Anonymous, Robust Post-Quantum Public Key Encryption

Varun Maram Applied Cryptography Group ETH Zurich



Joint work with Paul Grubbs and Kenneth G. Paterson [Full version of paper: <u>https://eprint.iacr.org/2021/708.pdf</u>]

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- But it is much more than that!

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... and more!

Under the Hood



Under the Hood

google.com	① rc4.badssl.com
	ScholarOne Manu 🦂 Editorial Manager® 🧧 💘 dblp: IACR Cryptol
Connection is secure	
Your information (for example, passwords or credit	
card numbers) is private when it is sent to this	
site. Learn more	EL S
Location Block V	
	This site can't provide a secure connection
Certificate (Valid)	rc4.badssl.com uses an unsupported protocol.
	ERR_SSL_VERSION_OR_CIPHER_MISMATCH
Cookies (23 in use)	
Site settings	
	Details



Under the Hood – the TLS 1.3 Handshake <u>Client</u> <u>Server</u>



Under the Hood – the TLS 1.3 Handshake



Bird's-eye View



Bird's-eye View



Bird's-eye View





Polynomial-Time Algorithms for Prime Factorization and Discrete Logarithms on a Quantum Computer^{*}

Peter W. Shor[†]

Abstract

A digital computer is generally believed to be an efficient universal computing device; that is, it is believed able to simulate any physical computing device with an increase in computation time by at most a polynomial factor. This may not be true when quantum mechanics is taken into consideration. This paper considers factoring integers and finding discrete logarithms, two problems which are generally thought to be hard on a classical computer and which have been used as the basis of several proposed cryptosystems. Efficient randomized algorithms are given for these two problems on a hypothetical quantum computer. These algorithms take a number of steps polynomial in the input size, e.g., the number of digits of the integer to be factored.

[FOCS'94]













EXPERTS' ESTIMATES OF THE LIKELIHOOD OF A QUANTUM COMPUTER ABLE TO BREAK RSA-2048 IN 24 HOURS

The experts were asked to indicate their estimate for the likelihood of a quantum computer that is cryptographically relevant—in the specific sense of being able to break RSA-2048 quickly—for various time frames, from a short term of 5 years all the way to 30 years.



[Image: Global Risk Institute, 2021 Quantum Threat Timeline Report]

















Conventional public-key cryptosystems that resist known quantum algorithms.

NIST Kicks Off Effort to Defend Encrypted Data from Quantum Computer Threat

April 28, 2016

road ahead.



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If an exotic quantum computer is invented that could break the codes we depend on to protect confidential electronic information, what will we do to maintain our security and privacy? That's the overarching question posed by a new report from the National Institute of Standards and Technology (NIST), whose cryptography specialists are beginning the long journey toward effective answers.

NIST Internal Report (NISTIB) 8105: Report on Post-Quantum Cryotography details the status of research into quantum computers, which would exploit the often counterintuitive world of quantum physics to solve problems that are intractable for conventional computers. If such devices are ever built, they will be able to defeat many of our modern cryptographic systems, such as the computer algorithms used to protect online bank transactions. NISTIR 8105 outlines a long-term approach for avoiding this vulnerability before it arises.

MEDIA CONTACT

Chad Boutin charles.boutin@nist.gov (301) 975-4261

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Information Technology Laboratory Computer Security Division

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"It will be a long process involving public vetting of quantum-resistant algorithms," Moody said. "And we're not expecting to have just one winner. There are several systems in use that could be broken by a quantum computer public-key encryption and digital signatures, to take two examples—and we will need different solutions for each of those systems."


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NIST <u>Kicks Off Effort to Defend Encrypted</u> Computer Threat April 28, 2016	Data from Quantum	US National Institute for Standards in Technology
Final expectationFinal expectation	MEDIA CONTACT Chad Boutin charles.boutin@nist.gov= (301) 975-4261 Computer Security Division SIGN UP FOR UPDATES FROM NIST Enter Email Address	 Is a part of the US Department of Commerce.
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- They are often adopted by other standards bodies, e.g. IETF and ISO.

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PQC Standardization Process: Third Round Candidate Announcement

NIST is announcing the third round finalists of the NIST Post-Quantum Cryptography Standardization Process. More details are included in NISTIR 8309.

July 22, 2020

It has been almost a year and a half since the second round of the NIST PQC Standardization Process began. After careful consideration, NIST would like to announce the candidates that will be moving on to the third round.

Third Round Finalists	Alternate Candidates
Public-Key Encryption/KEMs	Public-Key Encryption/KEMs
Classic McEliece	BIKE
CRYSTALS-KYBER	FrodoKEM
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Third Round Finalists	Alternate Candidates		 Tung Chou, Academia Sinica Carlos Cid, Royal Holloway, University of London and Simula UiB Jan Gilcher, ETH Zürich
Public-Key Encryption/KEMs Classic McEliece CRYSTALS-KYBER NTRU SABER	Public-Key Encryption/KEMs BIKE ErodoKEM HQC NTRU Prime SIKE		 Tanja Lange, Eindhoven University of Technology Varun Maram, ETH Zürich Ingo von Maurich, self Rafael Misoczki, Google Ruben Niederhagen, University of Southern Denmark Kenneth G. Paterson, ETH Zürich Edoardo Persichetti, Florida Atlantic University Christiane Peters, self Peter Schwabe, Max Planck Institute for Security and Privacy & Radboud University Nicolas Sendrier, Inria Jakub Szefer, Yale University Cen Jung Tjhai, PQ Solutions Ltd. Martin Tomlinson, PO Solutions Ltd.

Alice













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NTRU	HQC	NIST intends to standardize one or more schemes that enable "semantically secure"
SABER	NTRU Prime	encryption or key encapsulation with respect to adaptive chosen ciphertext attack, for
	SIKE	general use. This property is generally denoted IND-CCA2 security in academic
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IND-CCA Security



IND-CCA Security



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Robustness





PQC and NIST

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