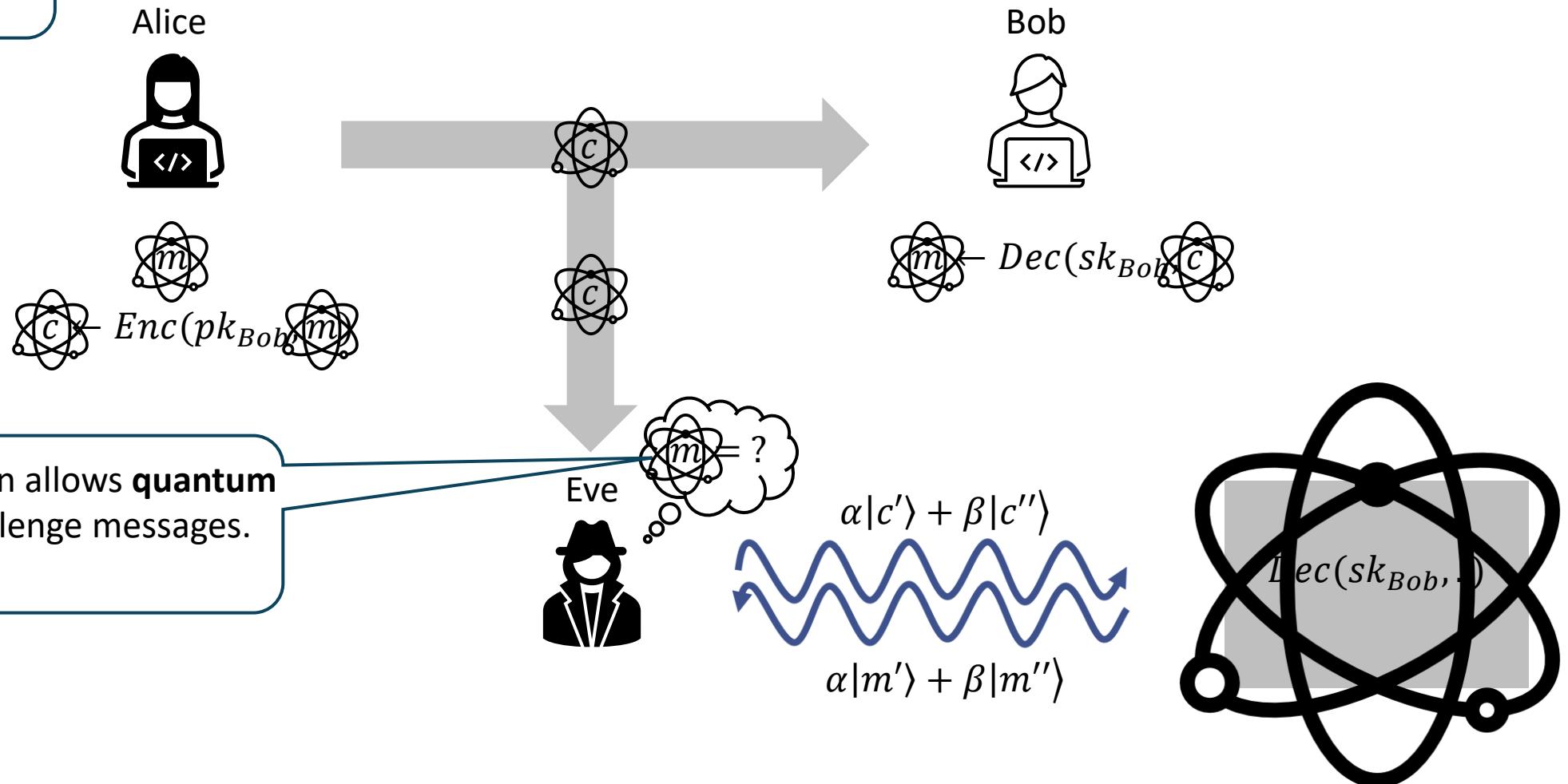
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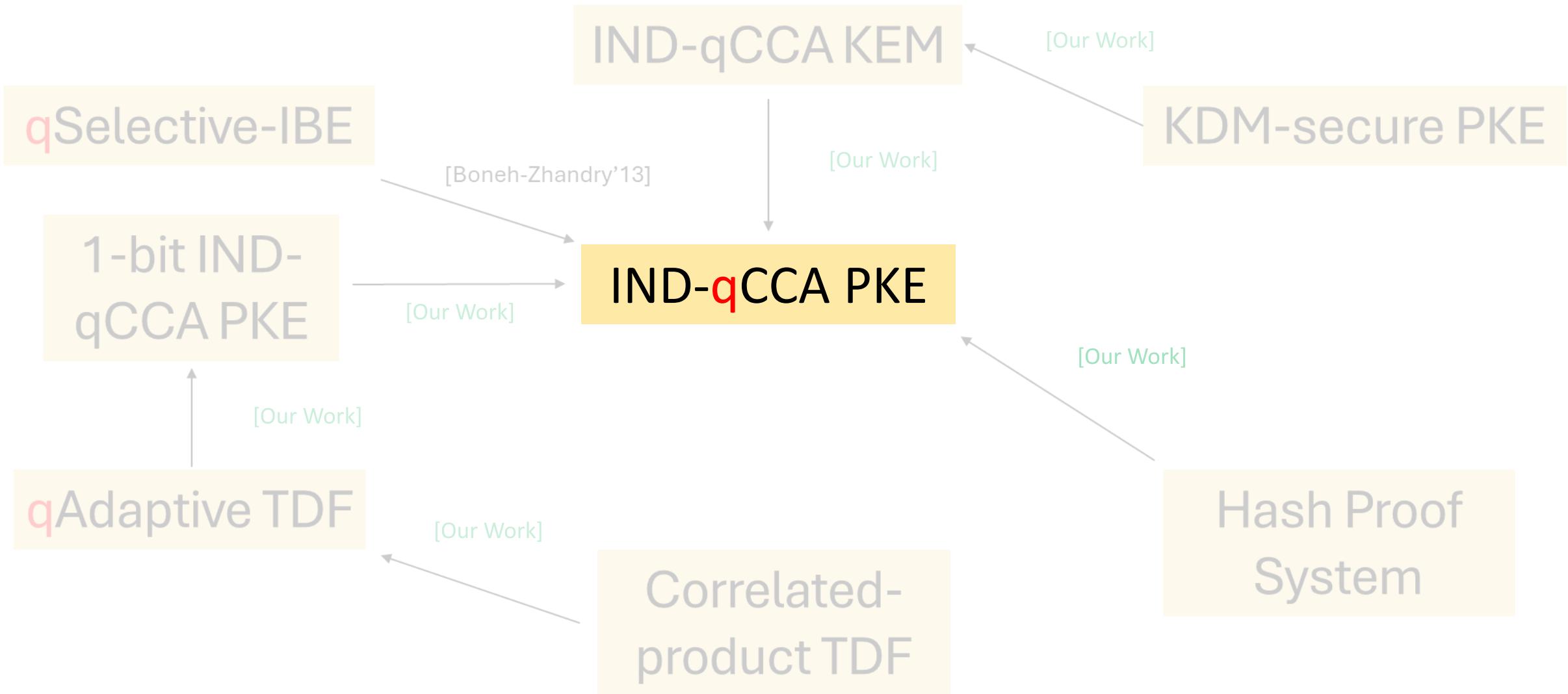
# $\mathbf{qIND}\text{-}\mathbf{qCCA}$ Security

Introduced by  
[Chevalier-Ebrahimi-  
Vu'22].

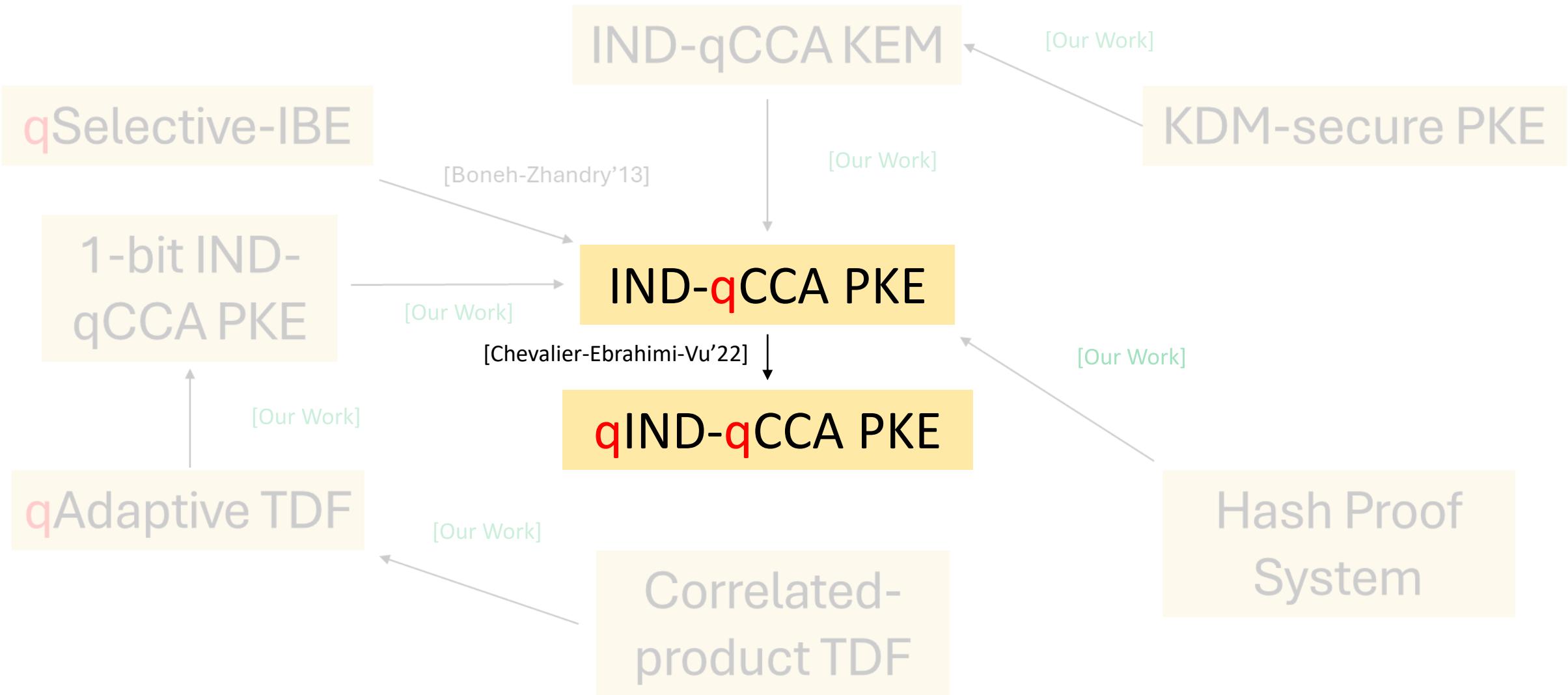
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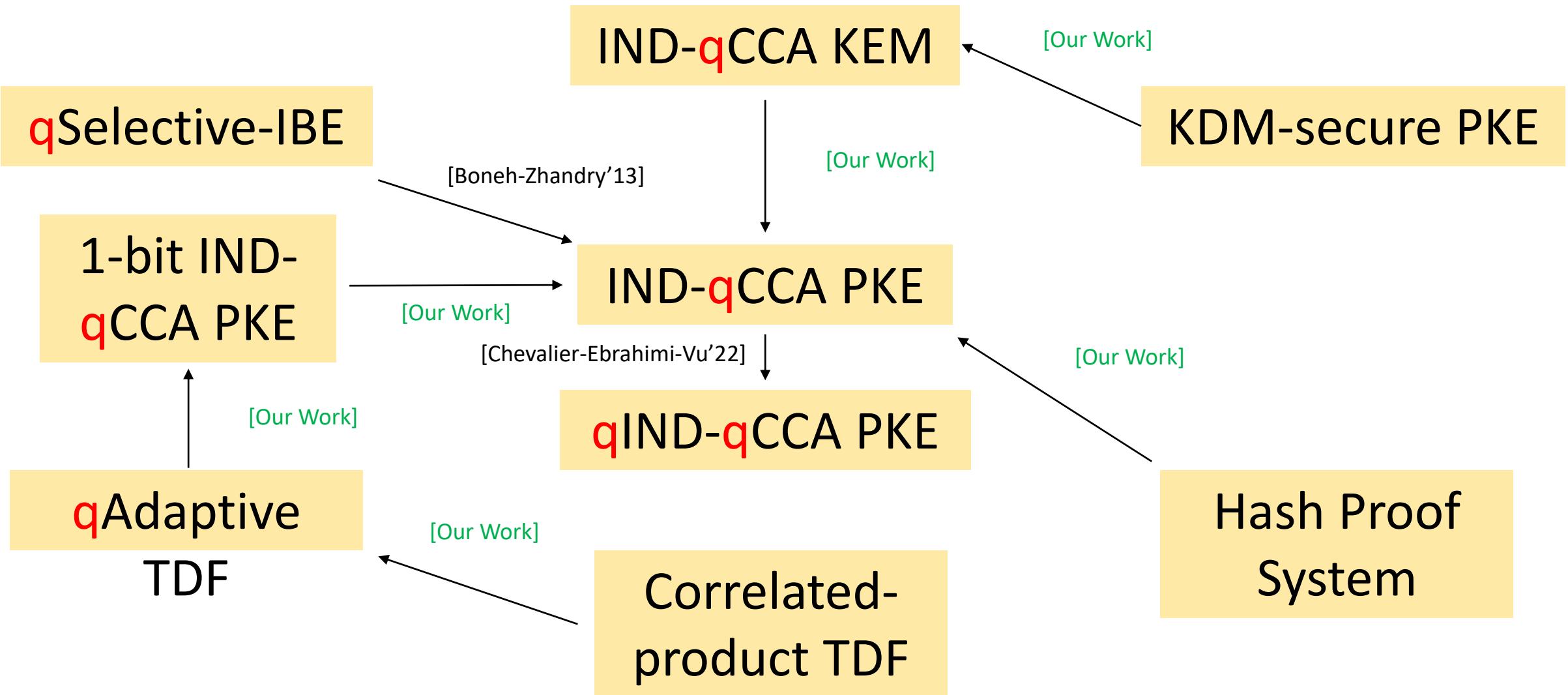
# Overview: Results



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# Overview: Results



Lattices

# Overview: Results

Codes

qSelective-IBE

1-bit IND-qCCA PKE

qAdaptive TDF

Lattices

IND-qCCA KEM

KDM-secure PKE

Group Actions

Hash Proof System

IND-qCCA PKE

qIND-qCCA PKE

Correlated-product TDF

[Boneh-Zhandry'13]

[Our Work]

[Applebaum-Cash-Peikert-Sahai'09]

[Boneh-Zhandry'13]

[Our Work]

[Our Work]

[Our Work]

[Alamati-De Feo-Montgomery-Patranabis'20]

[Our Work]

TDF

Lattices

[Micciancio-Peikert'13]

# Overview: Results

All our analyzed PKE constructions are **classical**.

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- They can be implemented on **classical computers**.

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All our analyzed PKE constructions are **classical**.

- They can be implemented on **classical computers**.
- As opposed to **quantum PKE schemes** (e.g., in [Barouti-Grilo-Huguenin(-)Dumittan-Malavolta-Sattath-Vu-Walter'23]) which need inherent quantum components, such as **quantum public keys**.

Lattices

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[Our Work]

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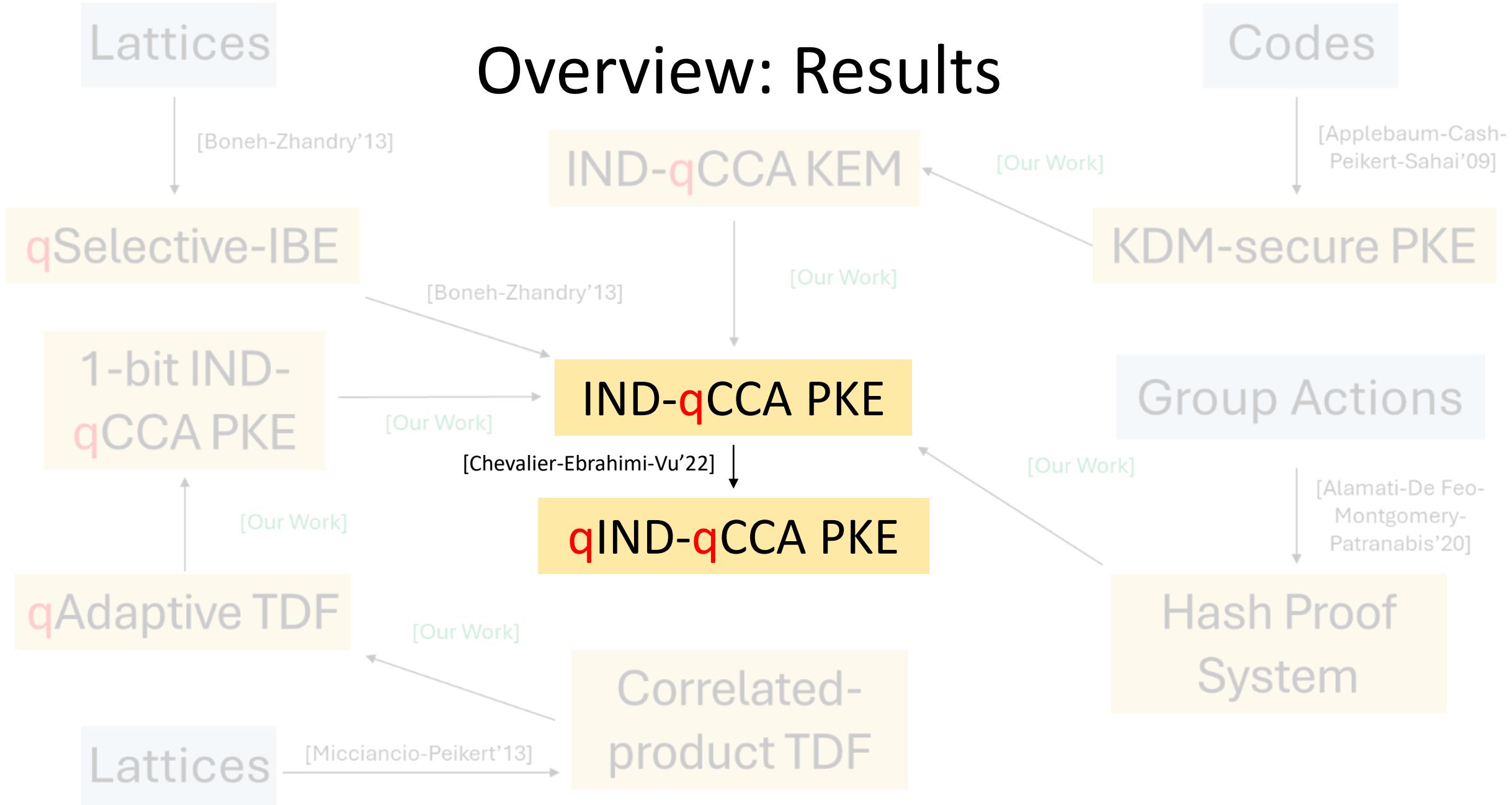
[Our Work]

TDF

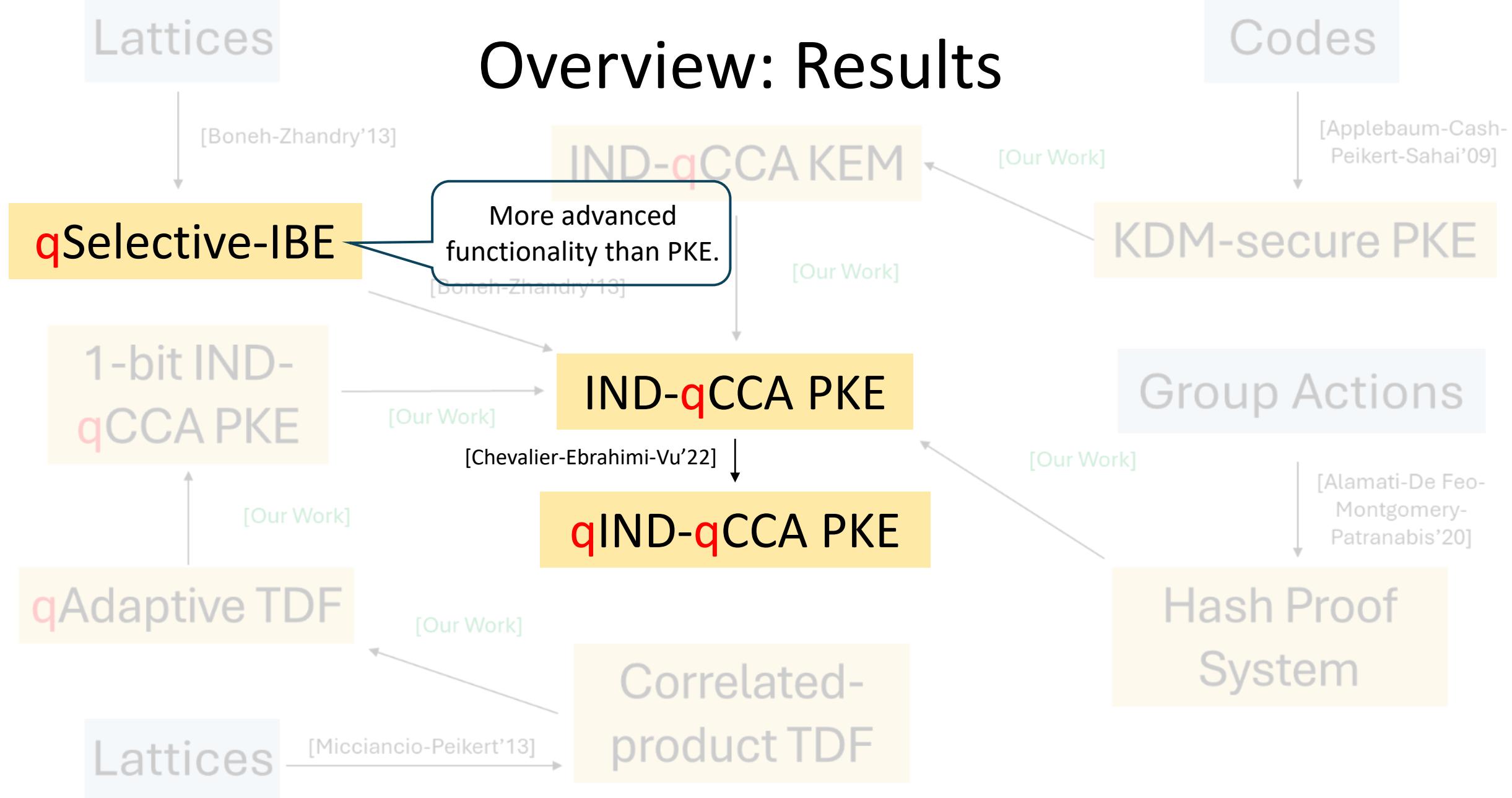
Lattices

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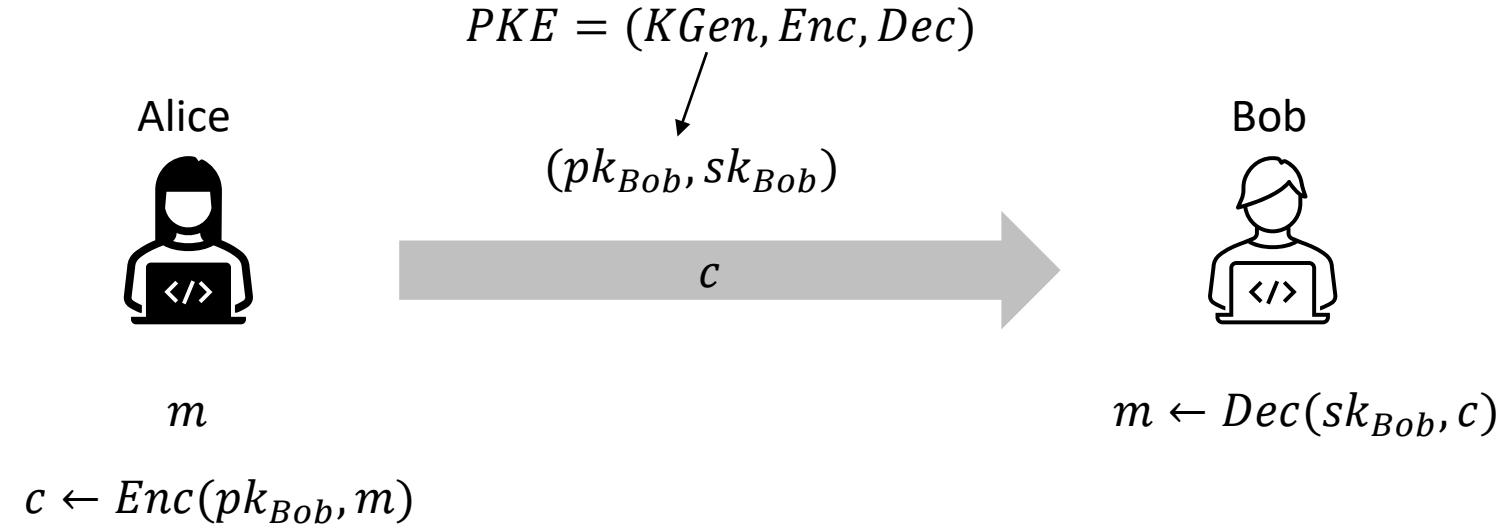
# Overview: Results



# Overview: Results



# PKE

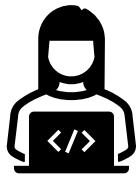


# ABE

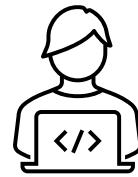
Attribute-Based  
Encryption.

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice



Bob



$$(\textcolor{red}{mpk}, \textcolor{red}{msk})$$

$c$

$m, \textcolor{red}{attr}$

$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$

# ABE

Attribute-Based  
Encryption.

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice

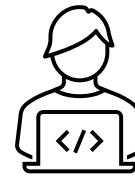


$m, \textcolor{red}{attr}$

$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$



Bob



$$(\textcolor{red}{mpk}, \textcolor{red}{msk})$$

# ABE

Attribute-Based  
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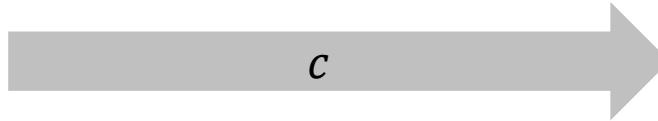
$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice



$m, \textcolor{red}{attr}$

$$c \leftarrow \text{Enc}(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$



( $\textcolor{red}{mpk}, \textcolor{red}{msk}$ )

Bob



$$\textcolor{red}{msk} \quad sk \leftarrow \text{SKGen}(\textcolor{red}{msk}, \textcolor{red}{pred})$$

“predicate”

# ABE

Attribute-Based  
Encryption.

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice



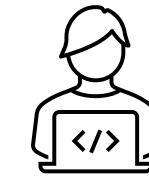
$m, \textcolor{red}{attr}$

$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$

$(\textcolor{red}{mpk}, \textcolor{red}{msk})$

$c$

Bob



$$m \leftarrow Dec(\textcolor{black}{sk}, c) \text{ if } \textcolor{red}{pred}(\textcolor{black}{attr}) = 1$$

$\textcolor{red}{msk}$

$\textcolor{red}{sk} \leftarrow SKGen(\textcolor{red}{msk}, \textcolor{red}{pred})$

“predicate”



# ABE

Attribute-Based  
Encryption.

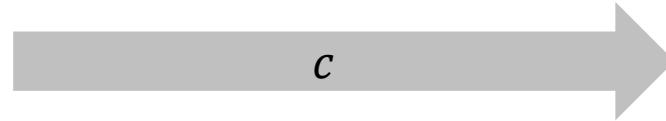
$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice



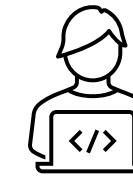
$m, \textcolor{red}{attr}$

$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$



$(\textcolor{red}{mpk}, \textcolor{red}{msk})$

Bob



$$\begin{aligned} m &\leftarrow Dec(\textcolor{black}{sk}, c) \text{ if } \textcolor{red}{pred}(\textcolor{black}{attr}) = 1 \\ \perp &\leftarrow Dec(\textcolor{black}{sk}, c) \text{ if } \textcolor{red}{pred}(\textcolor{black}{attr}) = 0 \end{aligned}$$

$$sk \leftarrow \textcolor{red}{SKGen}(\textcolor{red}{msk}, \textcolor{red}{pred})$$

“predicate”

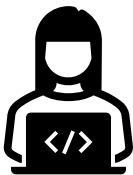


# ABE

Attribute-Based  
Encryption.

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice



$m, attr$

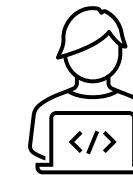
$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$

“Bob”

$(\textcolor{red}{mpk}, msk)$

$c$

Bob



$m \leftarrow Dec(\textcolor{red}{sk}, c) \text{ if } pred(attr) = 1$

$\perp \leftarrow Dec(\textcolor{red}{sk}, c) \text{ if } pred(attr) = 0$

$$sk \leftarrow SKGen(msk, pred)$$



$pred(“Bob”) = 1$

$pred(\cdot) = 0, \text{otherwise}$

# ABE

Attribute-Based  
Encryption.

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

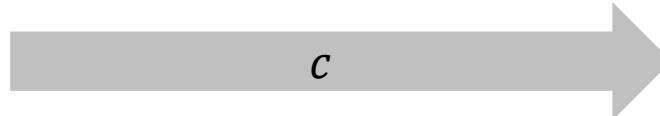
Alice



$m, attr$

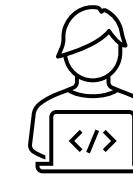
$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$

*“Dave”*



$(\textcolor{red}{mpk}, msk)$

Bob



$$\begin{aligned} m &\leftarrow Dec(\textcolor{red}{sk}, c) \text{ if } pred(attr) = 1 \\ \perp &\leftarrow Dec(\textcolor{red}{sk}, c) \text{ if } pred(attr) = 0 \end{aligned}$$

$$sk \leftarrow SKGen(msk, pred)$$



$$\begin{aligned} pred("Bob") &= 1 \\ pred(\cdot) &= 0, \text{ otherwise} \end{aligned}$$

# ABE

Attribute-Based  
Encryption.

Implies Identity-Based  
Encryption (IBE).

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

Alice



$m, attr$

$$c \leftarrow Enc(\textcolor{red}{mpk}, m, \textcolor{red}{attr})$$

*“Dave”*

$$(\textcolor{red}{mpk}, msk)$$

$c$

Bob



$$\begin{aligned} m &\leftarrow Dec(sk, c) \text{ if } pred(attr) = 1 \\ \perp &\leftarrow Dec(sk, c) \text{ if } pred(attr) = 0 \end{aligned}$$



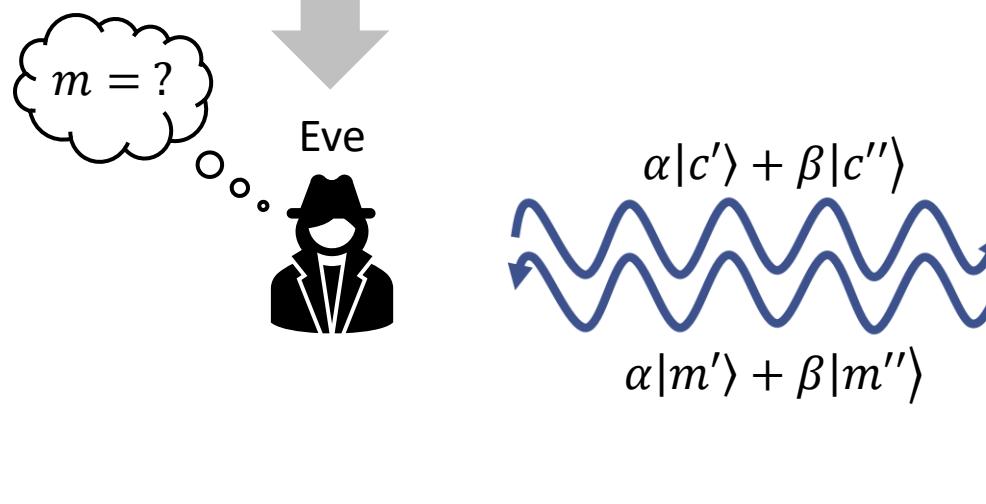
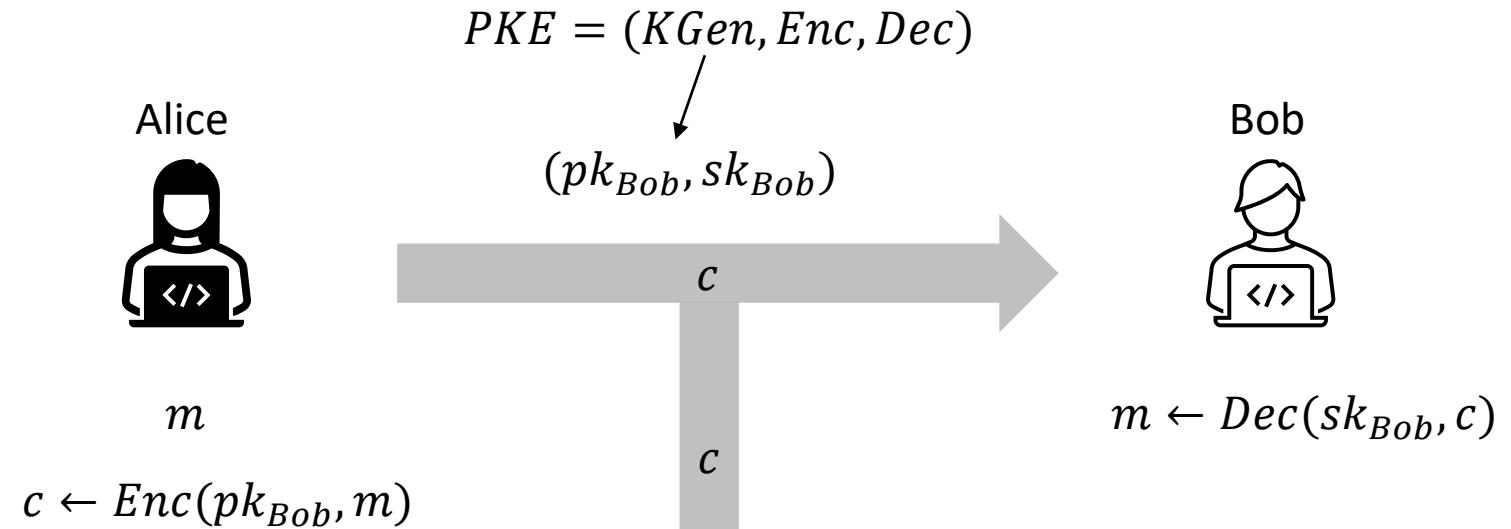
$msk$

$sk \leftarrow SKGen(msk, pred)$

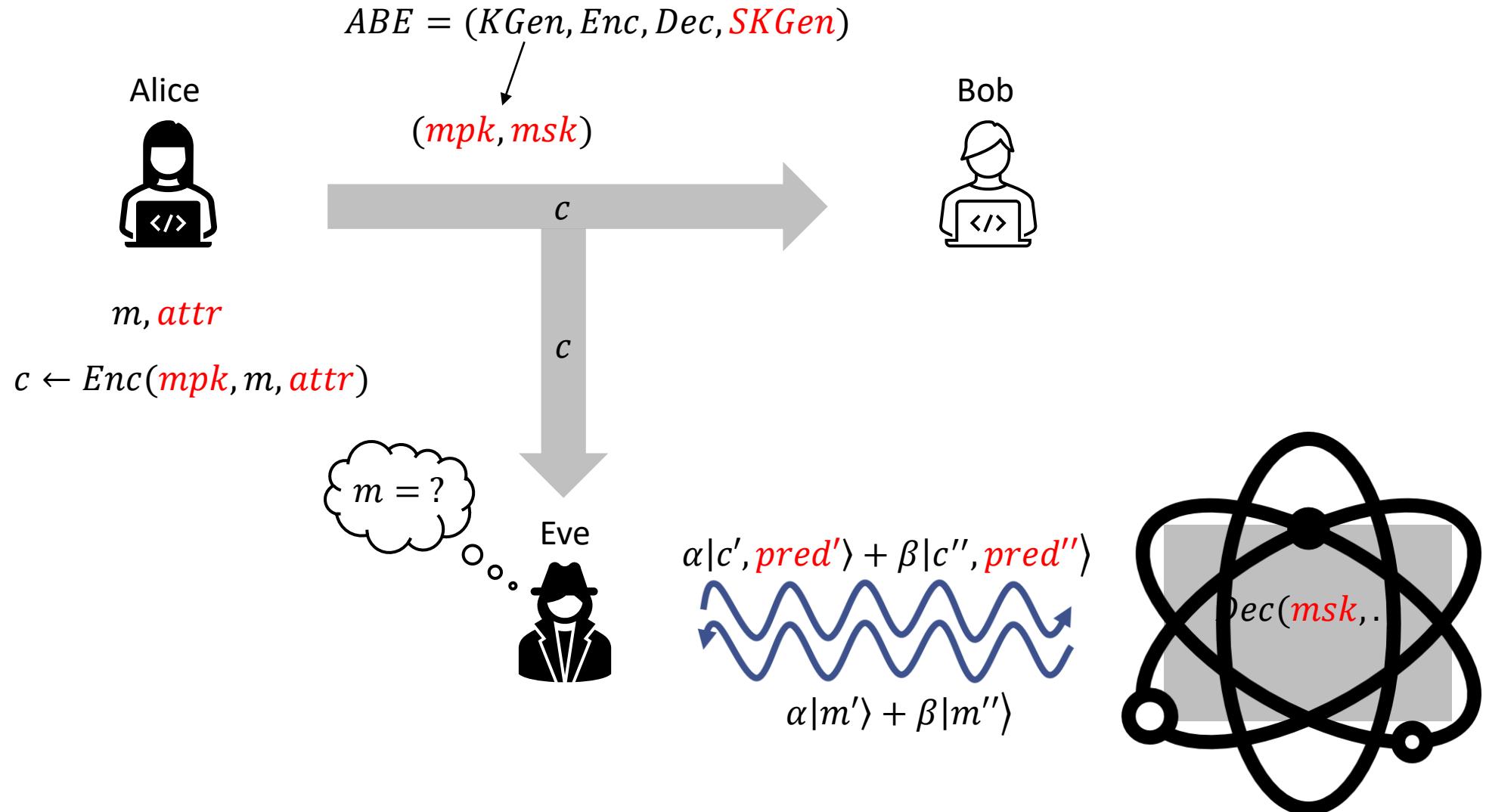
$$pred("Bob") = 1$$

$$pred(\cdot) = 0, \text{otherwise}$$

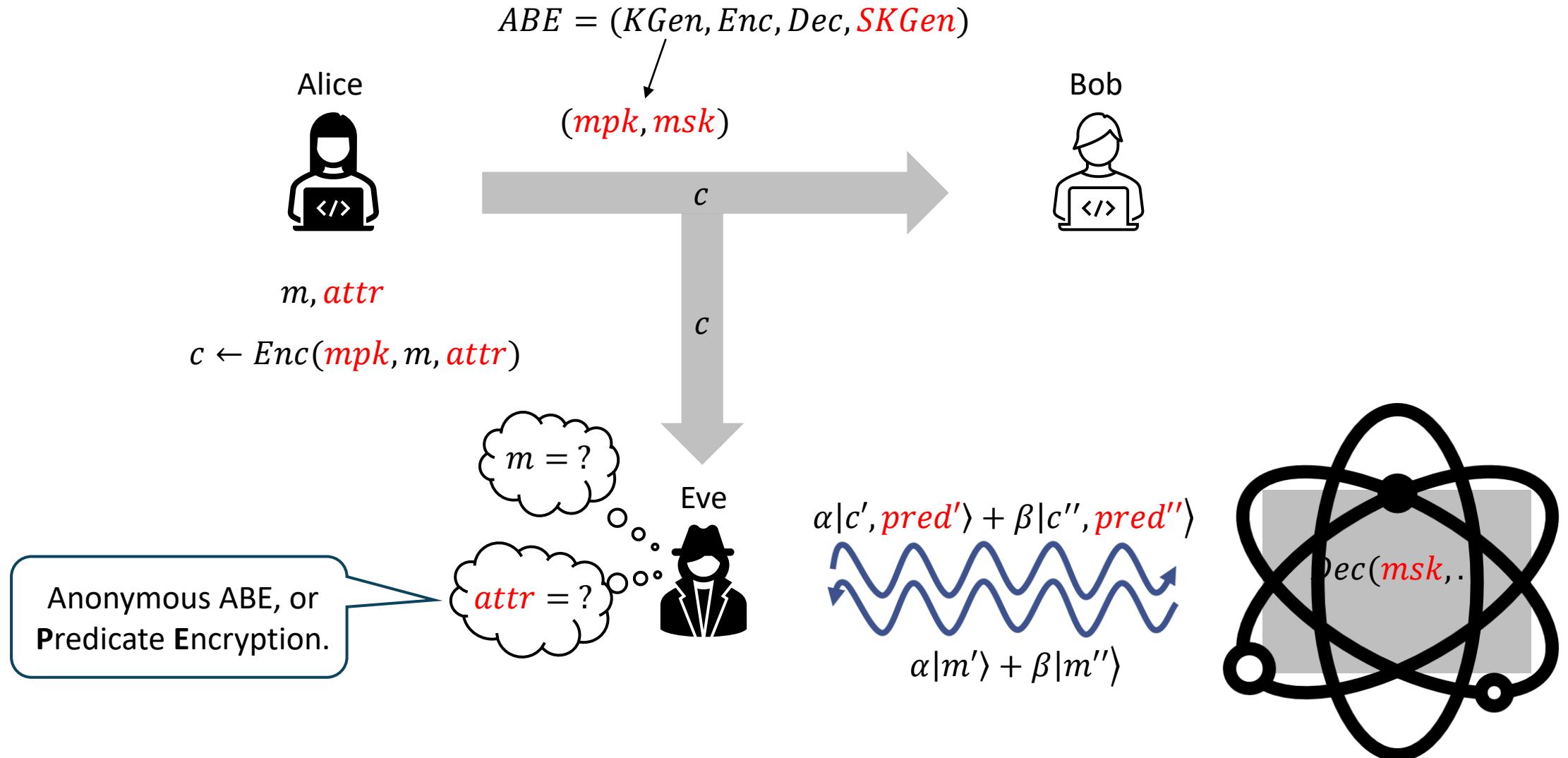
# IND-qCCA Secure PKE



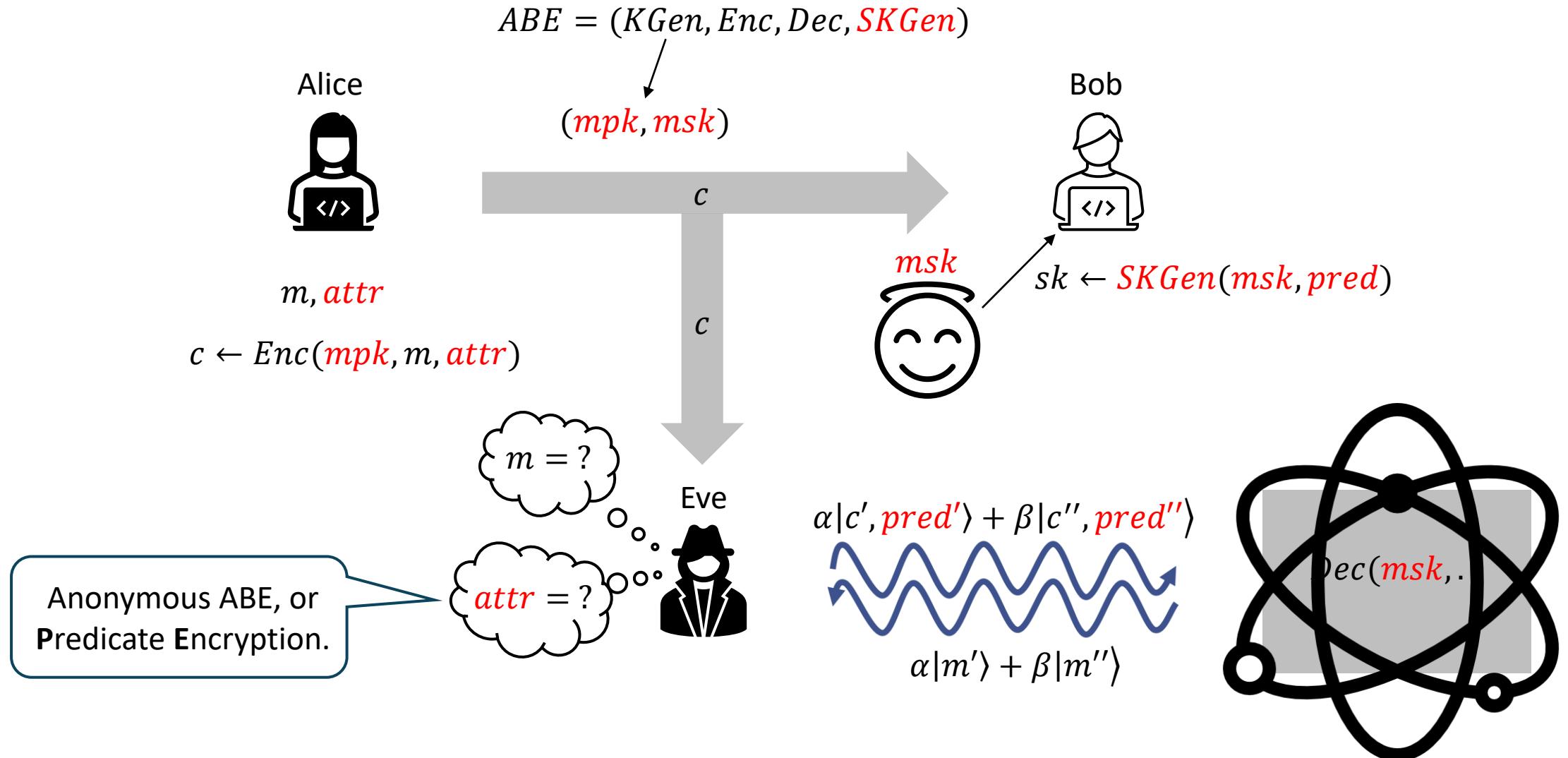
# IND-qCCA Secure ABE



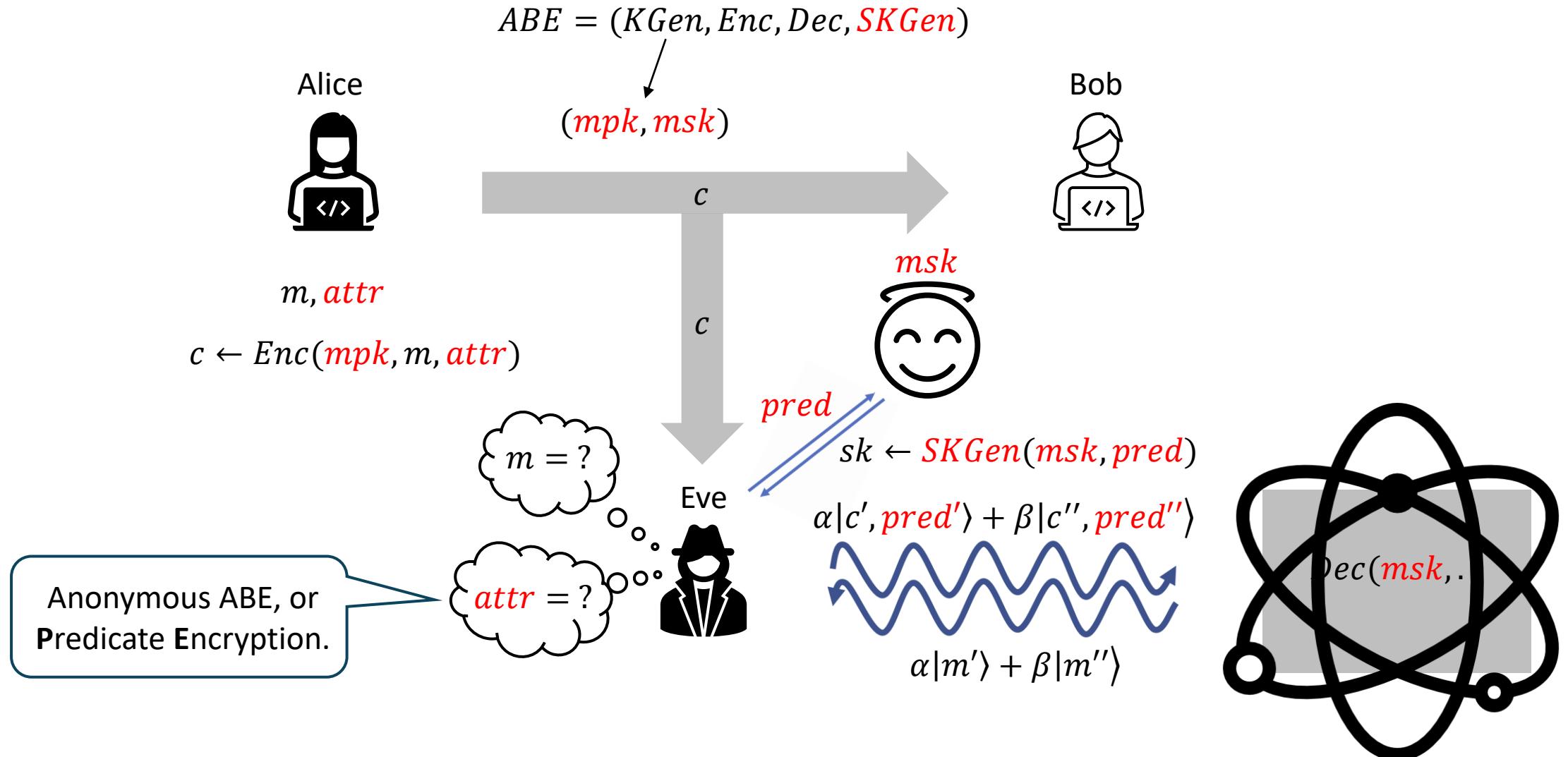
# IND-qCCA Secure ABE



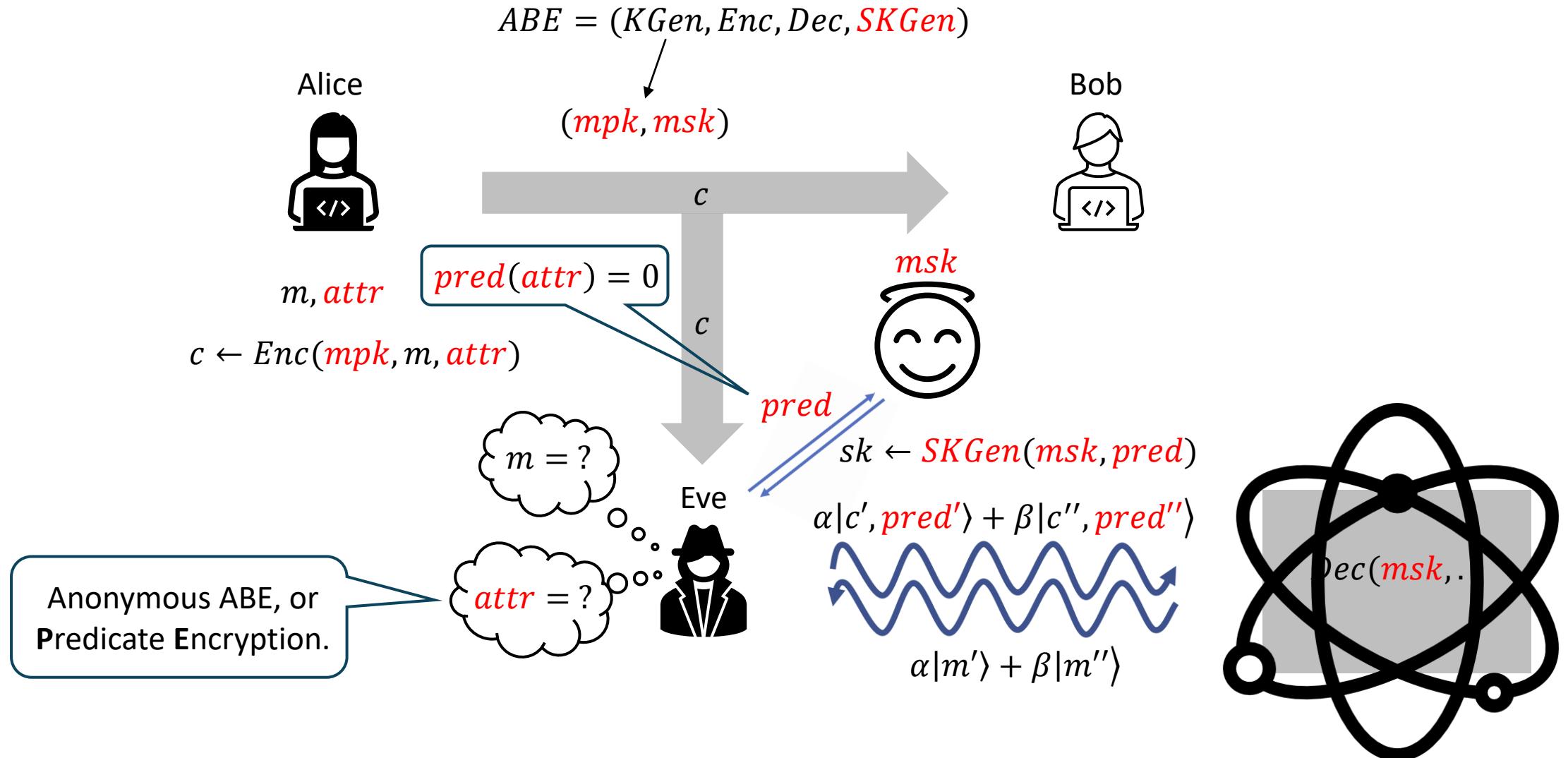
# IND-qCCA Secure ABE



# IND-qCCA Secure ABE



# IND-qCCA Secure ABE



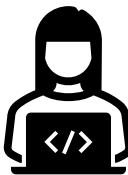
# IND-qCCA-CKG Secure ABE

Adversary can only make “classical” *SKGen* queries.

$$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$$

$$(mpk, msk)$$

Alice



Bob



$$m, attr$$

$$pred(attr) = 0$$

$$c \leftarrow Enc(mpk, m, attr)$$

*c*



*pred*

$$sk \leftarrow SKGen(msk, pred)$$

$$\alpha|c', pred'\rangle + \beta|c'', pred''\rangle$$

$$\alpha|m'\rangle + \beta|m''\rangle$$

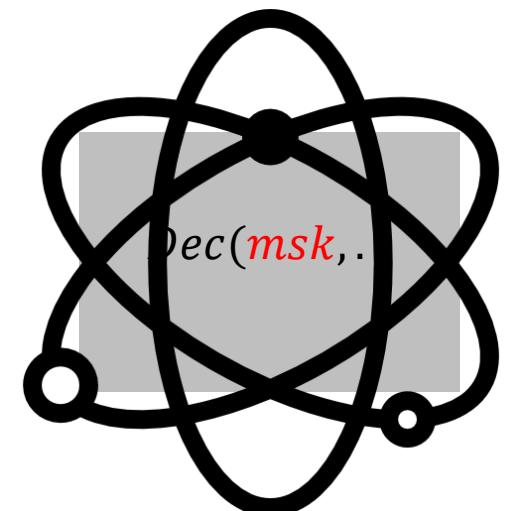
*m* = ?

*attr* = ?

Eve



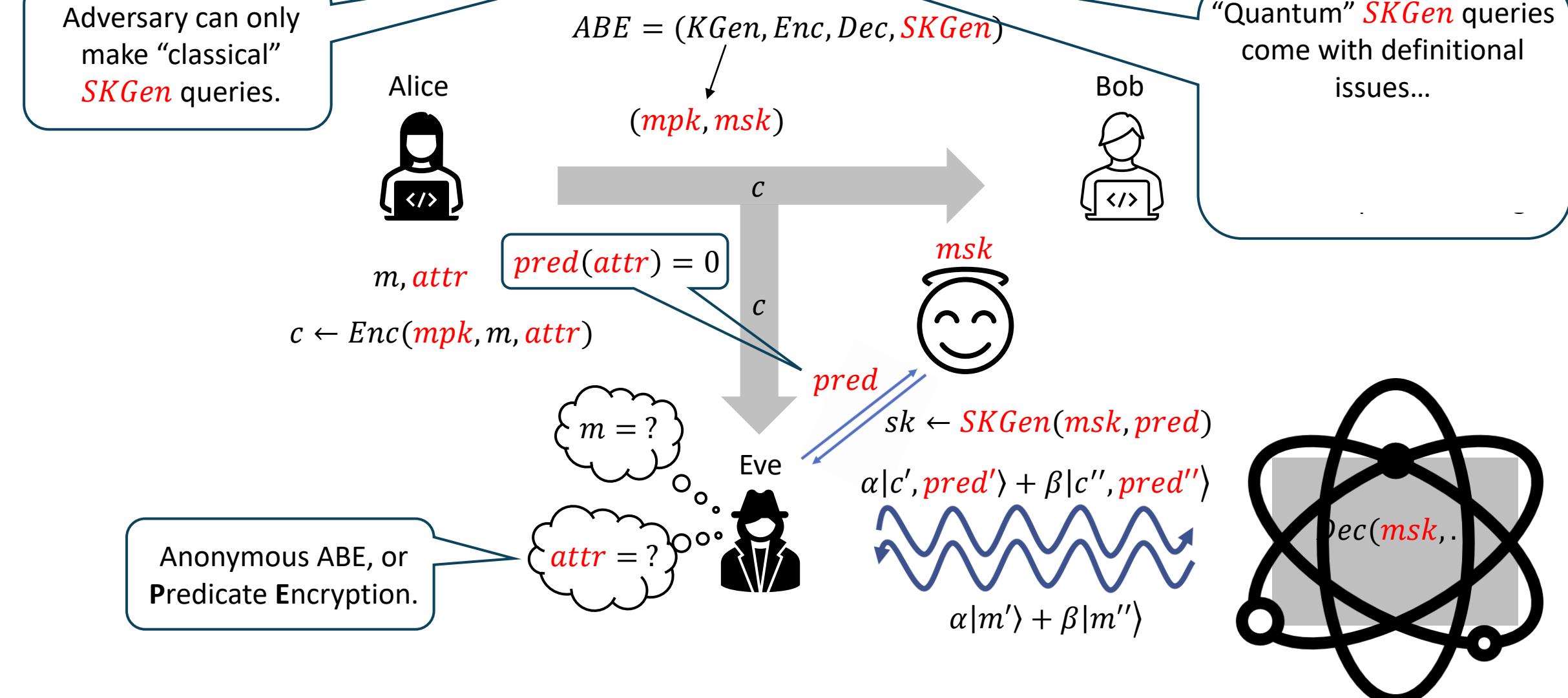
Anonymous ABE, or Predicate Encryption.



# IND-qCCA-CKG Secure ABE

Adversary can only make “classical” *SKGen* queries.

$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$



# IND-qCCA-CKG Secure ABE

Adversary can only make “classical” *SKGen* queries.

$ABE = (KGen, Enc, Dec, \textcolor{red}{SKGen})$

Alice



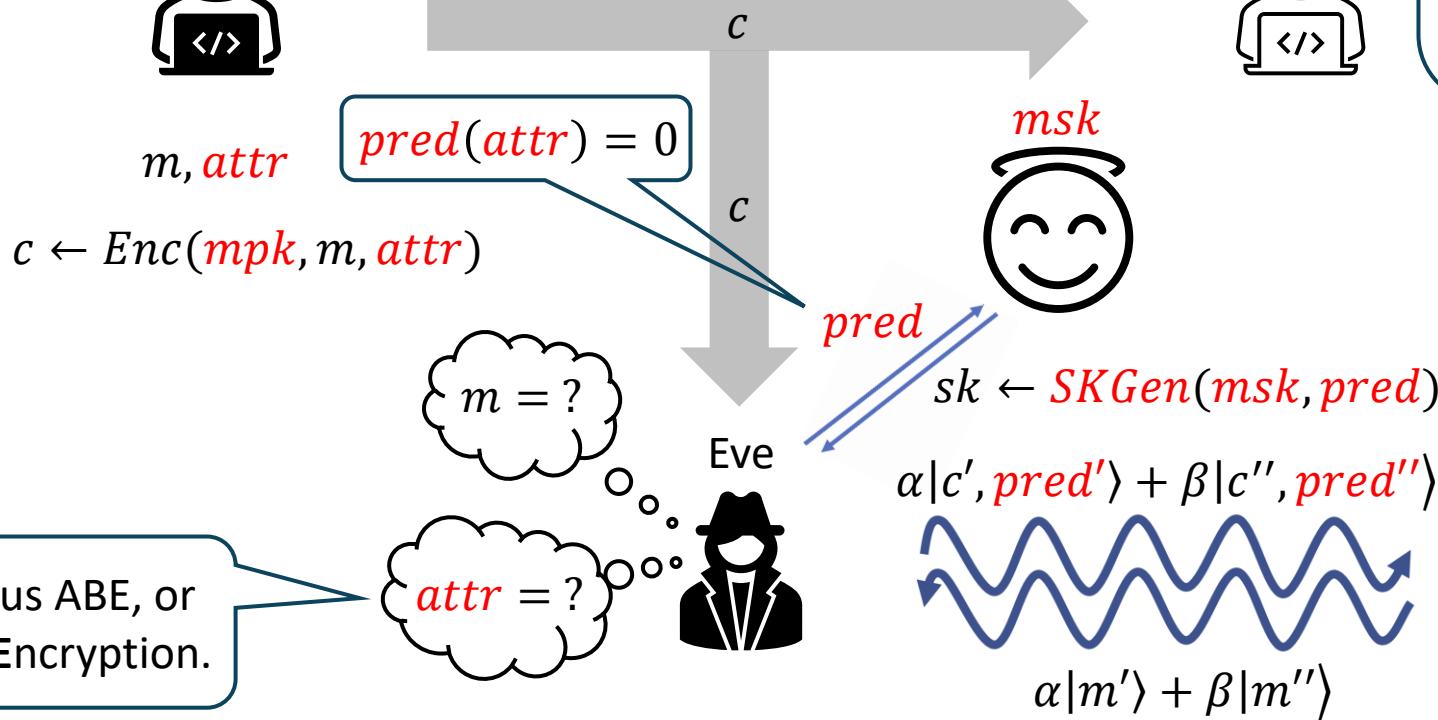
$(mpk, msk)$

Bob



“Quantum” *SKGen* queries come with definitional issues...

... but can be salvaged in a “semi-adaptive” setting.



# IND-**q**CCA-**c**KG Secure ABE

IND-CPA(-cKG) ABE

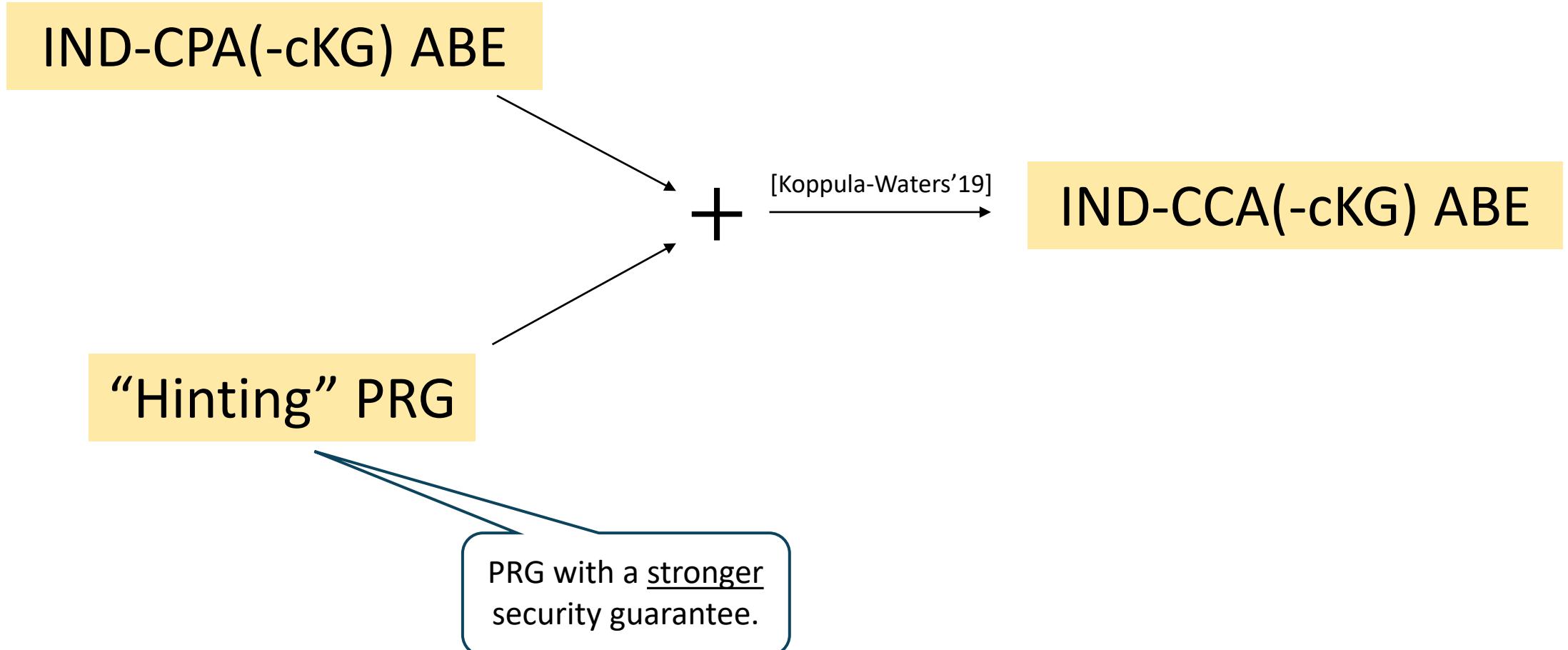
# IND-**q**CCA-**c**KG Secure ABE

IND-CPA(-cKG) ABE

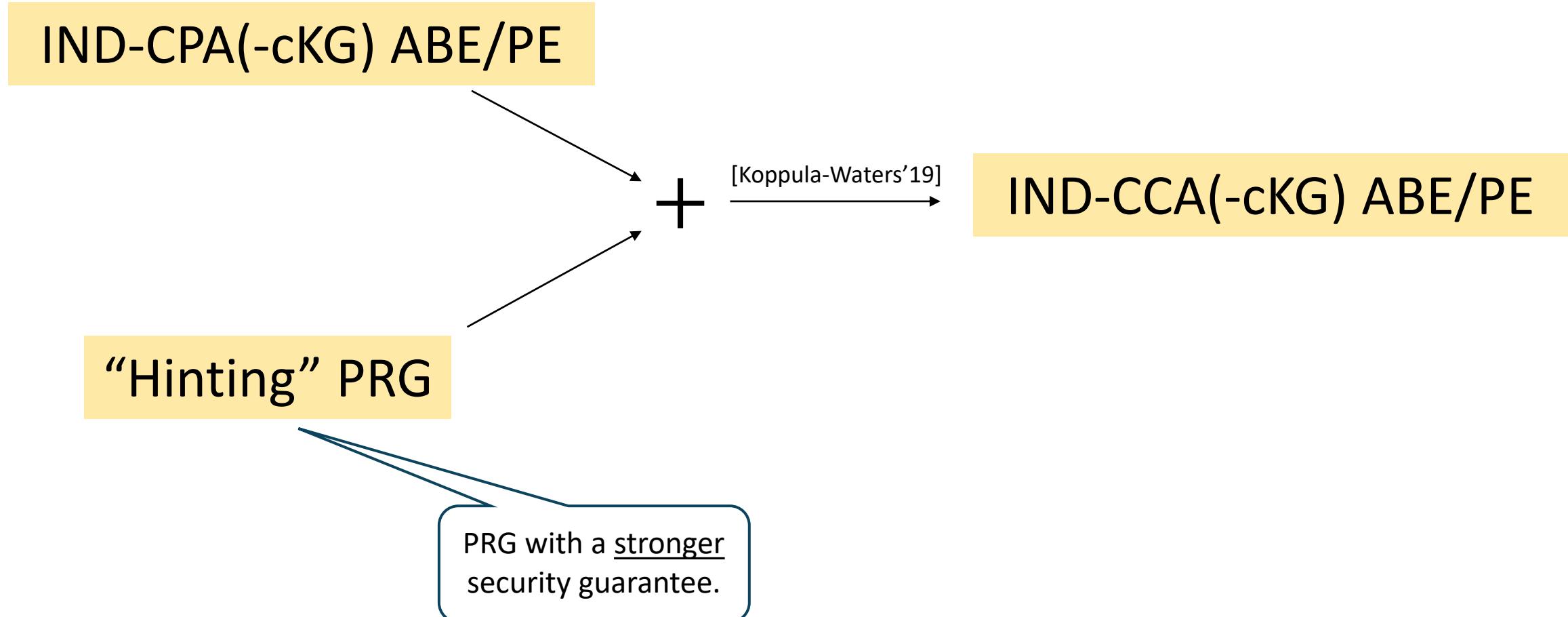
“Hinting” PRG

PRG with a stronger  
security guarantee.

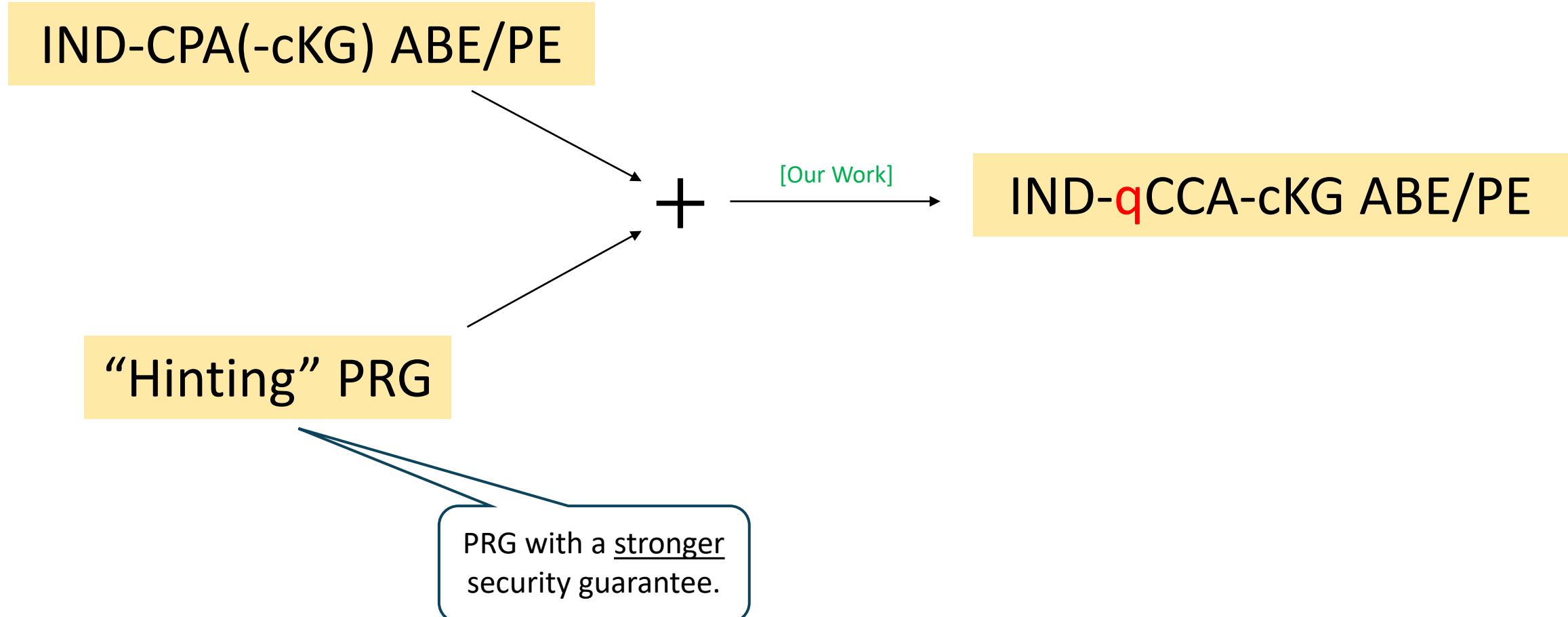
# IND-**q**CCA-**c**KG Secure ABE



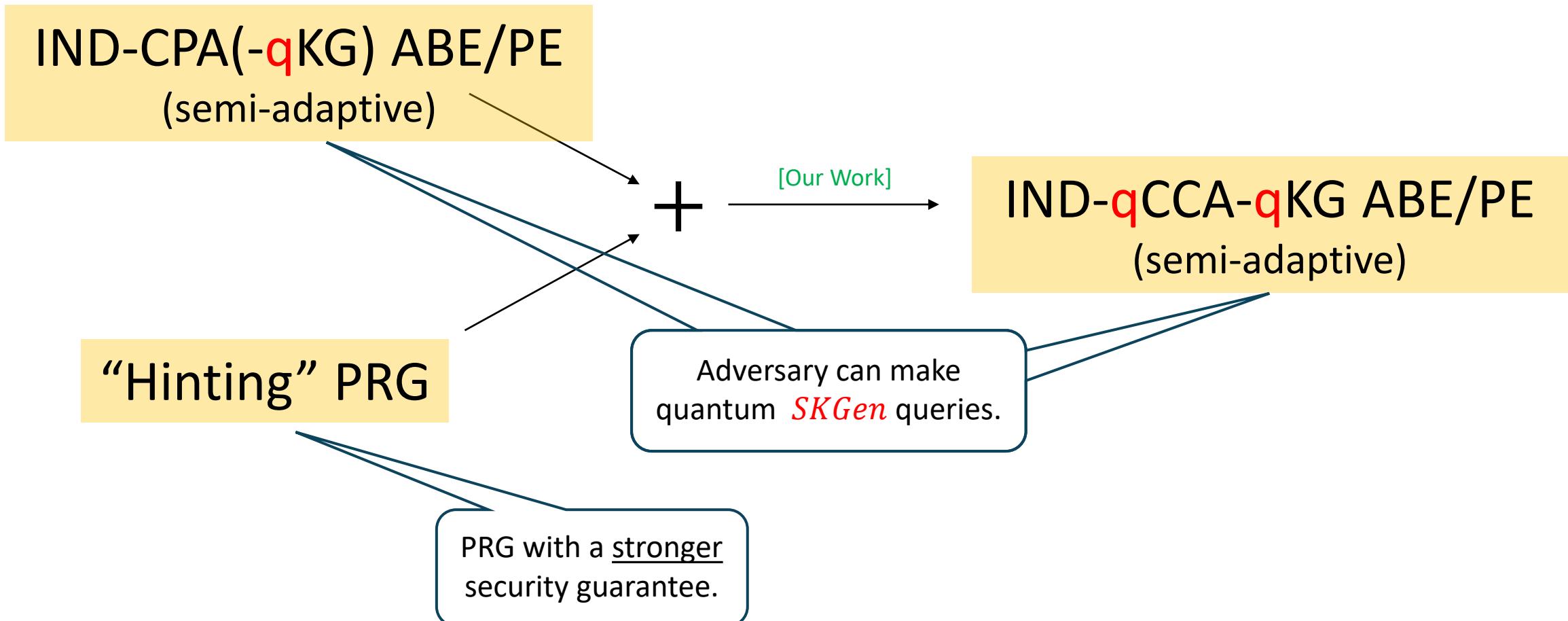
# IND-**q**CCA-**c**KG Secure ABE



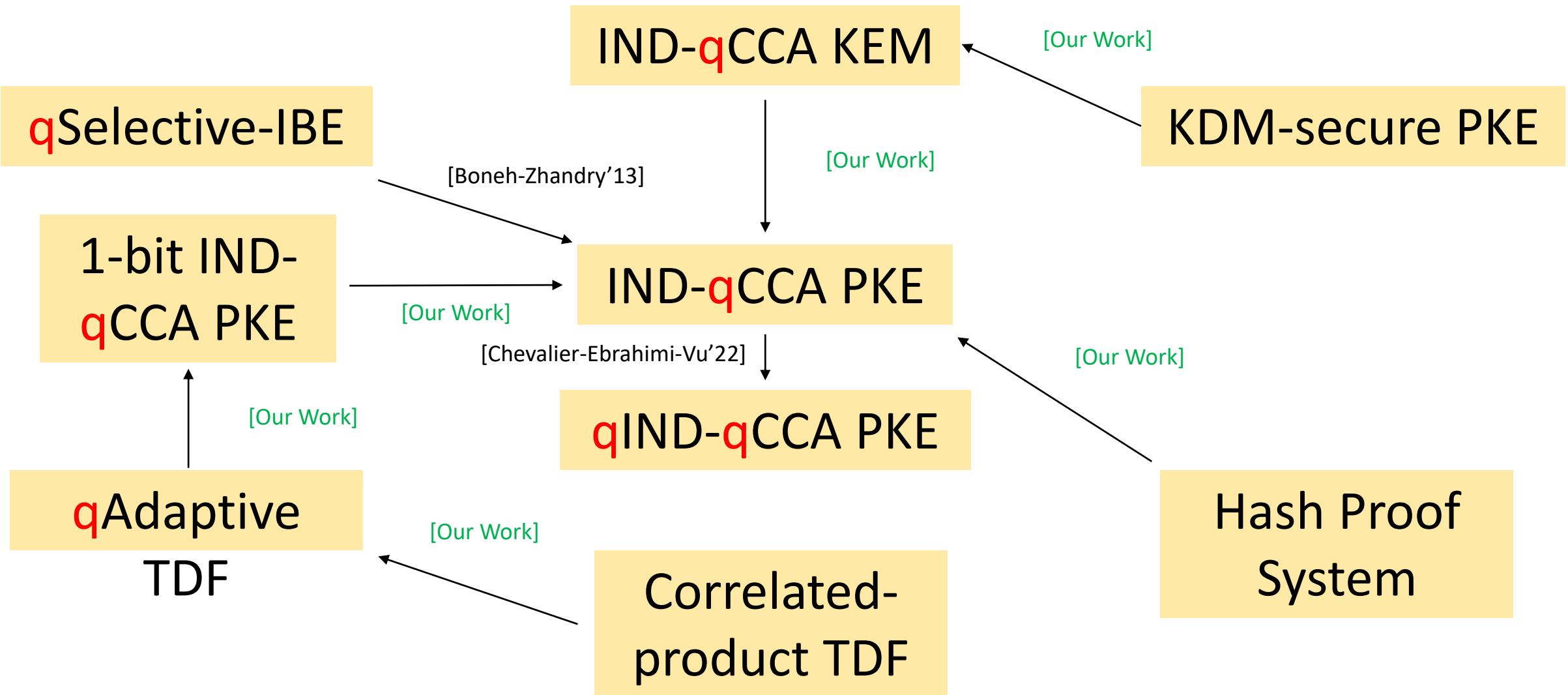
# IND-**q**CCA-**c**KG Secure ABE



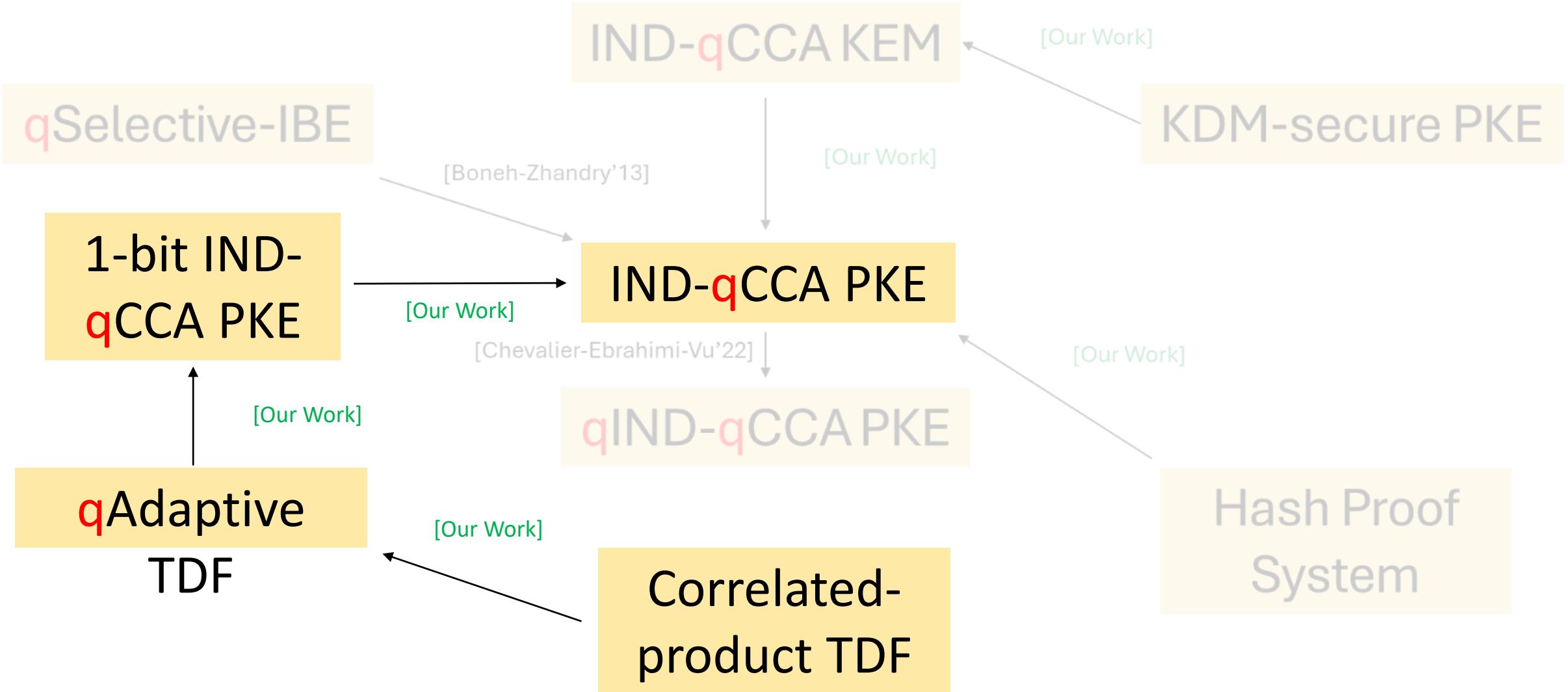
# IND-qCCA-qKG Secure ABE



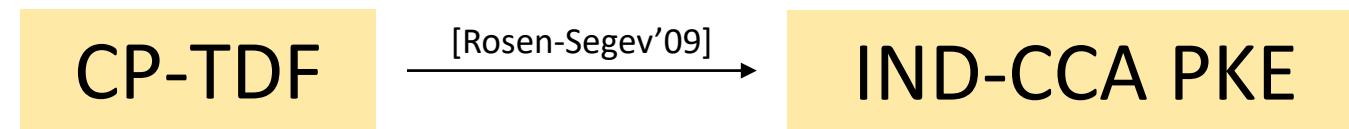
# Overview: Techniques



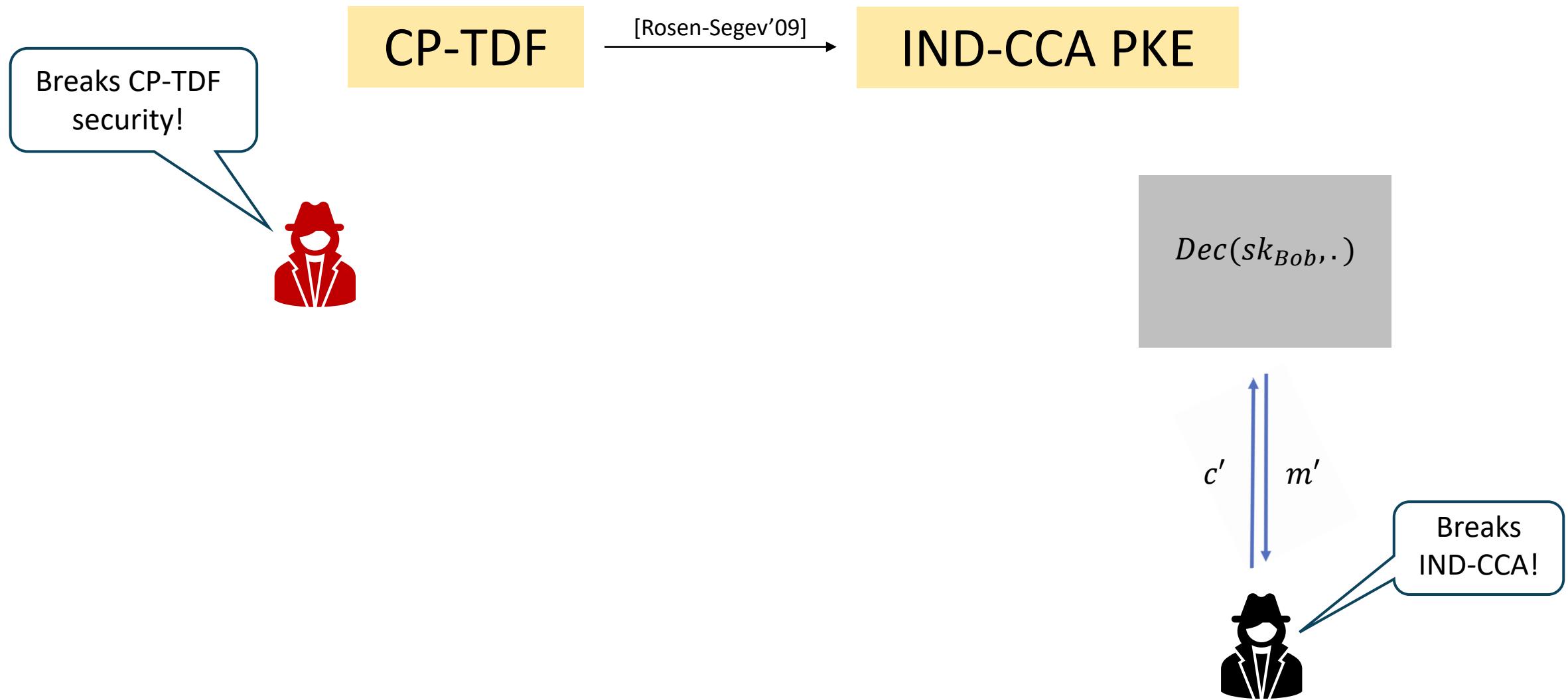
# Overview: Techniques



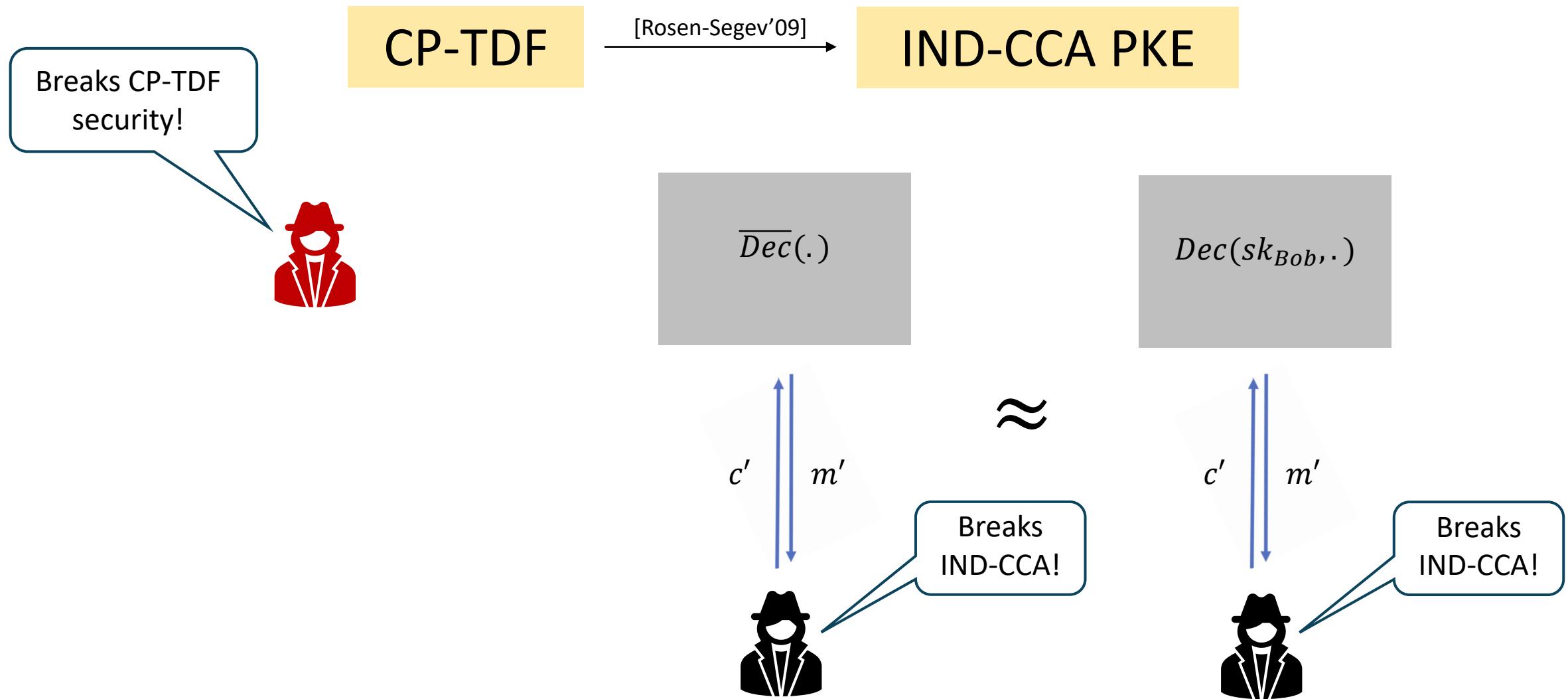
# Overview: Techniques



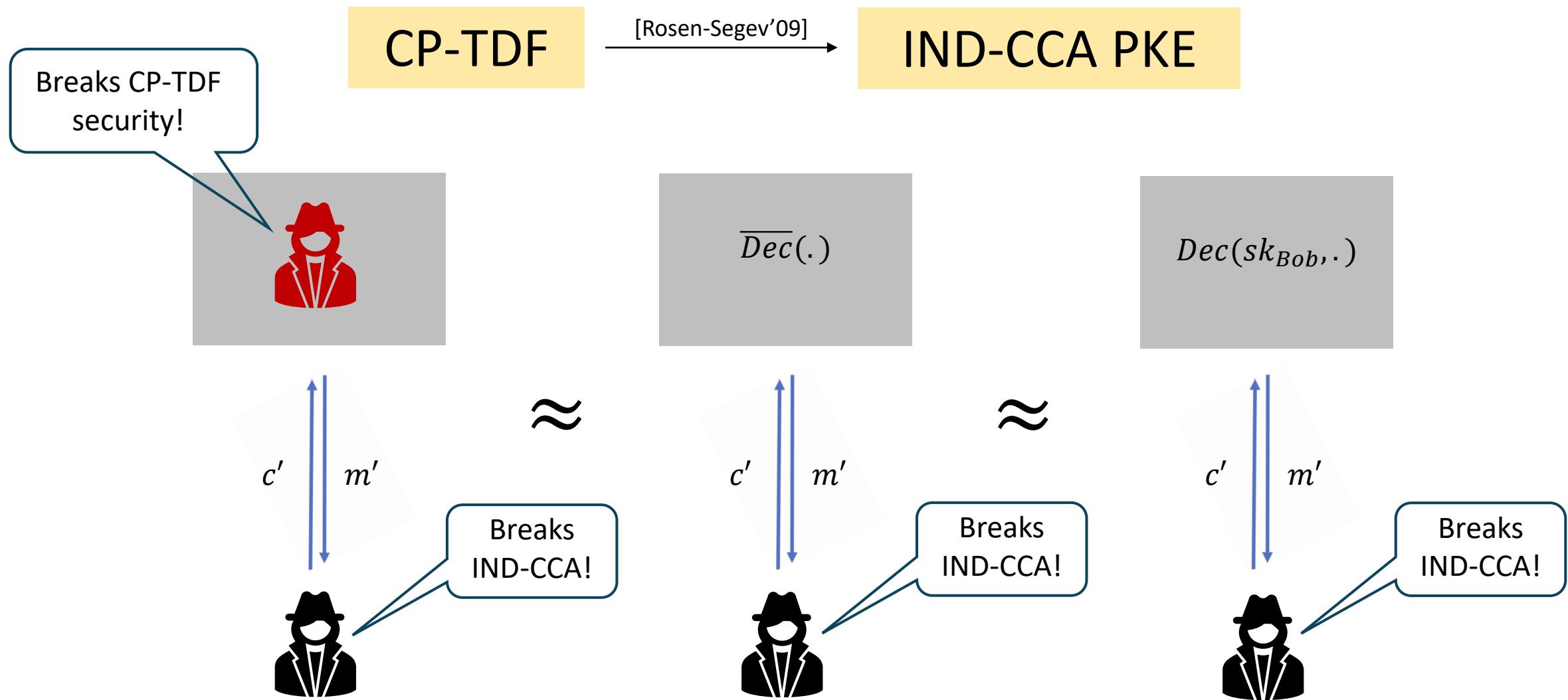
# Overview: Techniques



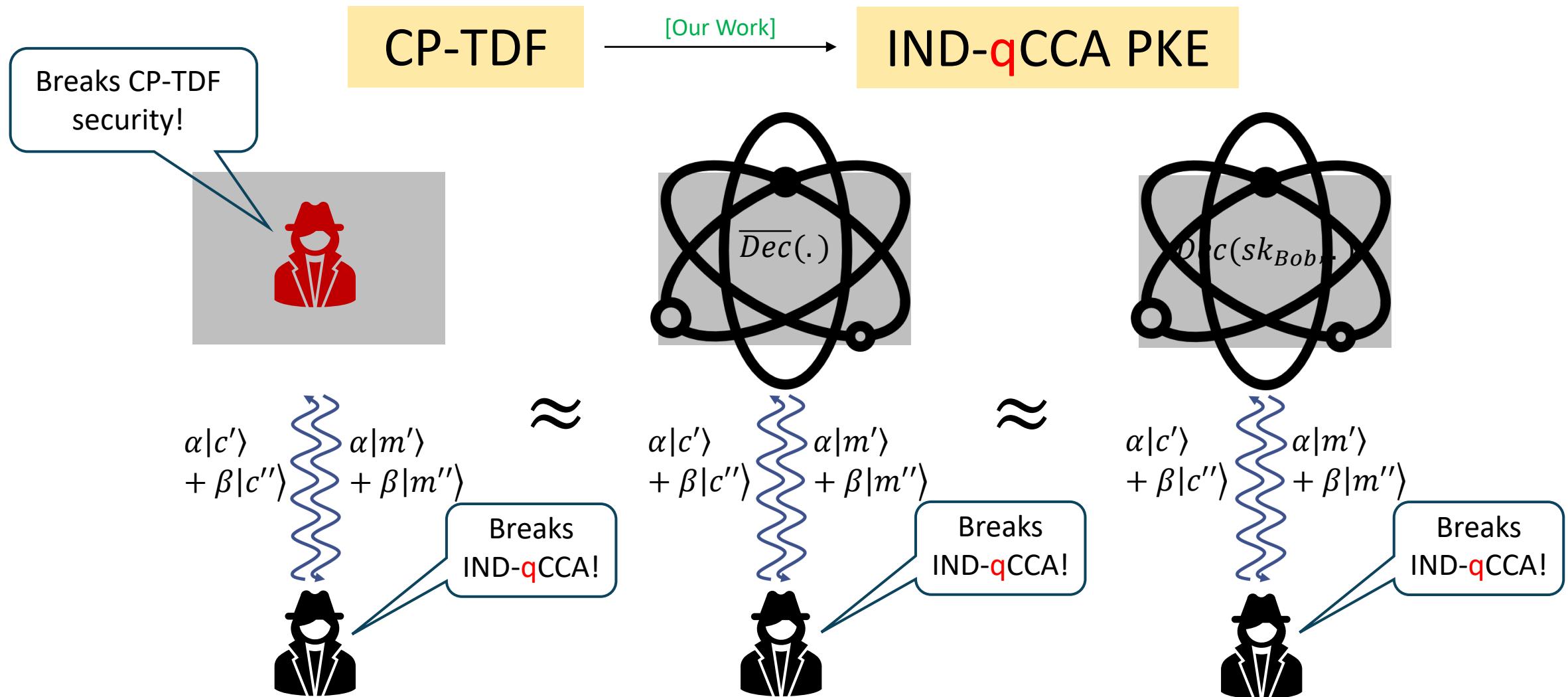
# Overview: Techniques



# Overview: Techniques

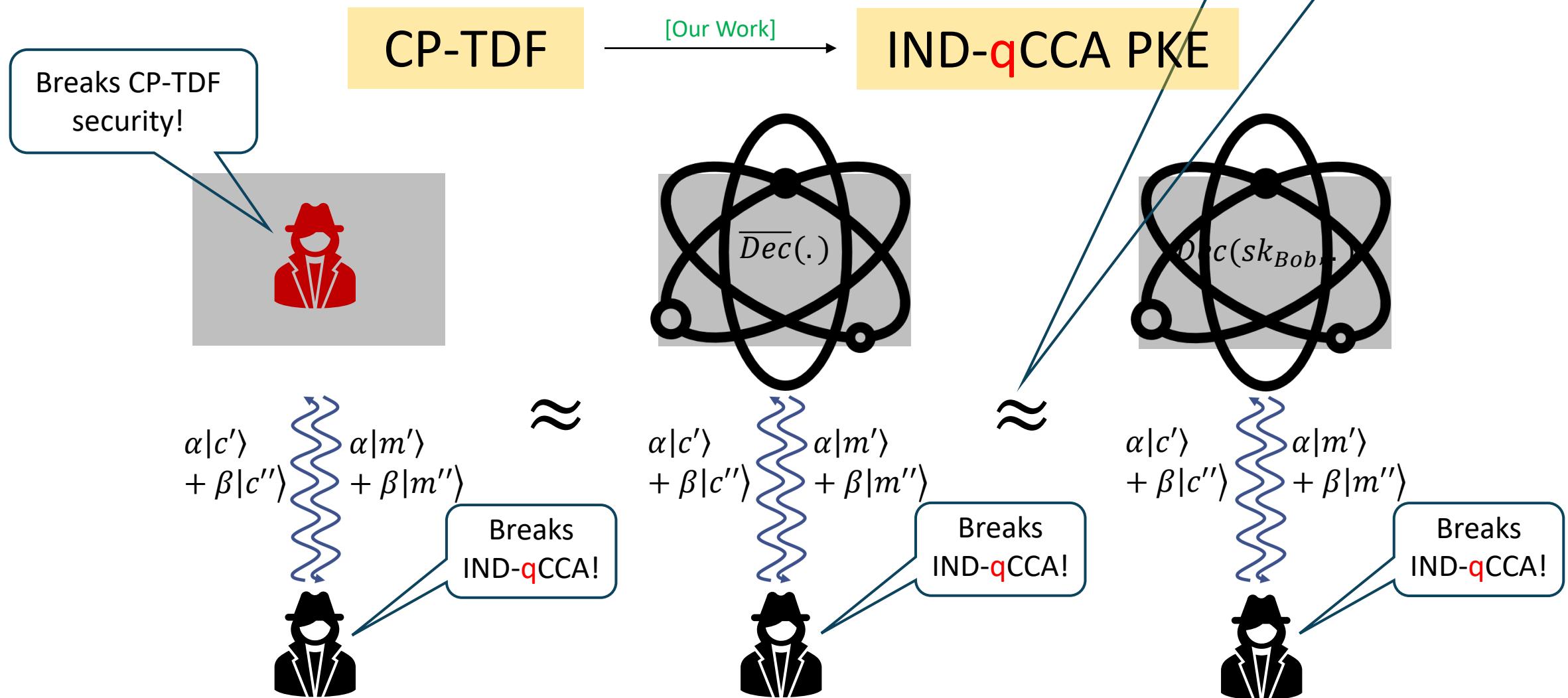


# Overview: Techniques



# Overview: Techniques

Showed using the **generalized OW2H lemma** of [Ambainis-Hamburg-Unruh'19].



Showed using the generalized OW2H lemma of [Ambainis-Hurung-Unruh'18].

# Overview: Techniques

- The original “**One-Way To Hiding**” (**OW2H**) lemma of [Unruh’14] was used to argue indistinguishability of **quantum (uniformly) random oracles**.

Showed using the generalized OW2H lemma of [Ambainis-Hamburg-Unruh'19].

# Overview: Techniques

- The original “**One-Way To Hiding**” (**OW2H**) lemma of [Unruh’14] was used to argue indistinguishability of **quantum (uniformly) random oracles**.
- The lemma was later generalized by [Ambainis-Hamburg-Unruh’19] to handle quantum oracles with **arbitrary output distributions**.
- Our work involves the first application of the (generalized) OW2H

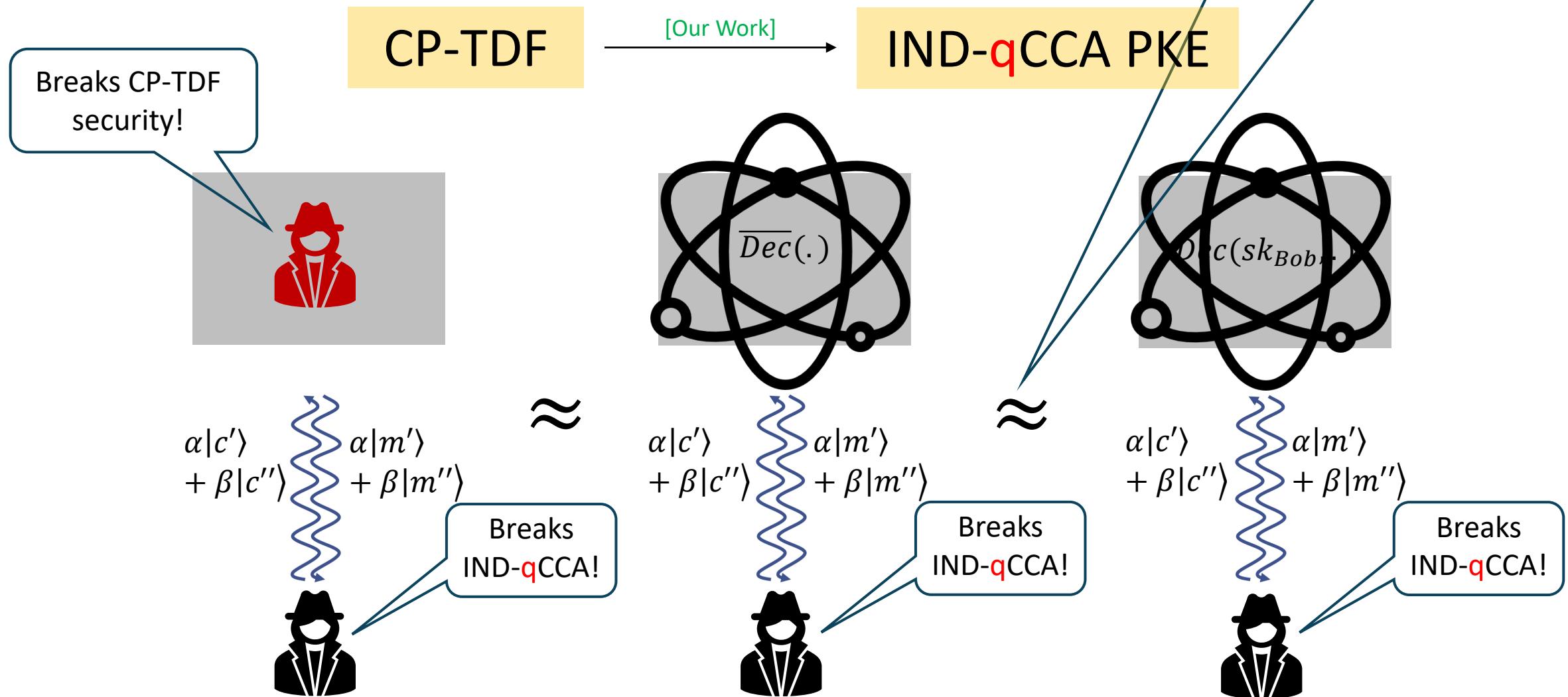
Showed using the generalized OW2H lemma of [Ambainis-Hamburg-Unruh'19].

# Overview: Techniques

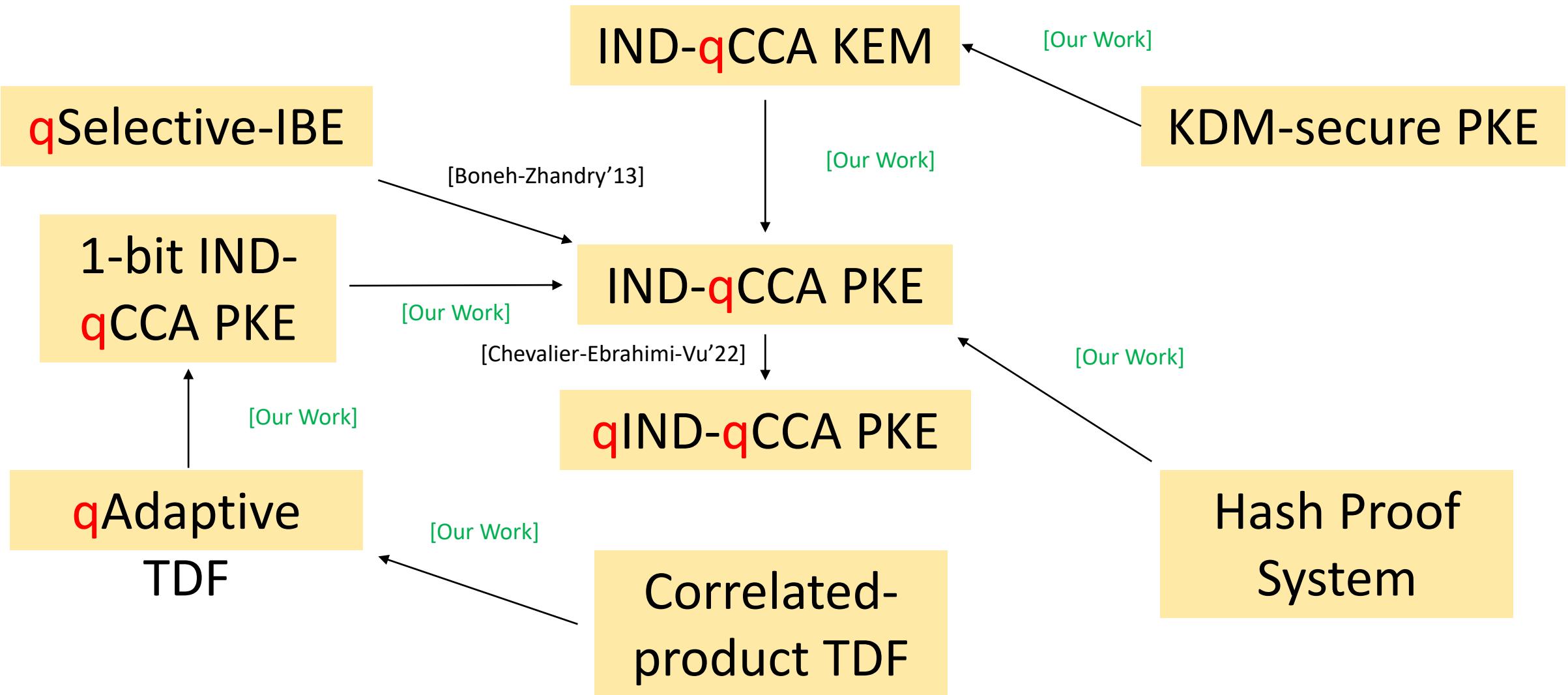
- The original “**One-Way To Hiding**” (**OW2H**) lemma of [Unruh’14] was used to argue indistinguishability of **quantum (uniformly) random oracles**.
- The lemma was later generalized by [Ambainis-Hamburg-Unruh’19] to handle quantum oracles with **arbitrary output distributions**.
- Our work involves the first application of the generalized OW2H lemma w.r.t. qCCA decryption oracles in the **standard model** – as opposed to the **QROM**.

# Overview: Techniques

Showed using the **generalized OW2H lemma** of [Ambainis-Hamburg-Unruh'19].

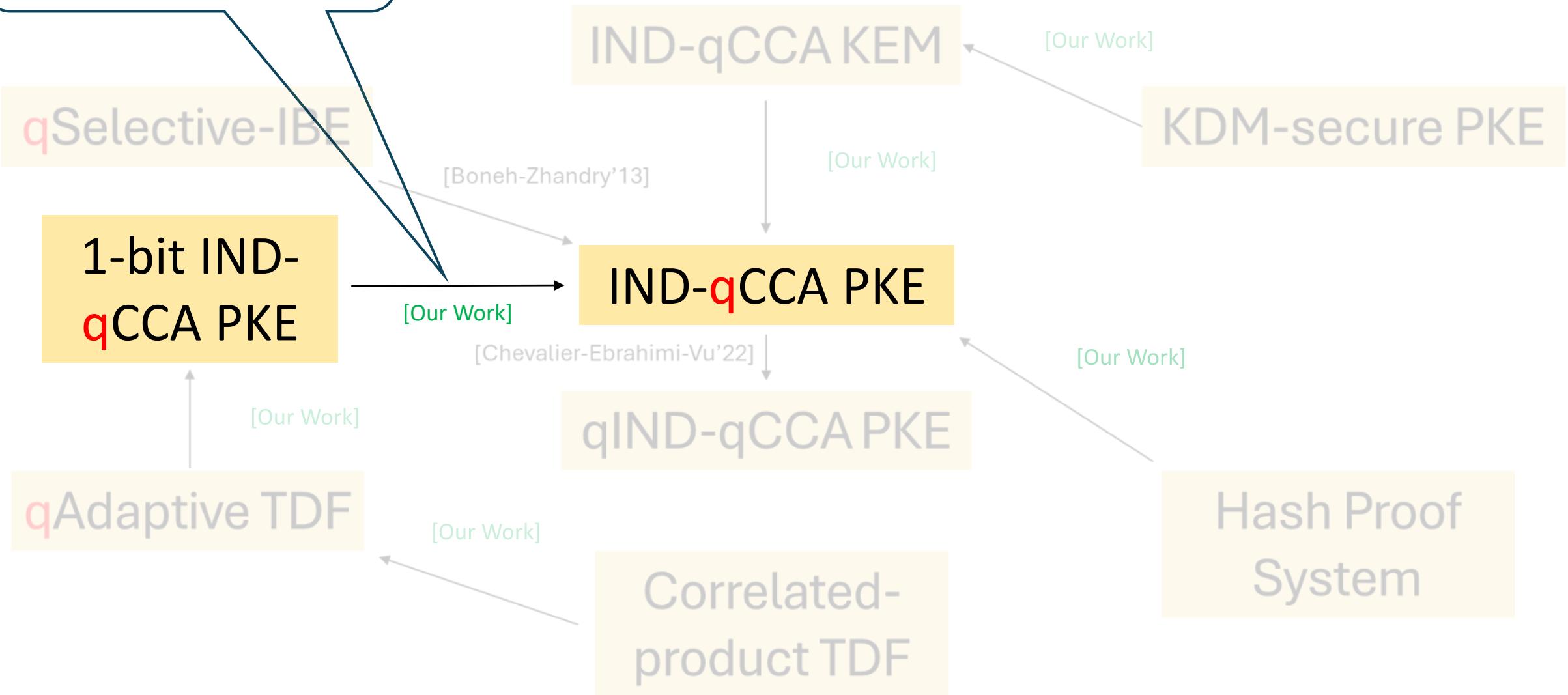


# Overview: Techniques



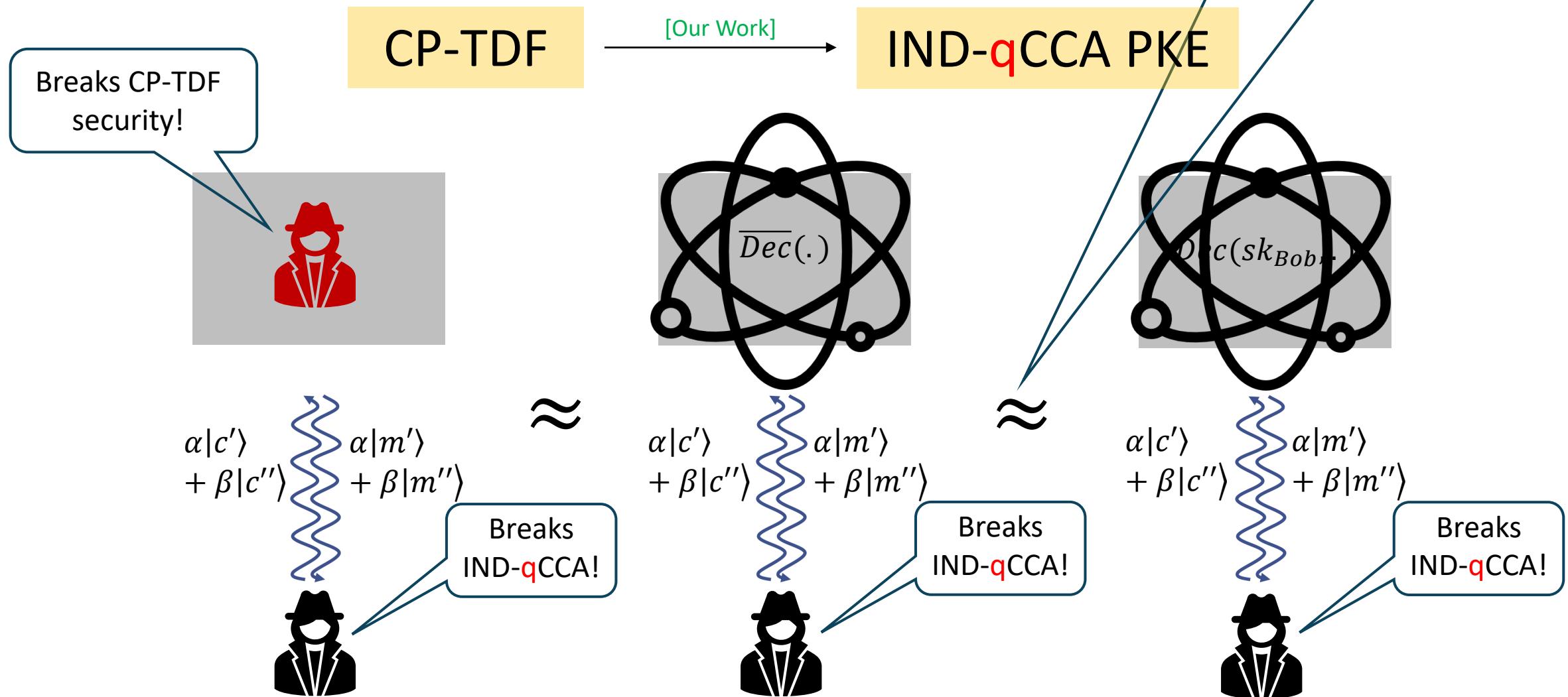
Required a “nested”  
**application** of the generalized  
OW2H lemma.

# Overview: Techniques



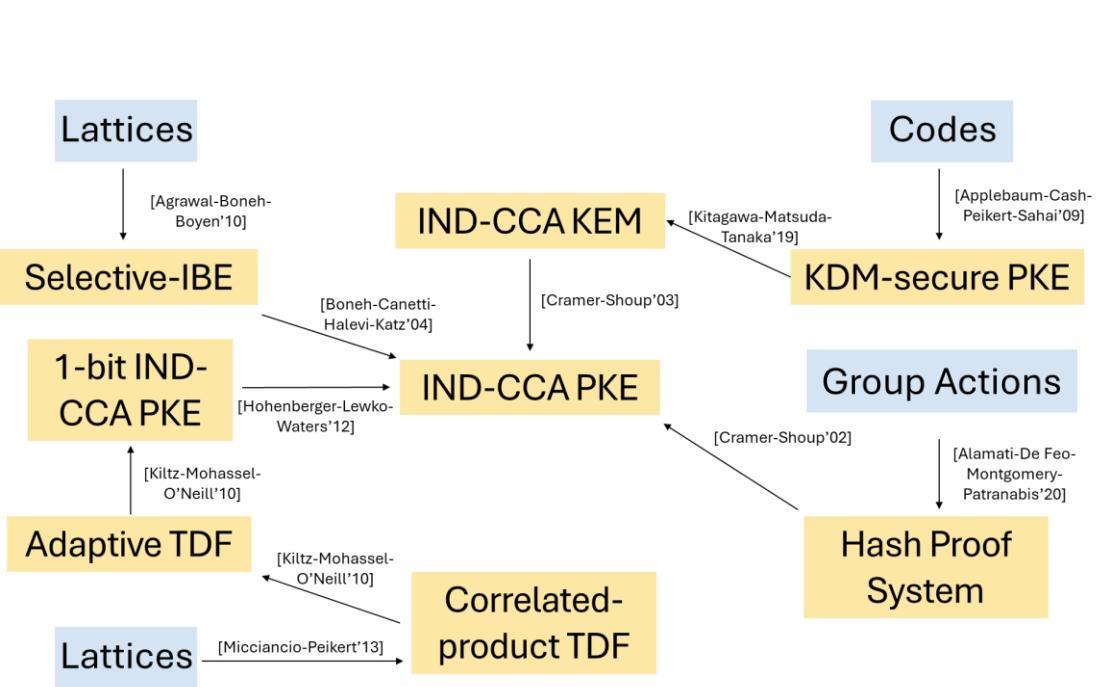
# Overview: Techniques

Showed using the **generalized OW2H lemma** of [Ambainis-Hamburg-Unruh'19].



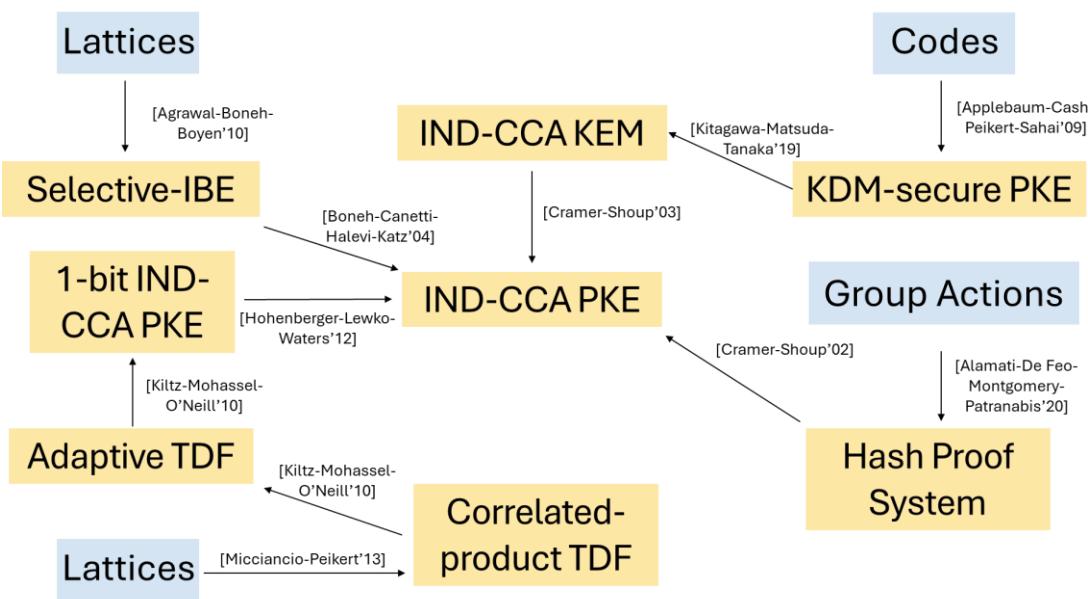
# Conclusion

# Conclusion

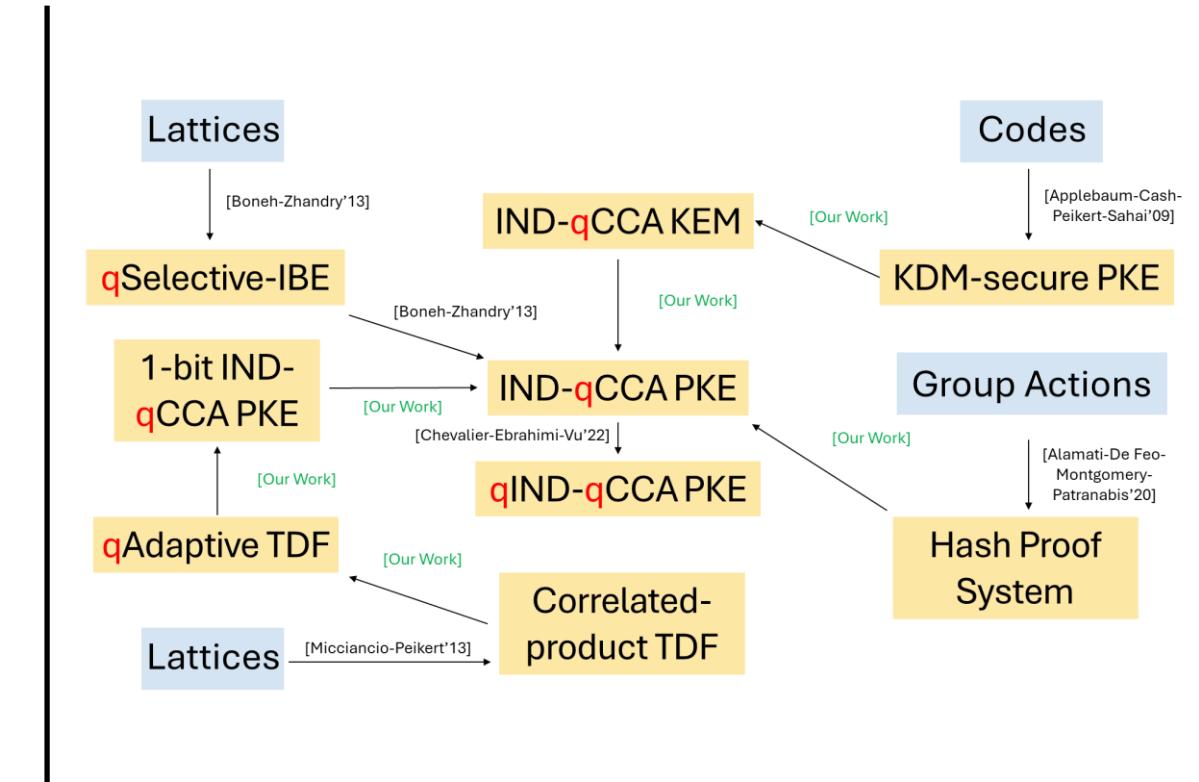


IND-CCA PKE

# Conclusion

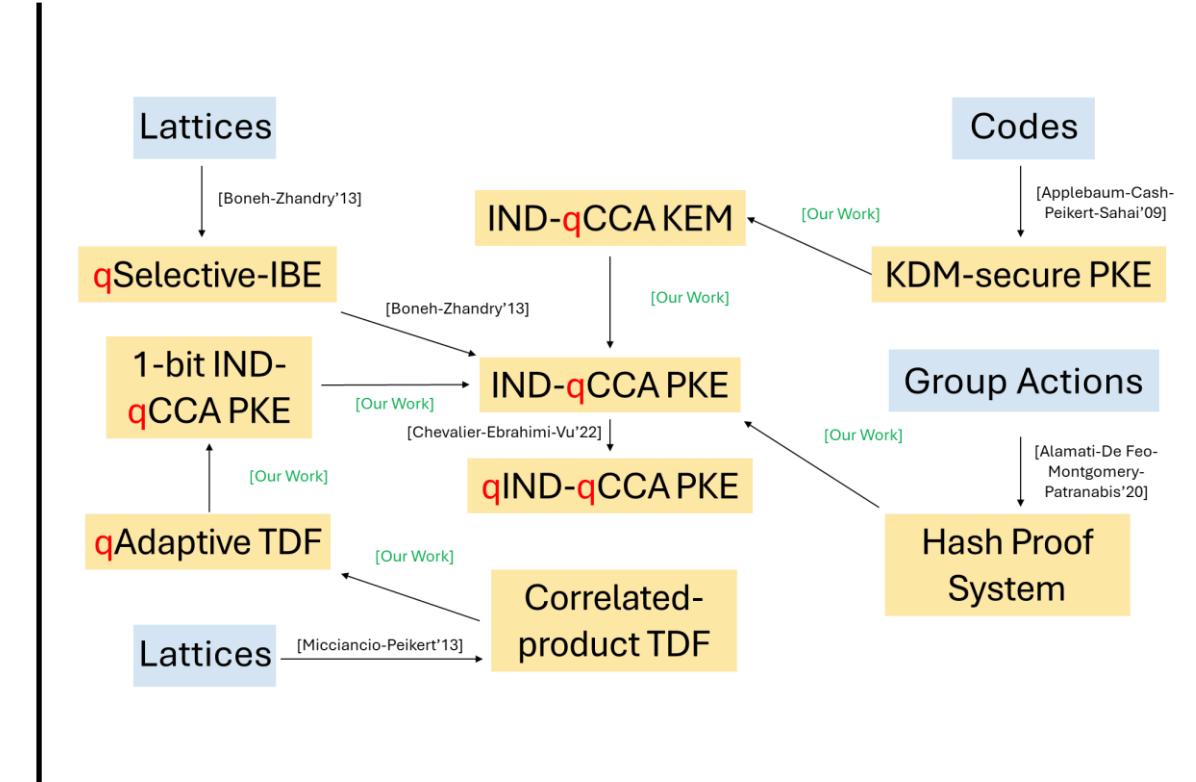
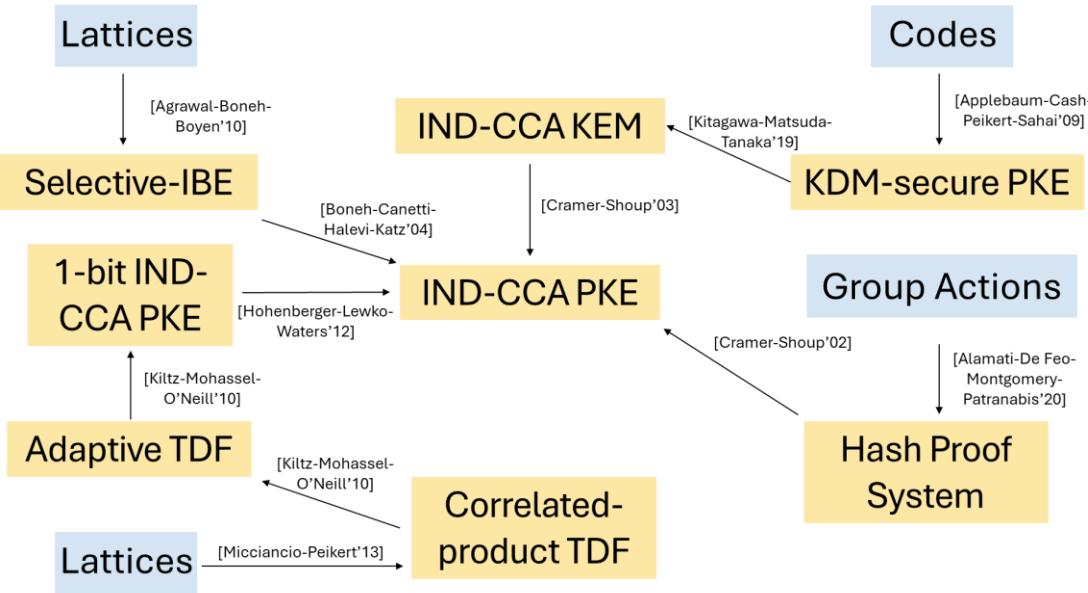


IND-CCA PKE



IND-qCCA PKE

# Conclusion



IND-CCA PKE

??

IND-qCCA PKE