Post-quantum Cryptographic Analysis of SSH



Varun Maram



: https://varun-maram.github.io/



SandboxAQ

n : varun-maram-pqc

Joint work with Benjamin Benčina, Benjamin Dowling, and Keita Xagawa







Why Analyze SSH?

Why Analyze SSH?

Log in Sign up

Top 10 real-world cryptographic protocols.

Here are ten widely used real-world cryptographic protocols that help secure communication, authentication, and data integrity across various applications:

1. Transport Layer Security (TLS) / Secure Sockets Layer (SSL)

- Use Case: Secure web browsing (HTTPS), email encryption, VoIP, and more.
- **Description**: TLS (successor to SSL) encrypts data transmission between clients and servers to ensure confidentiality and integrity.

- Use Case: Secure remote access to servers and encrypted file transfers (SCP, SFTP).
- **Description**: Uses public-key cryptography and symmetric encryption to secure login sessions over an unsecured network.

TLS @ RWC (≥ 27 talks)

- A long answer to the simple question, "Is TLS provably secure?" [2012]
- On the Security of the TLS and DTLS Record Protocols [2013]
- On the Security of SSL/TLS [2014]
- Provable security of advanced properties of TLS and SSH [2014]
- Post-quantum key exchange for the **TLS** protocol from the ring learning with errors problem [2015]
- TLS 1.3 [2015]
- Lucky Microseconds: A Timing Attack on Amazon's s2n Implementation of TLS [2016]
- TLS 1.3: Real-World Design Constraints [2016]
- Where the Wild Warnings Are: The TLS Story [2016]
- On the Security of TLS 1.3 and QUIC Against Weaknesses in PKCS#1 v1.5 Encryption [2016]
- TLS at the scale of Facebook [2016]
- No More Downgrades: Protecting TLS from Legacy Crypto [2016]
- The OPTLS Protocol and TLS 1.3 [2016]
- Automated Verification of TLS 1.3: 0-RTT, Resumption and Delayed Authentication [2016]
- PRNG Failures and TLS Vulnerabilities in the Wild [2017]
- Concerto: A Methodology Towards Reproducible Analyses of TLS Datasets [2017]
- Productizing TLS Attacks: The Rupture API [2017]
- Reactive and proactive standardisation of TLS [2018]
- TLS ecosystem [2018]
- The Era of TLS 1.3: Measuring Deployment and Use with Active and Passive Methods [2020]
- The 9 Lives of Bleichenbacher's CAT: New Cache ATtacks on TLS Implementations [2020]
- Deco: Liberating Web Data Using Decentralized Oracles for TLS [2020]
- Raccoon Attack: Finding and Exploiting Most-Significant-Bit-Oracles in TLS-DH(E) [2021]
- Post-quantum TLS without handshake signatures [2021]
- Justifying Standard Parameters in the TLS 1.3 Handshake [2022]
- ALPACA: Application Layer Protocol Confusion Analyzing and Mitigating Cracks in TLS
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- TLS-Anvil: Adapting Combinatorial Testing for TLS Libraries [2023]

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SSH @ RWC (2 talks)

- Provable security of advanced properties of TLS and SSH [2014]
- Terrapin Attack: Breaking SSH Channel Integrity By Sequence Number Manipulation [2024]

Sign up

Why Analyze SSH?

Me after spending \$3,999



- Use Case: Secure remote access to servers and encrypted file transfers (SCP, SFTP).
- **Description**: Uses public-key cryptography and symmetric encryption to secure login sessions over an unsecured network.

Why Analyze SSH?

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SSH Protocol



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2. Secure Shell (SSH)

- Use Case: Secure remote access to servers and encrypted file transfers (SCP, SFTP).
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Prior Analyses



Prior Analyses



Server



Security of Hybrid Key Establishment using Concatenation

Adam Petcher and Matthew Campagna

Amazon Web Services

[ePrint '23]

• Prior works either analyze the hybrid key exchange in isolation, or...

Prior Analyses



Server



Security of Hybrid Key Establishment using Post-quantum sound CRYPTOVERIF and verification of hybrid TLS and SSH key-exchanges

Bruno Blanchet Inria, F-75012 Paris, France bruno.blanchet@inria.fr Charlie Jacomme Université de Lorraine, CNRS, Inria, LORIA, F-54000 Nancy, France charlie.jacomme@inria.fr

[CSF '24]

- Prior works either analyze the hybrid key exchange in isolation, or...
- ... analyze post-quantum SSH in unsuitable protocol models, such as "authenticated key exchange (AKE)".

#1: "Post-quantum SSH is cryptographically secure in practice."

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(*Analysis does not cover low-level implementation details.)

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Server



- [BDKSS14] proves security of SSH in the "authenticated and confidential channel establishment (ACCE)" model.
- However, analysis is in the classical Diffie-Hellman setting.

[BDKSS14]: F. Bergsma, B. Dowling, F. Kohlar, J. Schwenk, D. Stebila, *"Multi-ciphersuite Security of the Secure Shell (SSH) Protocol"*, CCS 2014



[S&P '25]

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Client



cular viewer and Google chro

Our Contributions

"Hybridize" with (plausibly) quantum-secure KEM.



"EUF-CMA"

(Buffered Stateful(existentially unforgeable)

Server



- We establish security of SSH in a PQextension of ACCE model that accounts for "harvest now, decrypt later" attacks.
- Analysis also captures forward secrecy ٠ (unlike the classical ACCE analysis in [BDKSS14]).
- We then prove corresponding PQ security ٠ properties of SSH primitives.

[BDKSS14]: F. Bergsma, B. Dowling, F. Kohlar, J. Schwenk, D. Stebila, "Multiciphersuite Security of the Secure Shell (SSH) Protocol", CCS 2014

PRF

"Pseudo-

random"

KEM

"IND-CPA"

(passive security)

"BSAE"

Authenticated

Encryption)

#2: "Post-quantum SSH <u>can</u> be more efficient, and eco(log|nom)ical."



and verification of hybrid TLS and SSH key-exchanges", CSF 2024



(*honest reaction)



[BlaJac24]: B. Blanchet, C. Jacomme, "Post-quantum sound CryptoVerif and verification of hybrid TLS and SSH key-exchanges", CSF 2024



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(*honest reaction)

Diffie-Hellman key-exchange, not secure against quantum attackers.

Our Contributions

<u>c</u>C

Security"

"IND-CCA"

(active security)

"Hybridize" with (plausibly) quantum-secure KEM.

History of PQC in SSH

- **2018/03** OpenSSH adds experimental support for XMSS signatures. Disabled by default.
- 2018/12 TinySSH added support for hybrid Streamlined NTRU Prime / X25519 KEM sntrup4591761x25519-sha512
- 2019/01 OpenSSH added interoperable implementation labeled as experimental
- 2020/12 OpenSSH replaces implementation with sntrup761x25519-sha512
- 2021/11 OpenSSH includes sntrup761x25519-sha512 in the default client/server algorithms proposal
- 2022/02 OpenSSH promotes this algorithm the highest-preference position



"Fujisaki-Okamoto" transform "IND-CPA"

(passive security)

D. Miller, "OpenSSH PQC: Past, Present, Future", RWPQC 2024 [BlaJac24]: B. Blanchet, C. Jacomme, "Post-quantum sound CryptoVerif and verification of hybrid TLS and SSH key-exchanges", CSF 2024



- PQ-SSH analysis of [BlaJac24] relies on ٠ **IND-CCA** secure (ephemeral) KEMs.
- Whereas our analysis relies on the weaker ٠ property of IND-CPA security.
- Our analysis suggests FO transform is not ٠ needed, which in turn can lead to performance improvements in PQ-SSH.



(*honest reaction)

 Table 1. IND-CCA vs IND-CPA benchmarks w.r.t. ephemeral KEMs in post-quantum SSH.

Scope	KEM	IND-CCA[s]	$\mathbf{IND}\text{-}\mathbf{CPA}[\mathbf{s}]$	$\mathbf{Speedup}[\%]$
Primitive-level	sntrup761 mlkem768	$2.8164 \cdot 10^{-2} 2.7853 \cdot 10^{-5}$	$\begin{array}{c} 2.7056 \cdot 10^{-2} \\ 1.3242 \cdot 10^{-5} \end{array}$	$3.93 \\ 52.46$
(CPU timings of all KEM operations)	sntrup761x25519-sha512 mlkem768x25519-sha256	$\begin{array}{c} 3.0290 \cdot 10^{-2} \\ 3.1412 \cdot 10^{-3} \end{array}$	$\begin{array}{c} 2.9105 \cdot 10^{-2} \\ 3.1015 \cdot 10^{-3} \end{array}$	3.91 1.26
Protocol-level (Networks timings of an SSH connection)	sntrup761x25519-sha512 mlkem768x25519-sha256	$0.1565 \\ 0.1325$	$0.1534 \\ 0.1316$	$\begin{array}{c} 1.98 \\ 0.68 \end{array}$



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S. Frolov, R. Misoczki, "Meta PQC Updates", RWPQC 2024 (https://x.com/bwesterb/status/1771958142147973390)



(*honest reaction)



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Email: varun.maram@sandboxaq.com

Email: keita.xagawa@tii.ae [S&P '25]



Q: "<u>Should</u> post-quantum SSH/TLS be made efficient, and eco(log|nom)ical?"



Sasha Frolov and Rafael Misoczki

- Key exchange is a (very) commonly performed operation at Meta
- Currently, "0.05% of CPU cycles in Meta's data centers are spent doing X25519 key exchange
- We hope this data point is useful for making cost estimates while defining PQC standards specs

This means

- Deploying post-quantum key exchange has a non-negligible capacity cost
- Apparently innocuous steps can cost hundreds of thousands or even millions of dollars a year
- e.g. extra hashing steps, like hashing randomness or hashing parts of the transcript, which are being discussed as part of finalizing Kyber specification
- Even if an extra step does not affect latency, the extra power usage/consumption of shared resources on highly parallel servers still has costs

Feedback? Write to sashafrolov@meta.com or rafam@meta.com.

"TLS, and not SSH, represents the major workload for Meta."

- Reviewer

S. Frolov, R. Misoczki, "Meta PQC Updates", RWPQC 2024 (https://x.com/bwesterb/status/1771958142147973390)



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Stebila, et al. Internet-Draft Expires 18 July 2025 ietf-tls-hybrid-design

[Page 15] January 2025

that the hash function is a dual-PRF.

As noted in Section 2, KEMs used in the manner described in this document MUST explicitly be designed to be secure in the event that the public key is reused, such as achieving IND-CCA2 security or having a transform like the Fujisaki-Okamoto transform applied. ML-KEM has such security properties. However, some other post-quantum KEMs designed to be IND-CPA-secure (i.e., without countermeasures such as the FO transform) are completely insecure under public key reuse; for example, some lattice-based IND-CPA-secure KEMs are vulnerable to attacks that recover the private key after just a few thousand samples [FLUHRER].

- IND-CCA secure KEMs defend against potential public key-reuse attacks in faulty TLS/SSH implementations.
- Is there a way to retain IND-CPA efficiency, while preventing such implementation errors from happening?

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- IND-CCA secure KEMs defend against potential public key-reuse attacks in faulty TLS/SSH implementations.
- Is there a way to retain IND-CPA efficiency, while preventing such implementation errors from happening?
- Or, should we formally analyze TLS/SSH in a "faulty/adversarial implementation" (i.e., kleptographic) model?
 - We might then have to rely on "<u>stronger-</u> <u>than-IND-CCA</u>" security of KEMs.

D. Stebila , S. Fluhrer , S. Gueron, "Hybrid key exchange in TLS 1.3" (https://datatracker.ietf.org/doc/draft-ietf-tls-hybrid-design/)

Efficient IND-CPA secure KEMs suffice for post-quantum SSH!



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Cool! Are such IND-CPA secure





Damien Miller (OpenSSH Maintainer) KEMs FIPS-compliant?

Efficient IND-CPA secure KEMs suffice for post-quantum SSH!

Cool! Are such IND-CPA secure KEMs FIPS-compliant?





Damien Miller (OpenSSH Maintainer)



Efficient IND-CPA secure KEMs suffice for post-quantum SSH!





Damien Miller (OpenSSH Maintainer)

Should NIST have an "on-ramp" process for IND-CPA secure KEMs w.r.t. key exchange protocols? Cool! Are such IND-CPA secure KEMs FIPS-compliant?

4.A.3 Security Definition for Ephemeral-Only Encryption/Key-Establishment While chosen ciphertext security is necessary for many existing applications (for example, nominally ephemeral key exchange protocols that allow key caching), it is possible to implement a purely ephemeral key exchange protocol in such a way that only passive security is required from the encryption or KEM primitive.

For these applications, NIST will consider standardizing an encryption or KEM scheme which provides semantic security with respect to chosen plaintext attack. This property is generally denoted *IND-CPA security* in academic literature.

NIST, "Call for Proposals for Post-Quantum Cryptography Standardization", December 2016

Post-quantum Cryptographic Analysis of SSH



Varun Maram



: https://varun-maram.github.io/



SandboxAQ

n : varun-maram-pqc

Joint work with Benjamin Benčina, Benjamin Dowling, and Keita Xagawa





